

# Evolution of Representations in the Transformer

Lena Voita

Based on EMNLP 2019 paper by Elena Voita<sup>1,2,3</sup>, Rico Sennrich<sup>4,2</sup>, Ivan Titov<sup>2,3</sup>

**Y**andex Research



THE UNIVERSITY  
*of* EDINBURGH



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University of  
Zurich<sup>UZH</sup>

# Words -> words in context

- Shift from static embeddings to contextualized word representations

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ELMo



Architecture: bi-LSTM

Training objective: LM

How: add ELMo representations  
to the task-specific model

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- Shift from static embeddings to contextualized word representations

ELMo

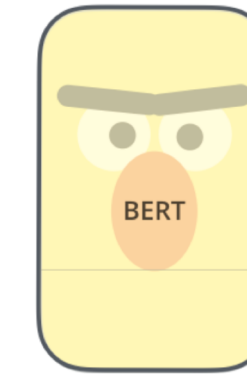


Architecture: bi-LSTM

Training objective: LM

How: add ELMo representations to the task-specific model

BERT



Architecture: Transformer

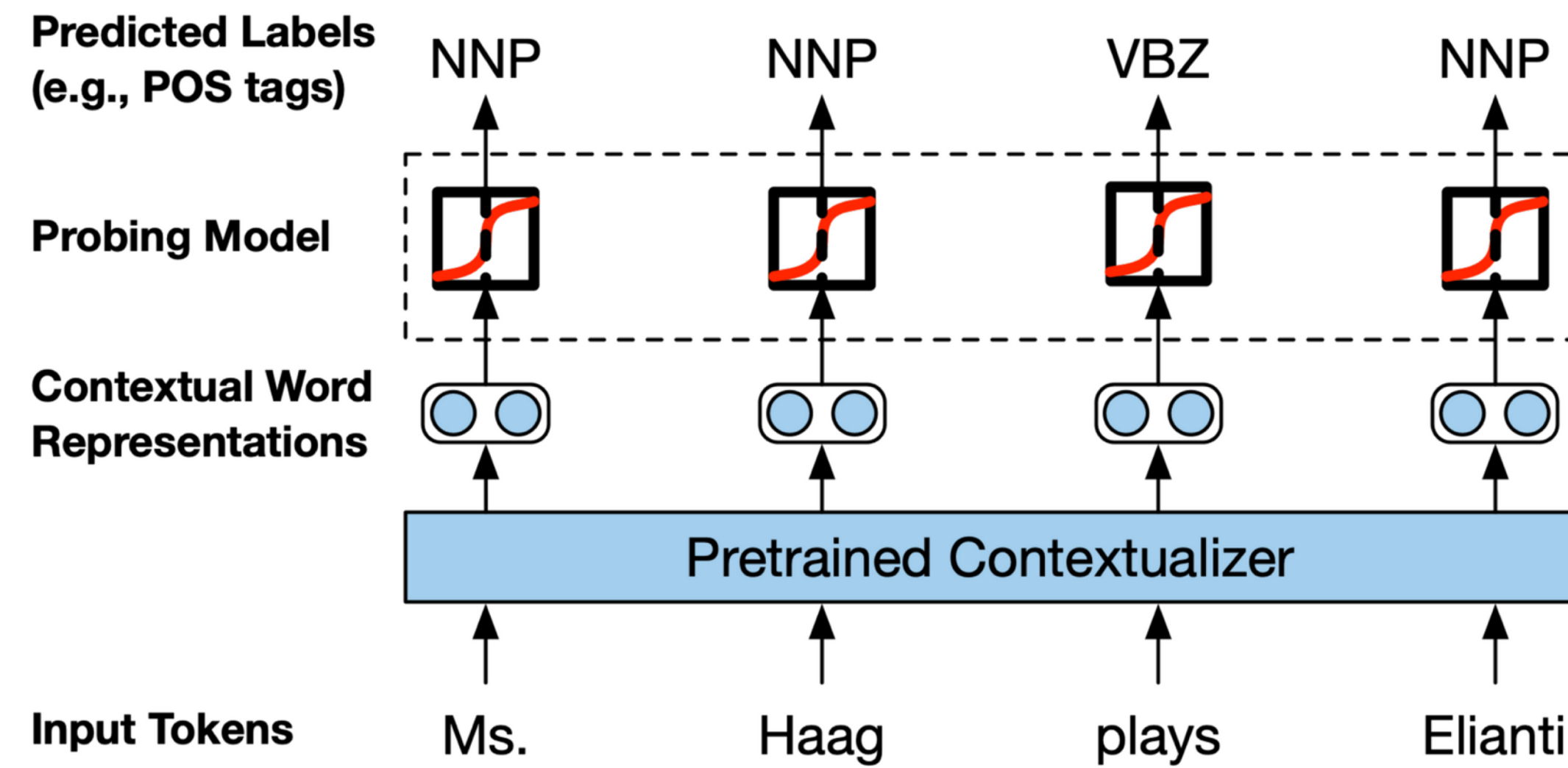
Training objective: MLM

How: use BERT representations **INSTEAD** of the task-specific model

And it was the beginning of a very long story...

# What do models learn?

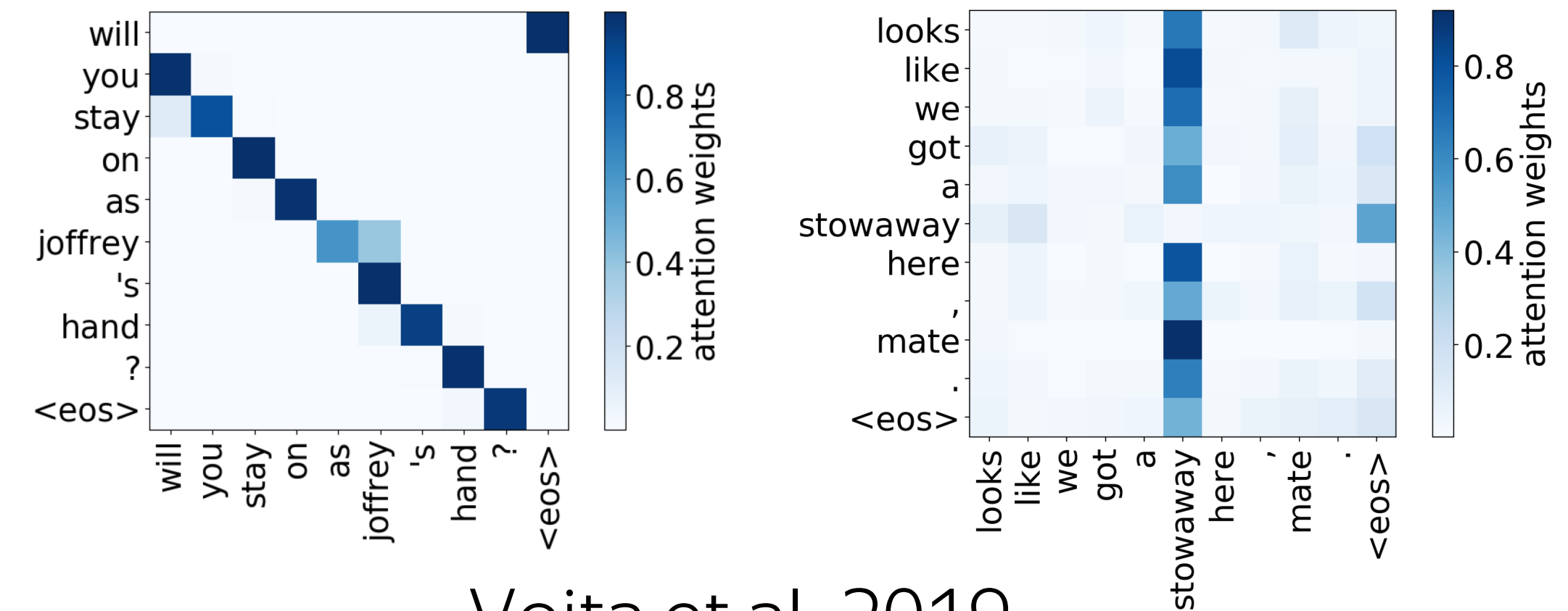
- probing classifiers



Picture credit: Liu et al, 2019

# What do models learn?

- probing classifiers
- model components (e.g., importance and functions of attention heads)



Voita et al, 2019

# What do models learn?

- probing classifiers
- model components (e.g., importance and functions of attention heads)
- fill in the blanks

Prompts

DirectX is developed by  $y_{\text{man}}$   
 $y_{\text{mine}}$  released the DirectX  
DirectX is created by  $y_{\text{para}}$

Top 5 predictions and log probabilities

	$y_{\text{man}}$		$y_{\text{mine}}$		$y_{\text{para}}$	
1	Intel	-1.06	<u>Microsoft</u>	-1.77	<u>Microsoft</u>	-2.23
2	<u>Microsoft</u>	-2.21	They	-2.43	Intel	-2.30
3	IBM	-2.76	It	-2.80	default	-2.96
4	Google	-3.40	Sega	-3.01	Apple	-3.44
5	Nokia	-3.58	Sony	-3.19	Google	-3.45

Picture credit: Jiang et al, 2019



# Why a more general understanding is important?

It can:

- give intuition for creating a better training objective
- give intuition of how to properly use pretrained representations
- explain “puzzles” from previous work

# Plan

- Evolution of representations of individual tokens
- Training objectives: LM, MLM, MT
- "Puzzles" from previous work
- The Information-Bottleneck: our point of view
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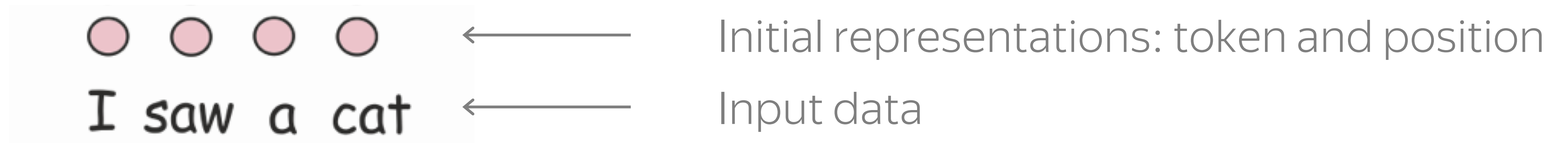
# Representations of individual tokens

I saw a cat

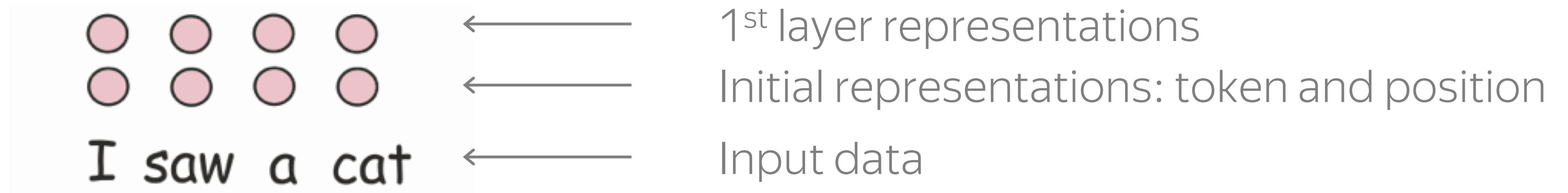


Input data

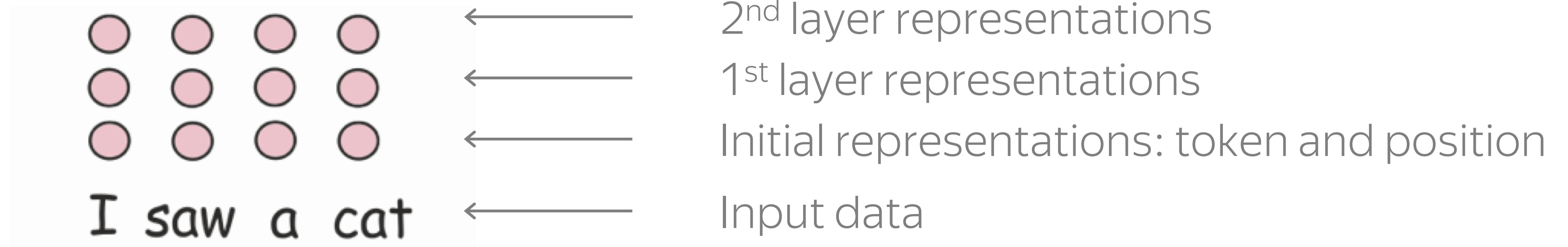
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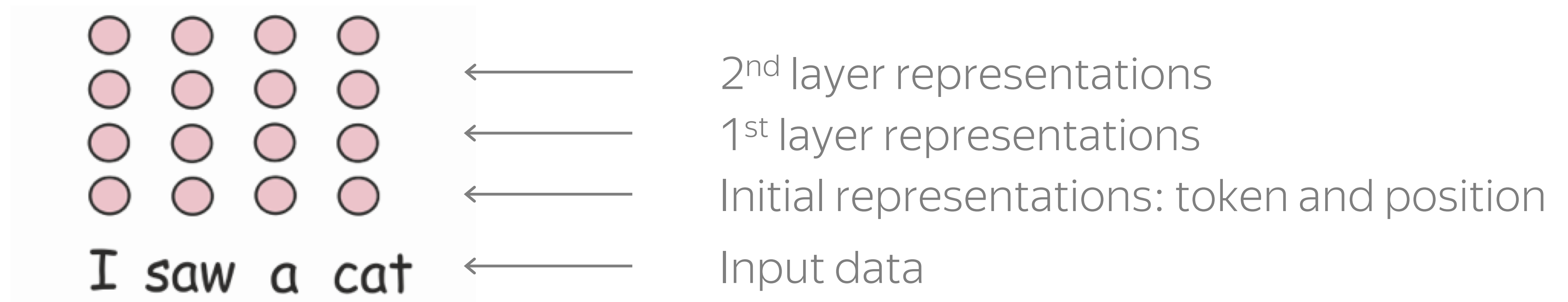
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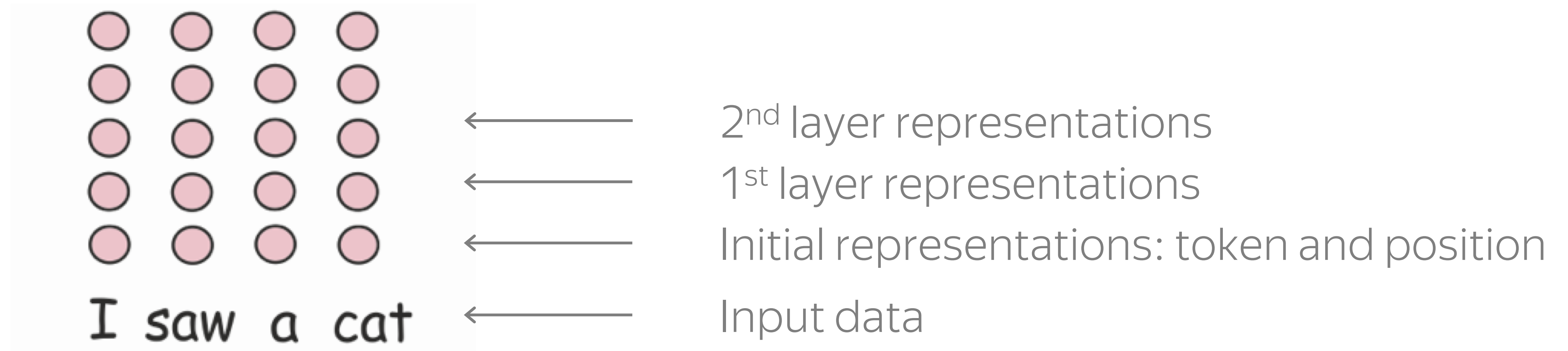


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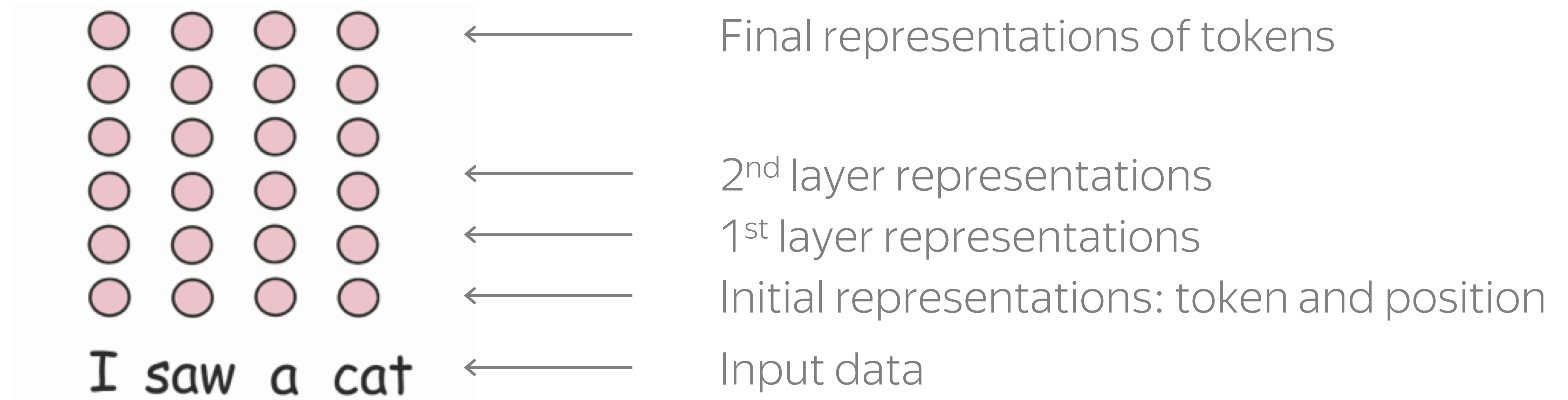




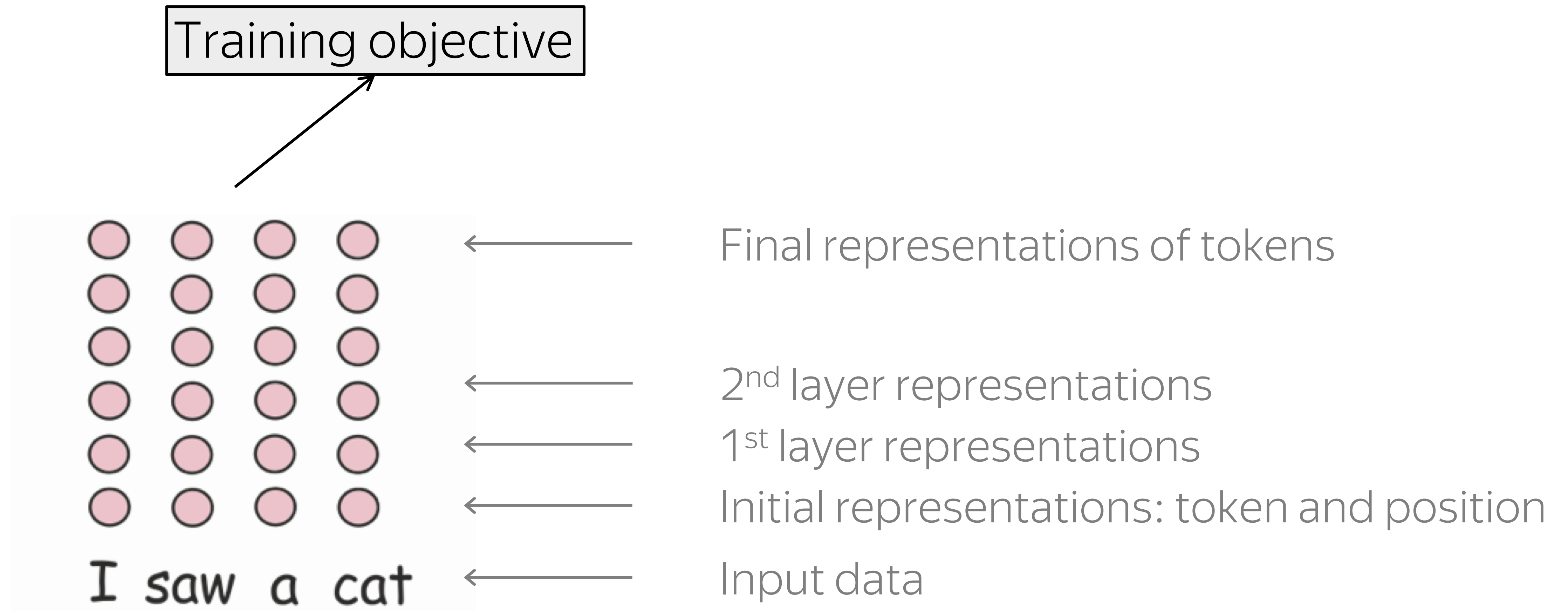
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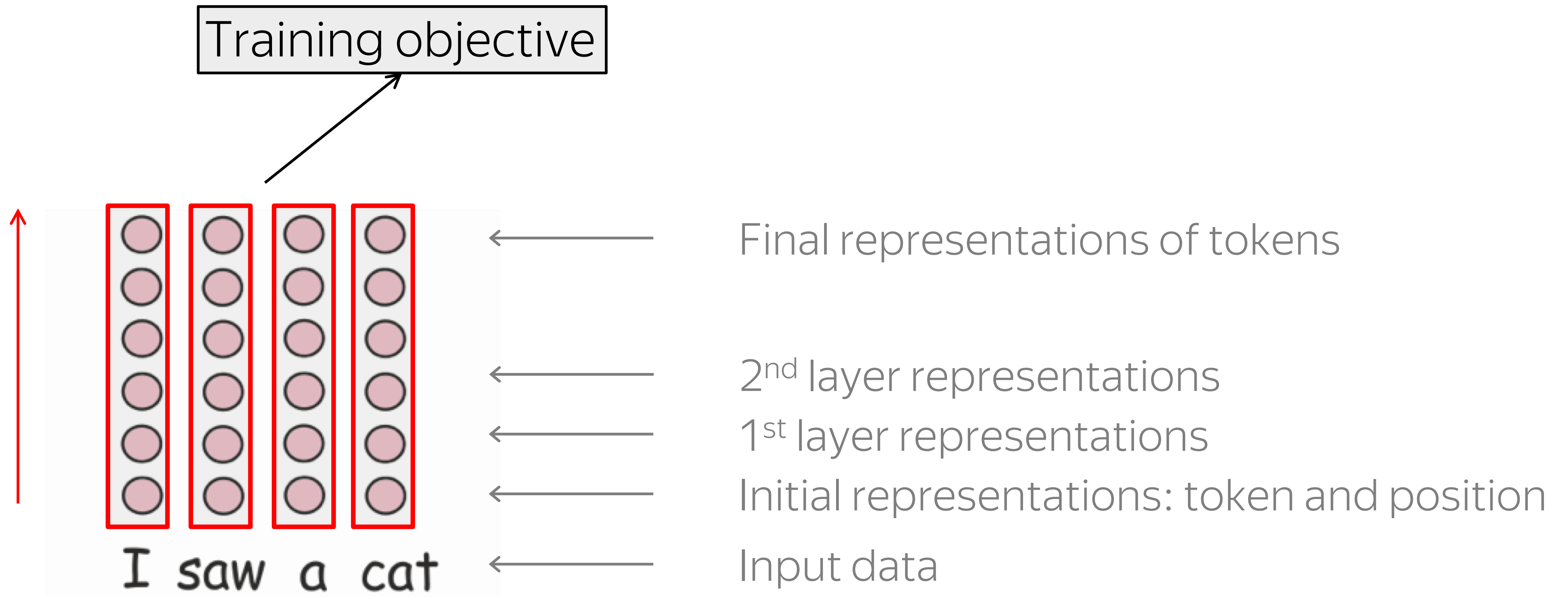
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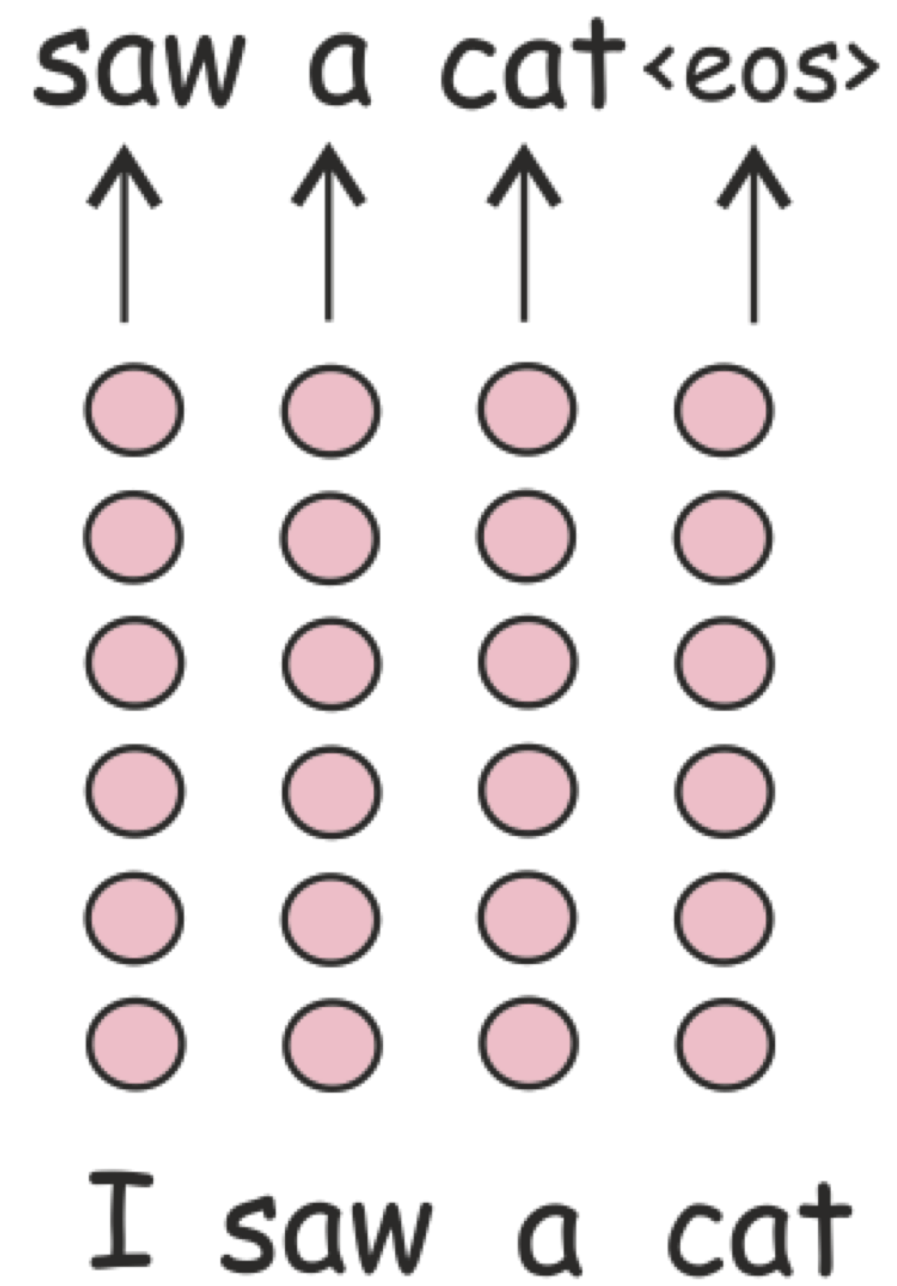
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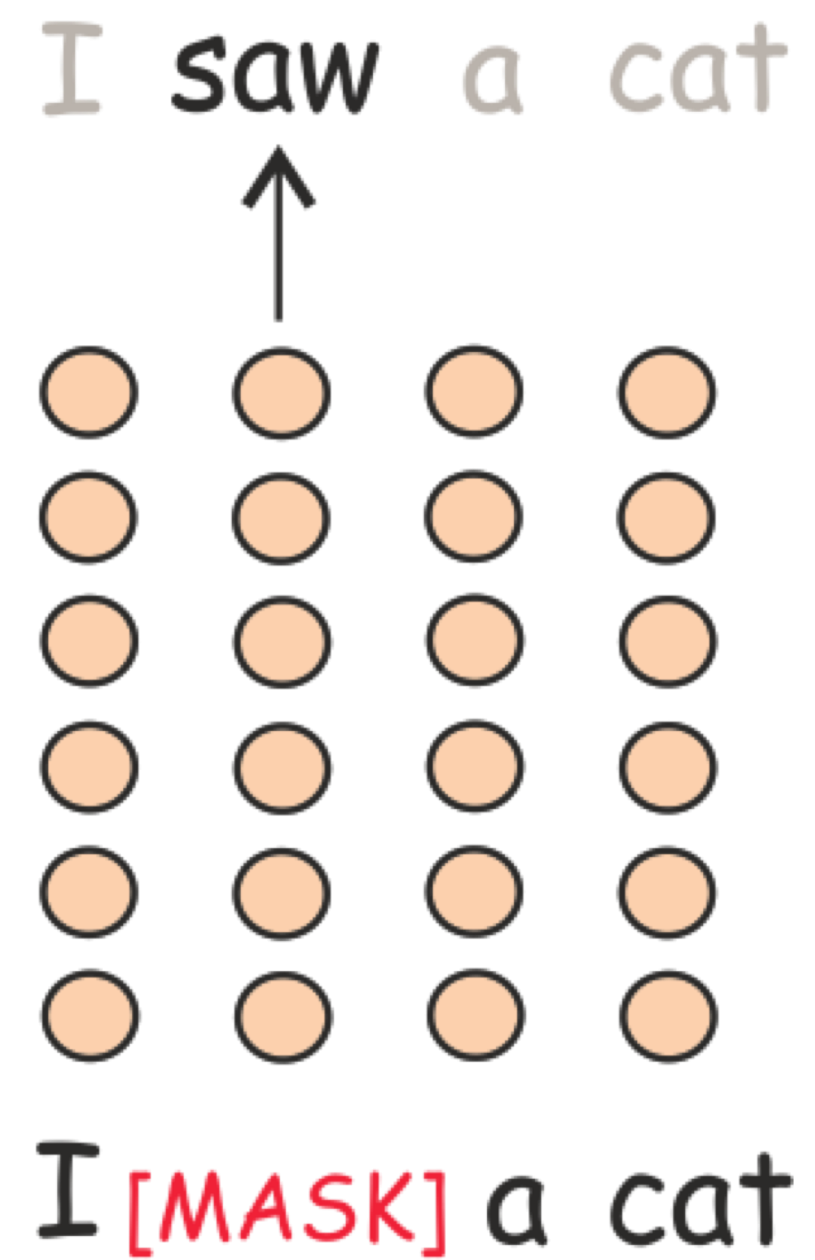
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# Tasks: LM, MLM, MT

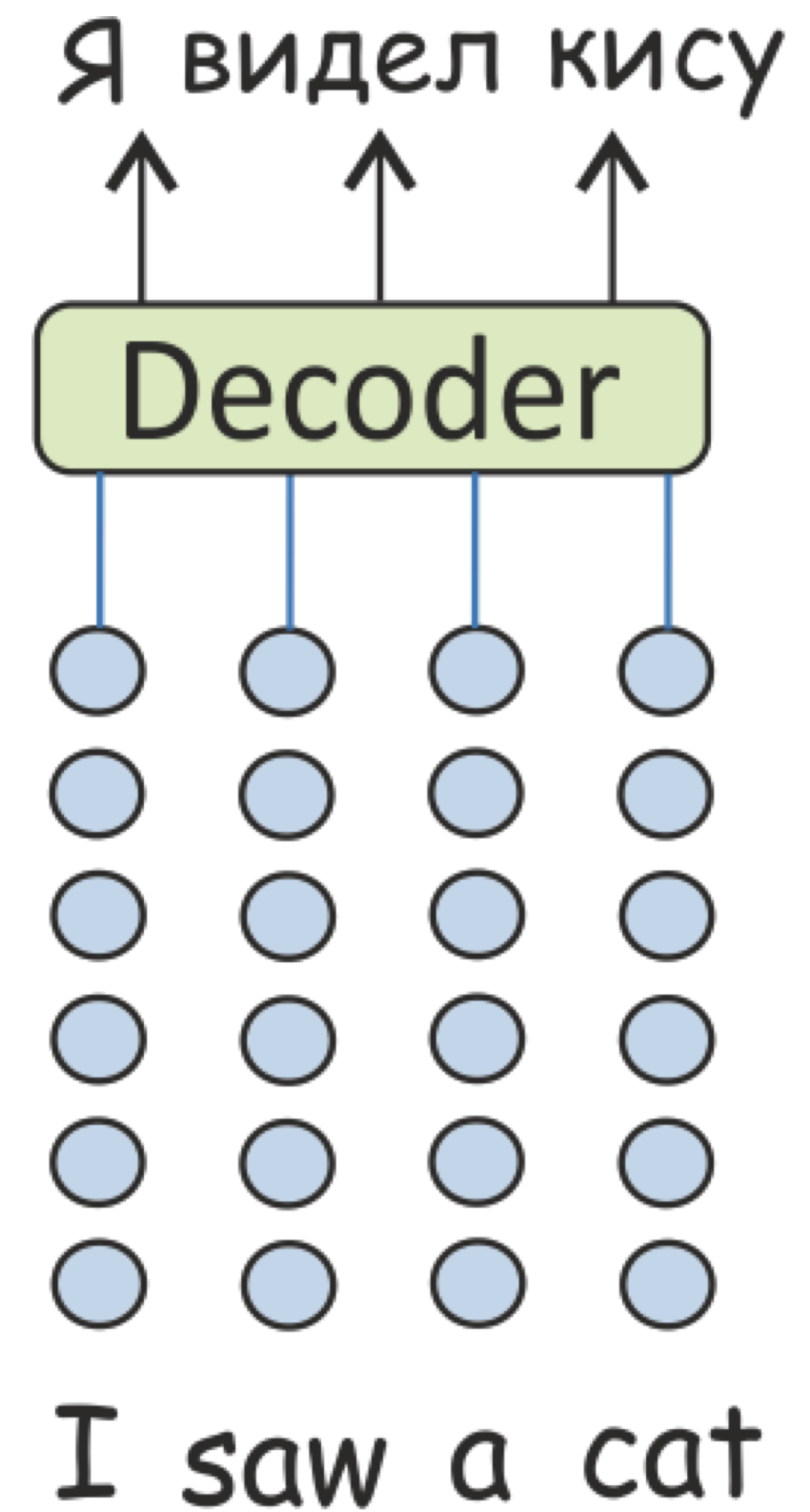
LM



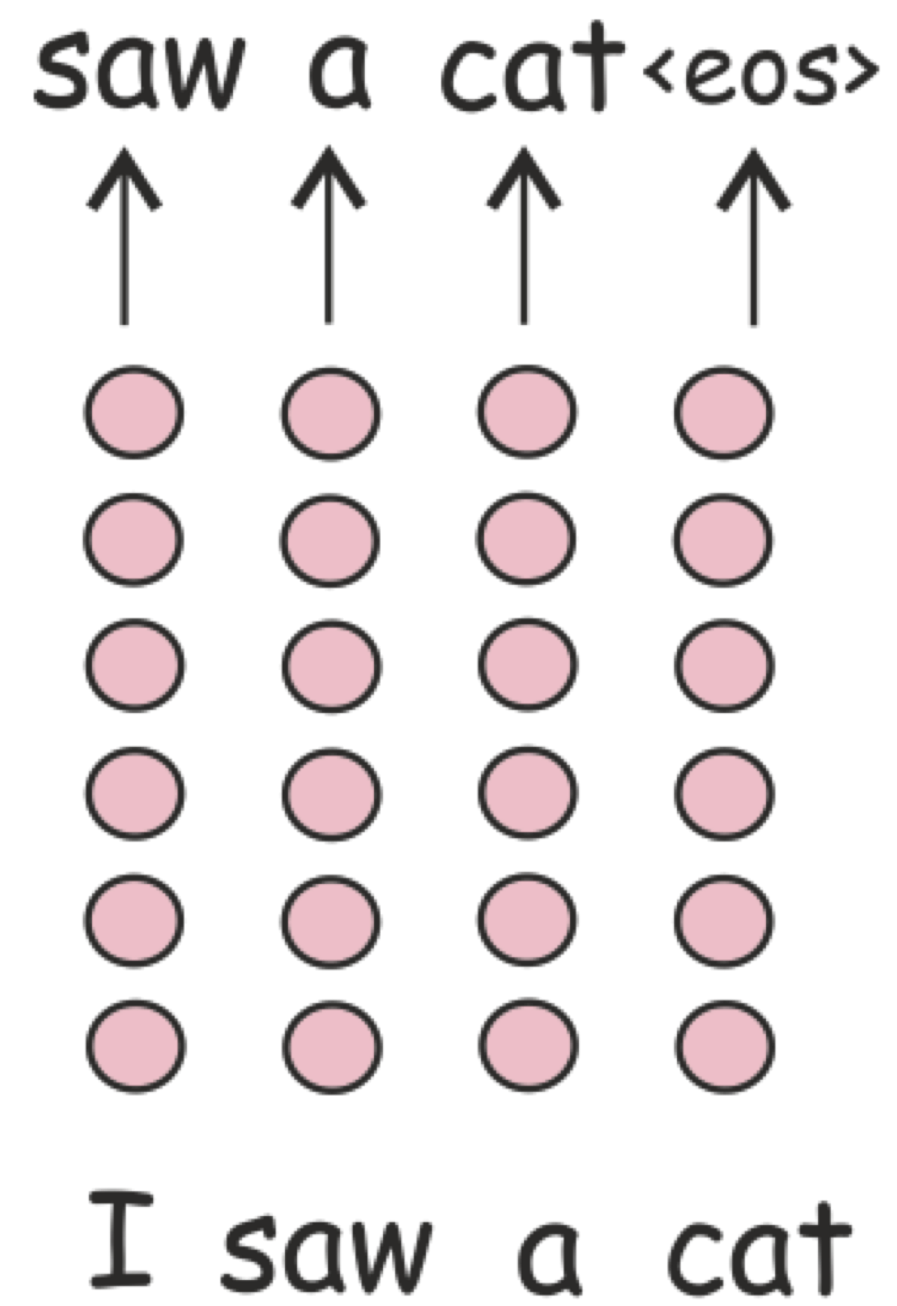
MLM



MT

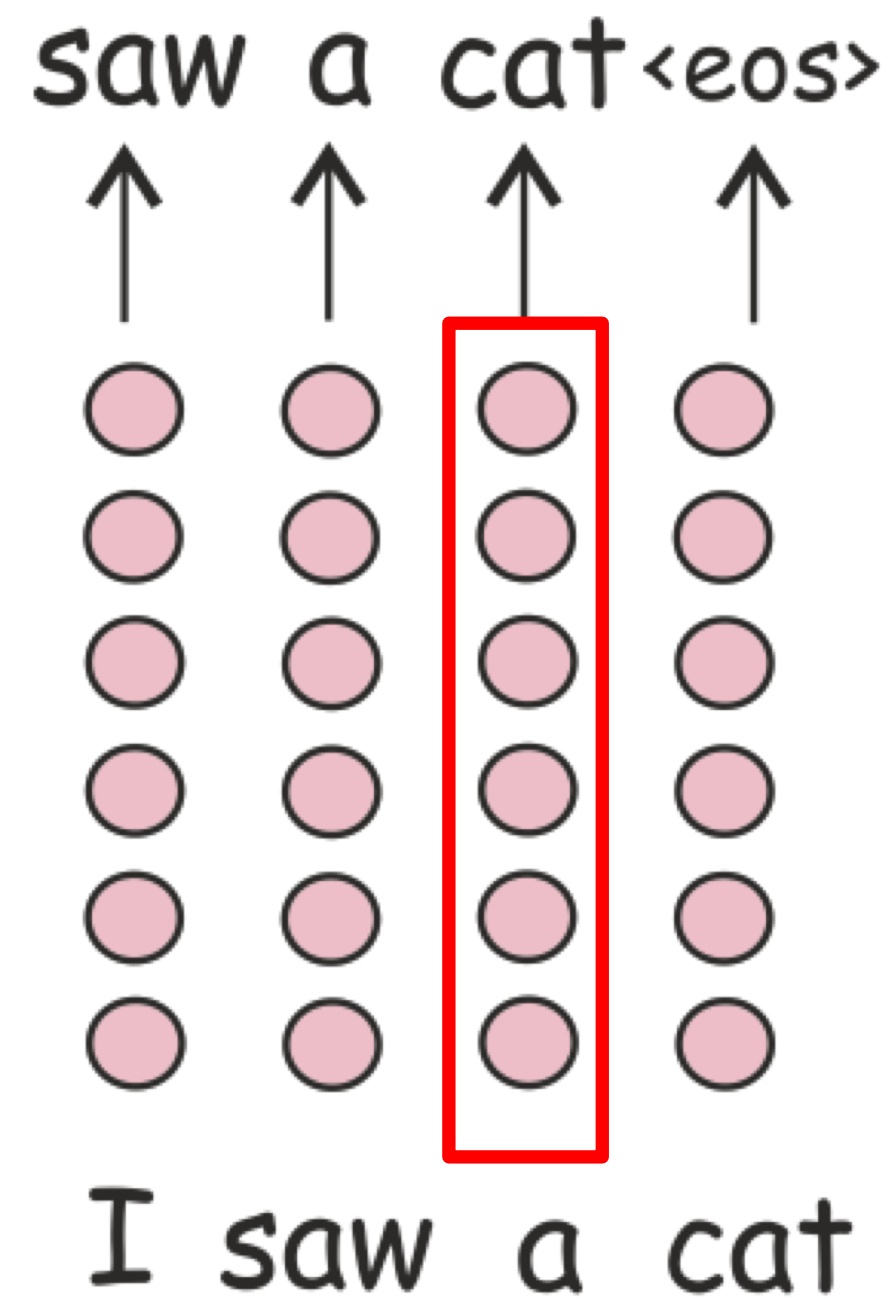


# LM - Language Modeling





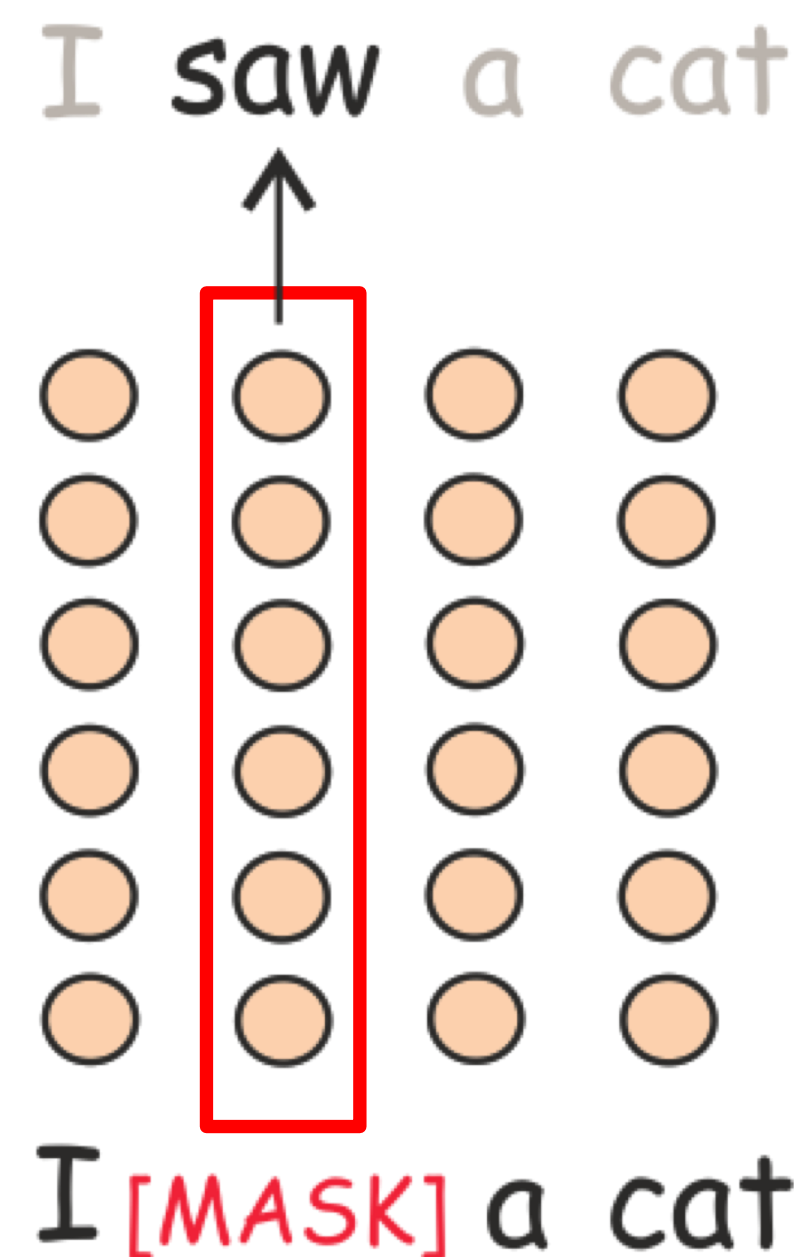
# LM - Language Modeling



Input: current token identity and position

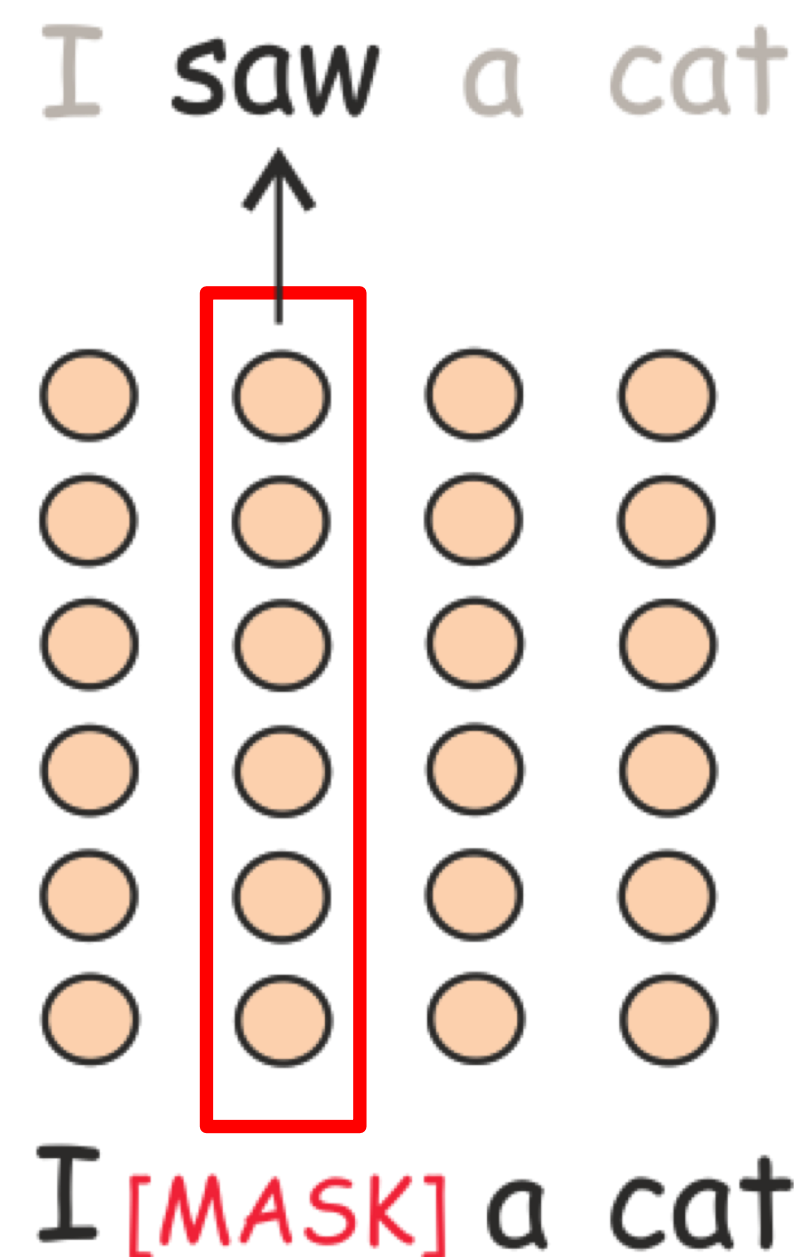
Output: next token

# MLM – Masked Language Modeling (aka BERT)



- some tokens are selected (with probability  $p=15\%$ )
- selected tokens are either replaced with **[mask]**, random or current token

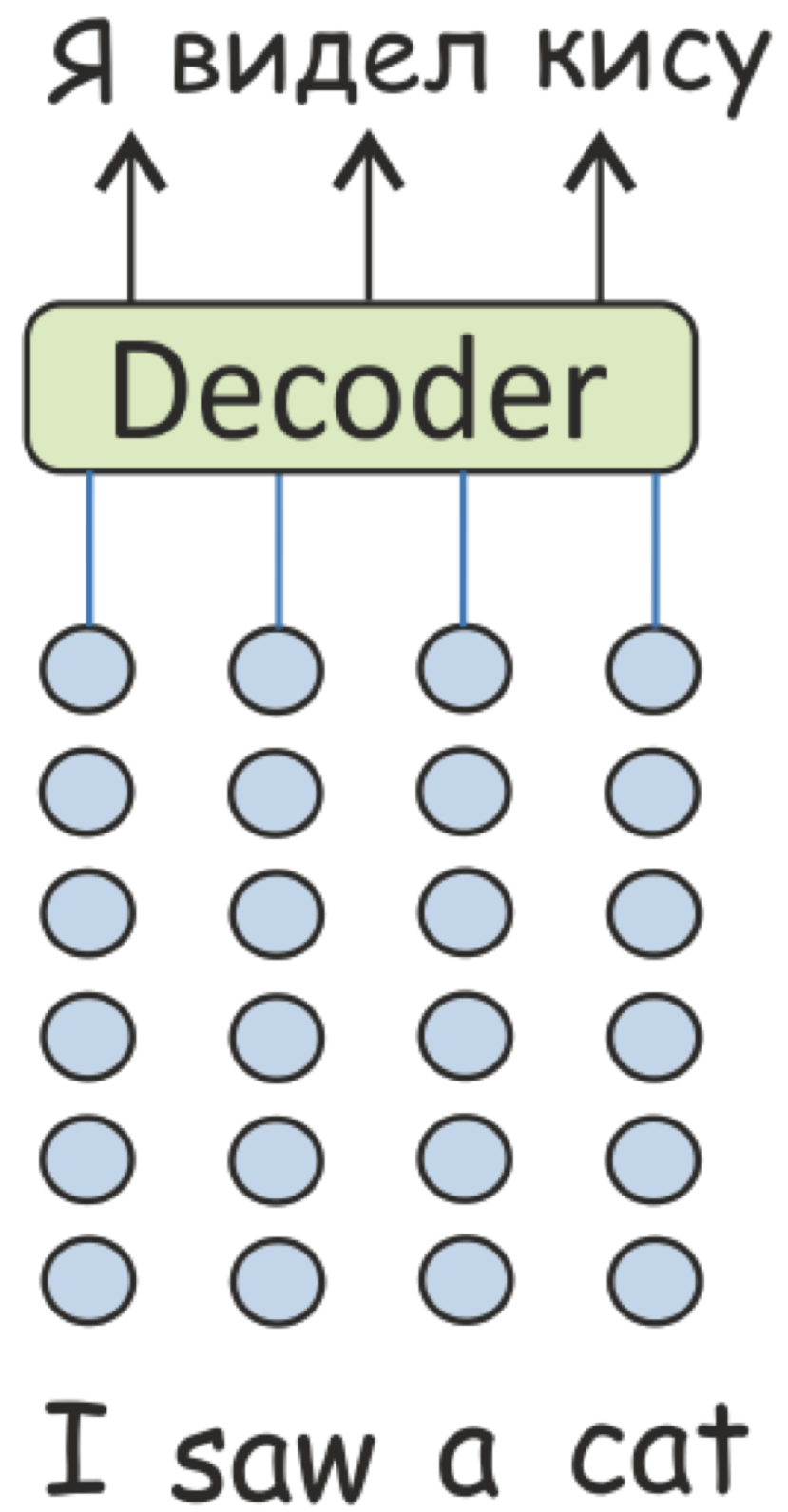
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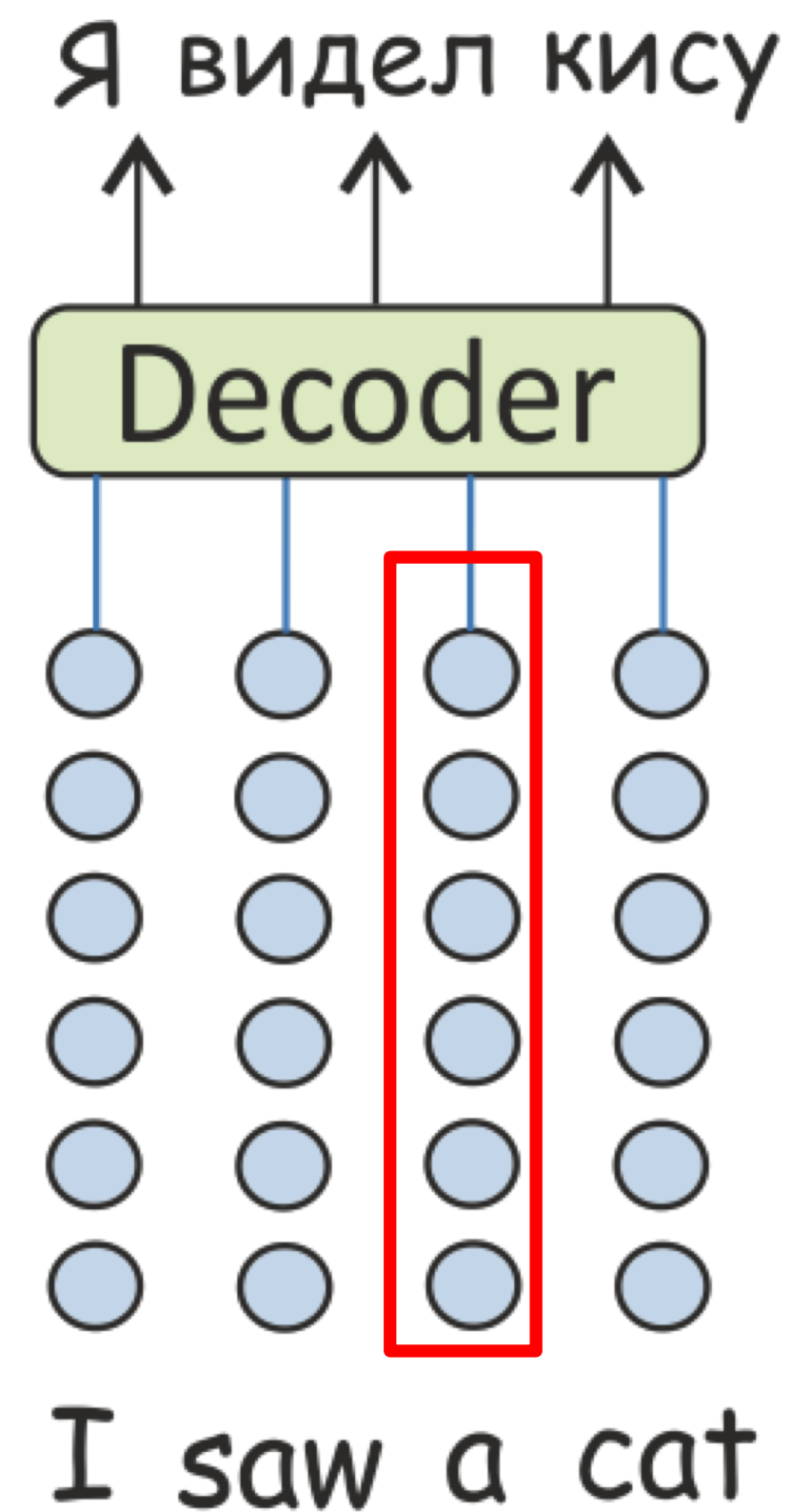
Input: **[mask]**, random or current token identity and position

Output: current token

# MT – Machine Translation



# MT – Machine Translation



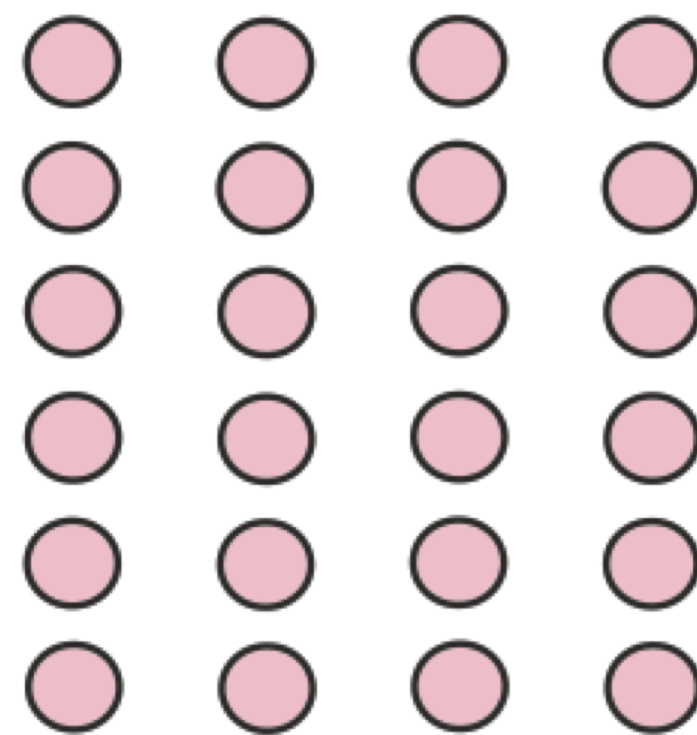
Input: current token identity and position

Output: nothing is predicted directly

# The bottom-up evolution

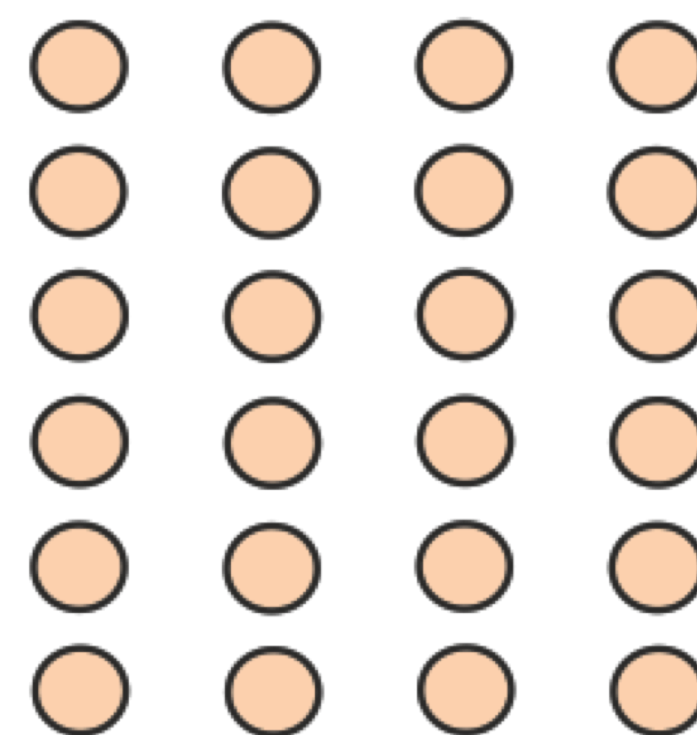
- Fix: model and training data
- Vary: training objective

LM



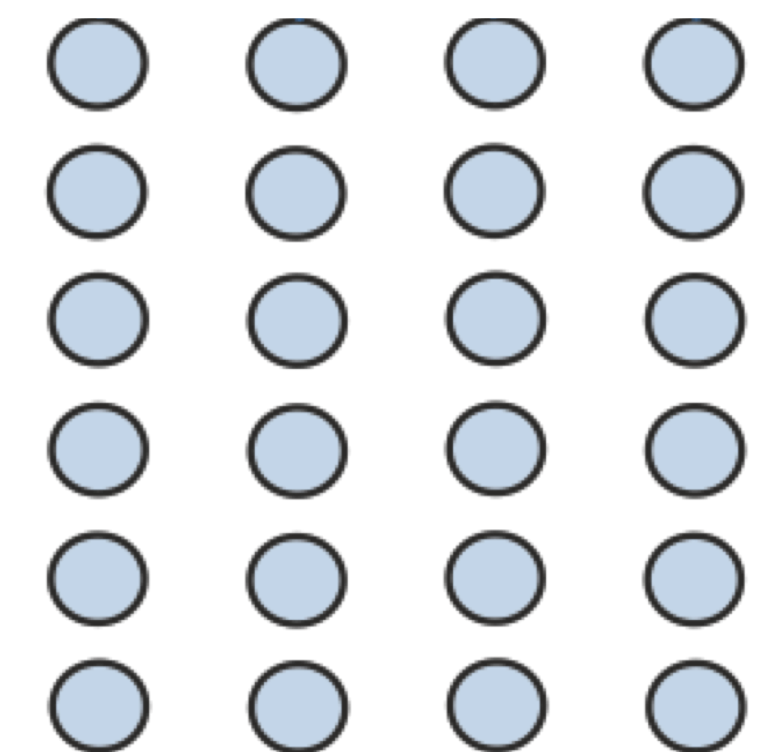
I saw a cat

MLM



I saw a cat

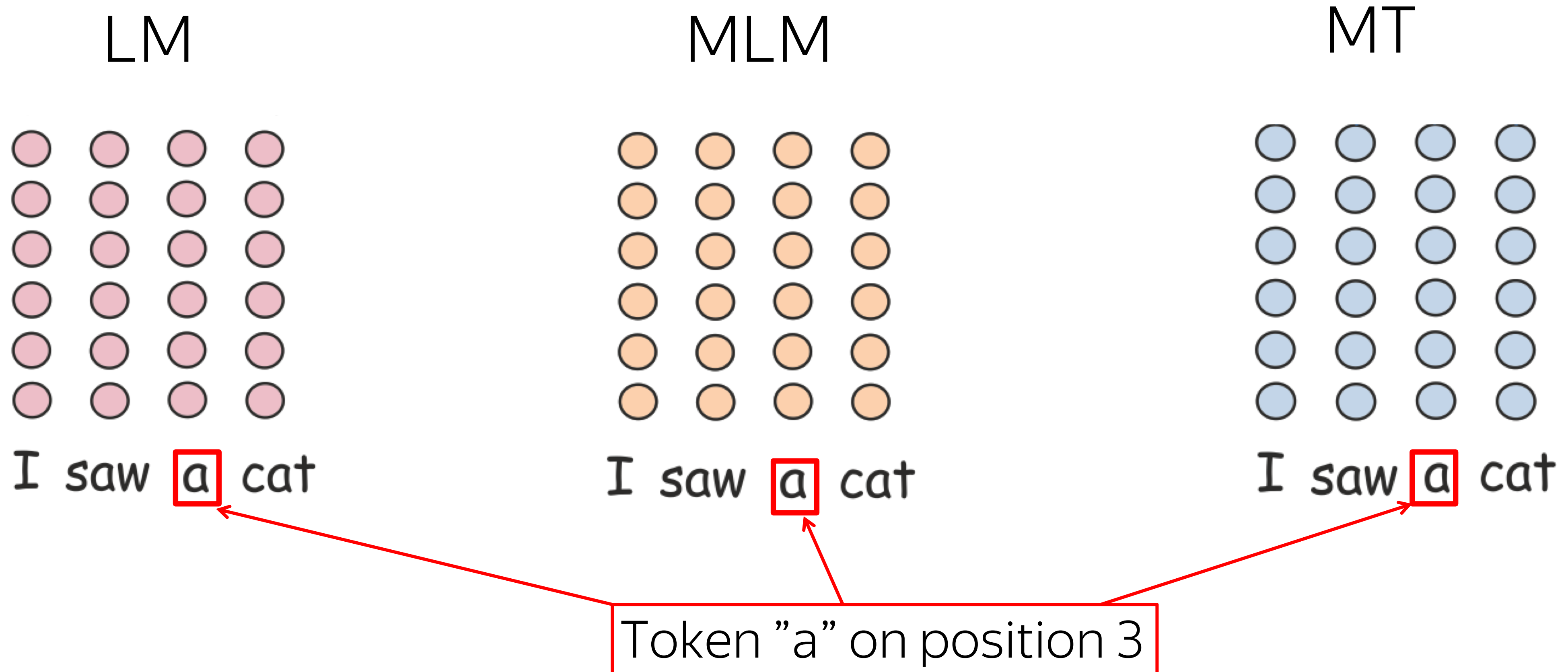
MT



I saw a cat

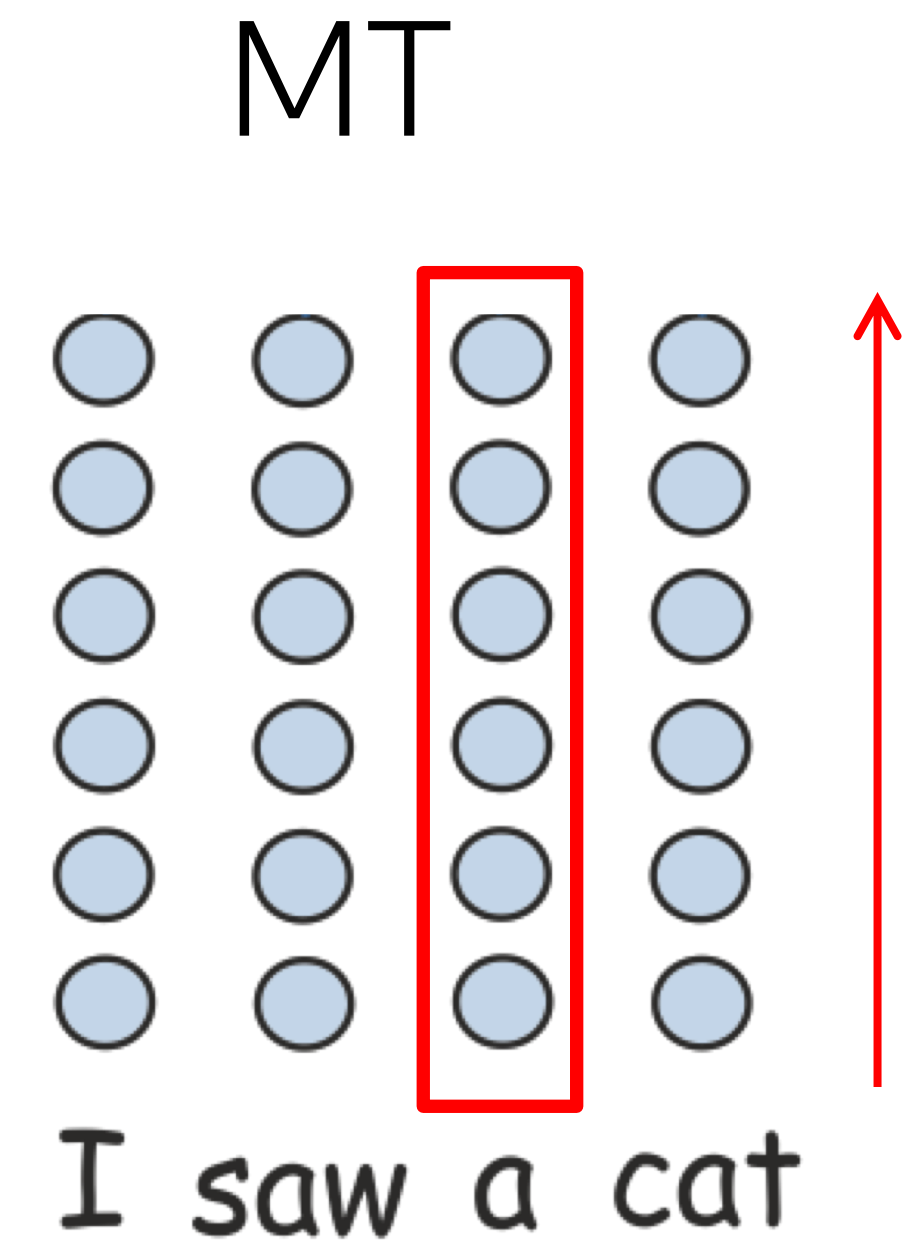
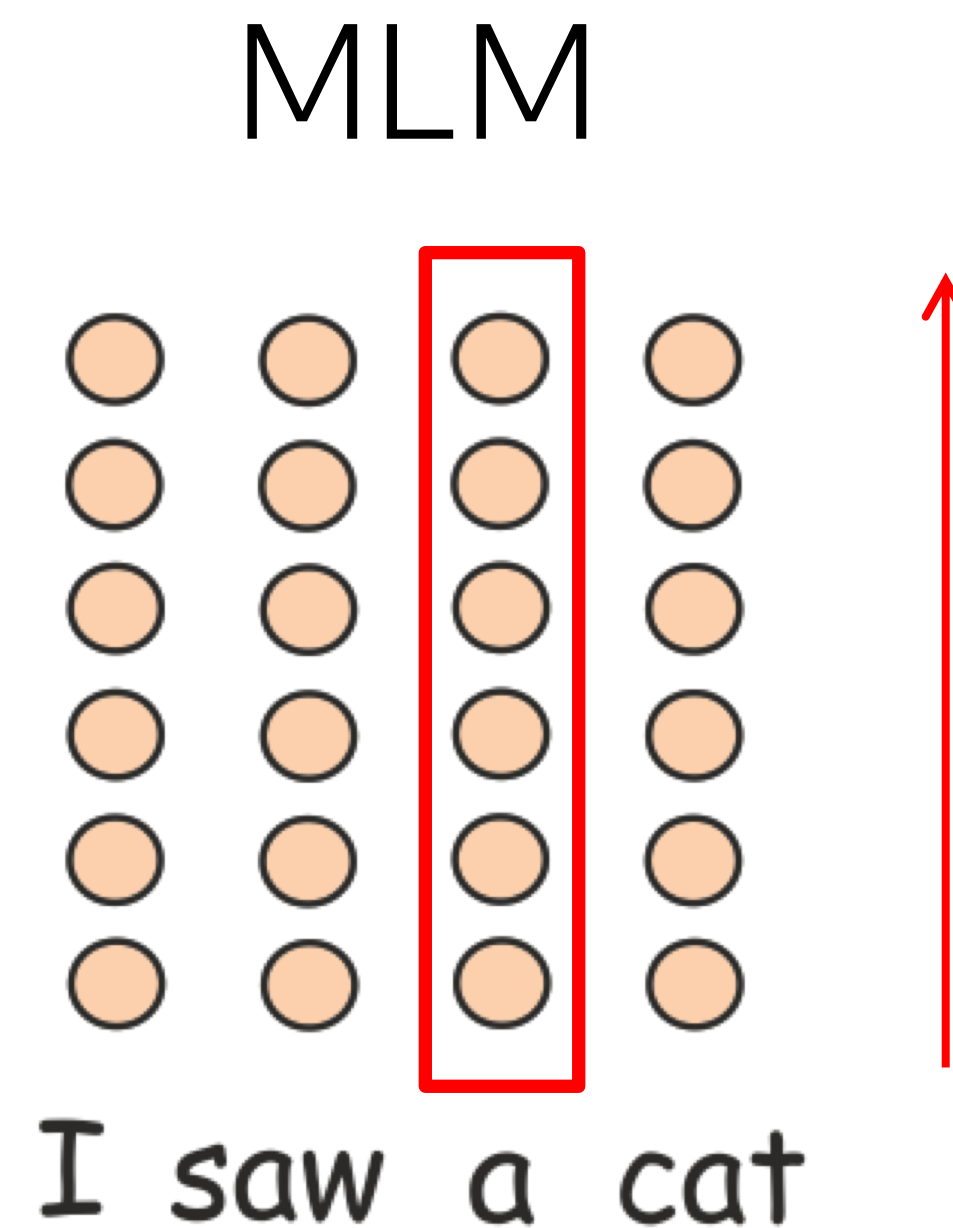
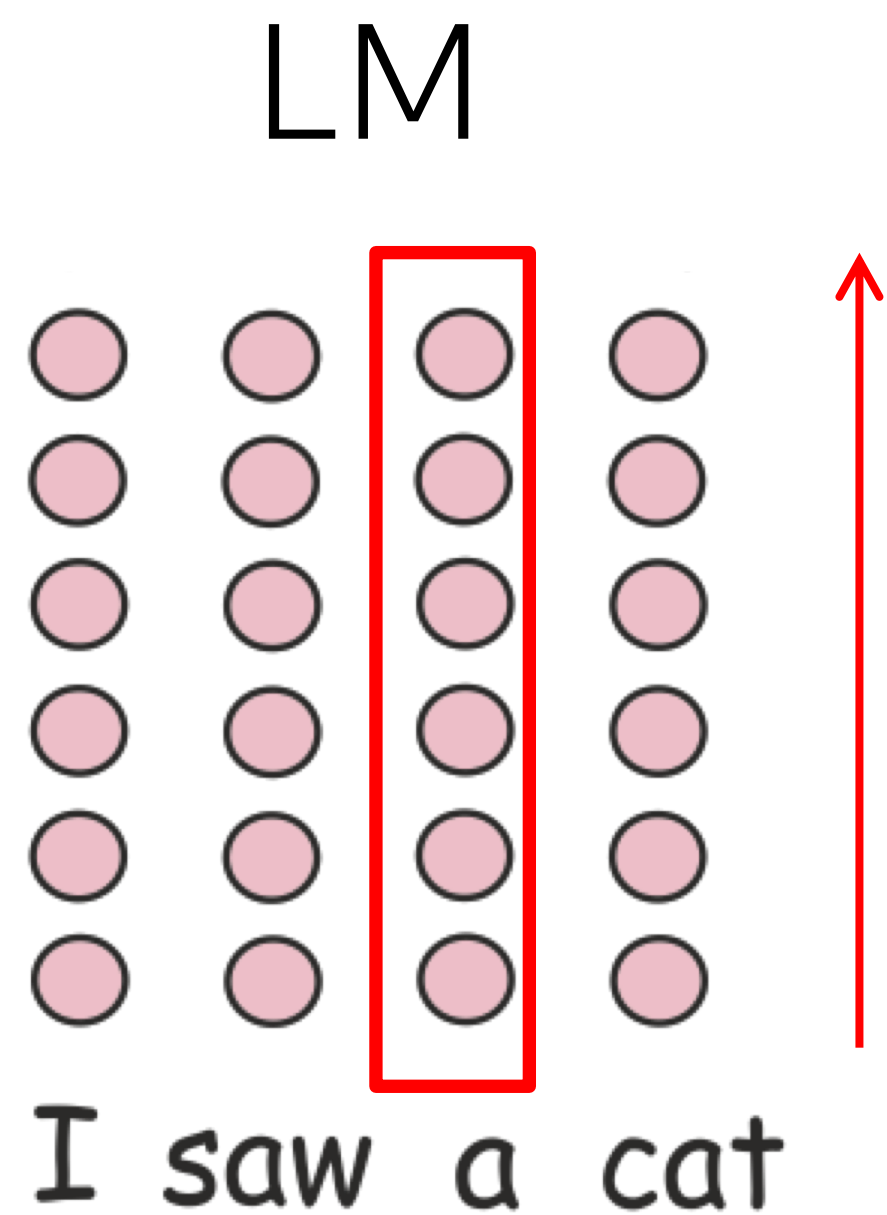
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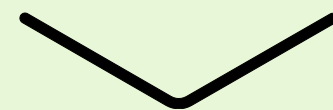




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Previous work: “puzzling” results



# Untrained LSTMs are better for token prediction

- Untrained LSTMs outperform trained ones for word identity prediction task (Zhang & Bowman, 2018)

# MT behavior is monotonic, LM is not

- For constituent labeling prediction, MT shows monotonic behavior, while LM non-monotonic (Blevins et al, 2018)

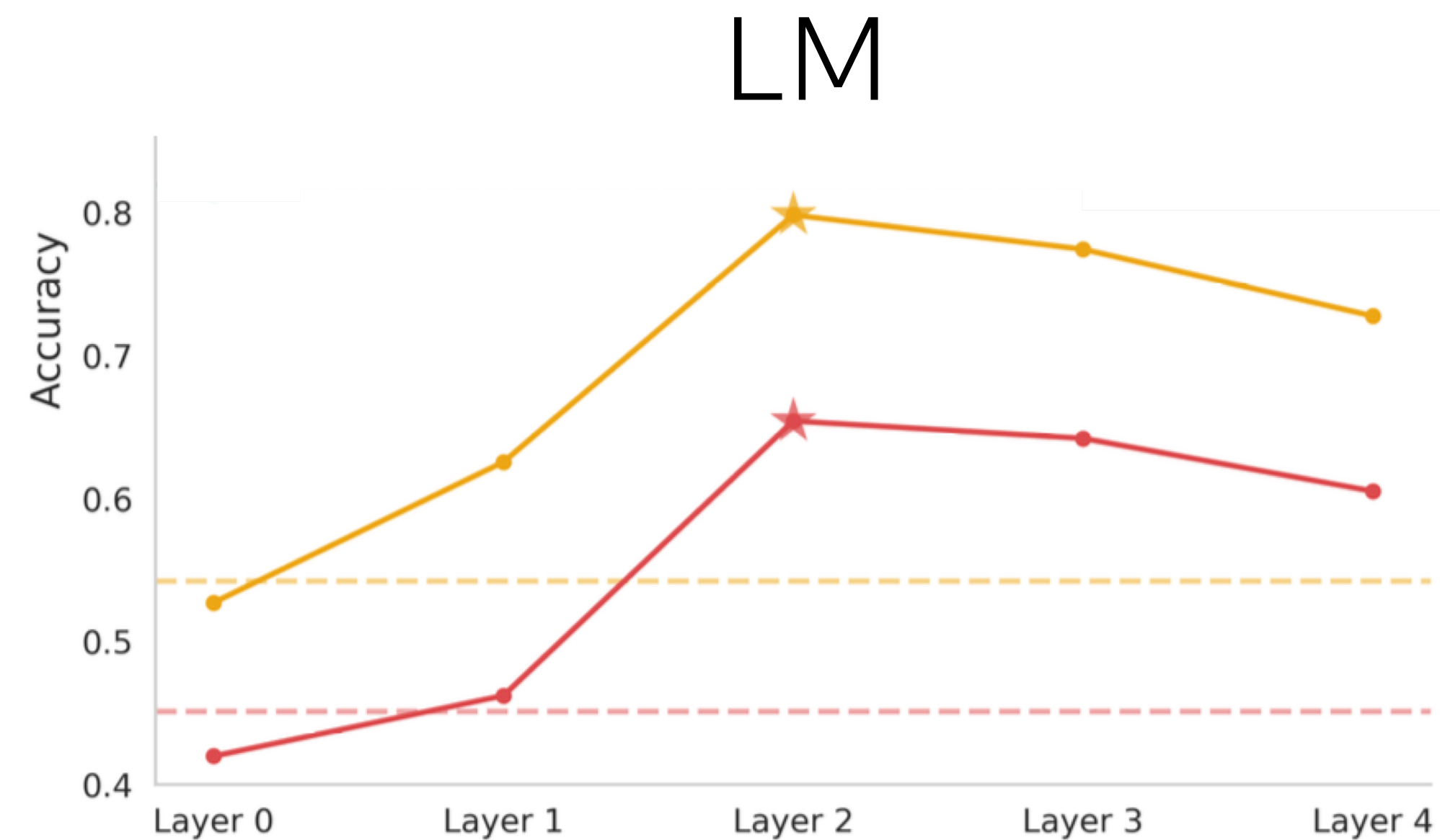
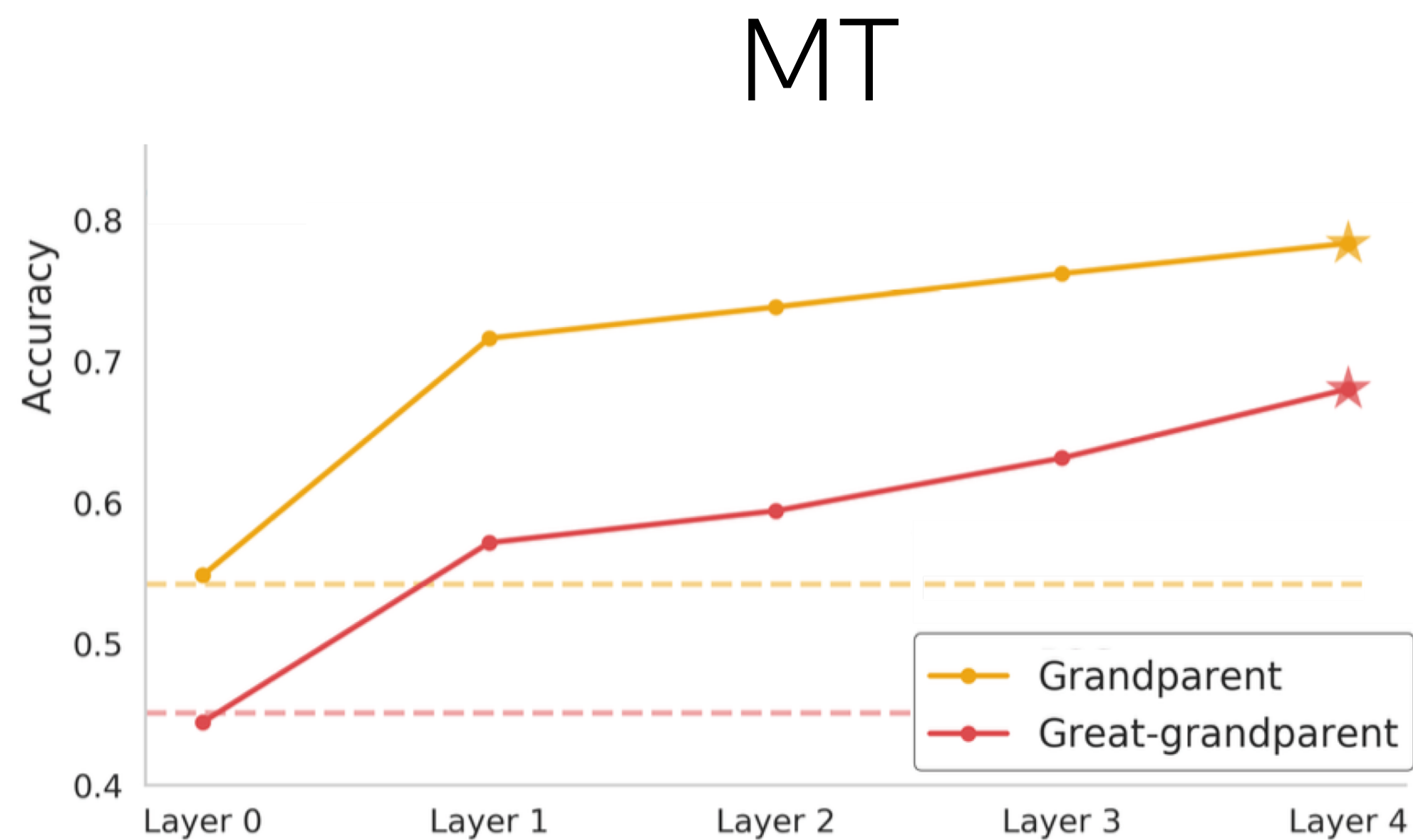


Illustration is from the original paper by Blevins et al, 2018

# BERT behavior is not monotonic

- For different tasks the contribution of a layer to a task increases up to a certain layer, but then decreases at the top layers (Tenney et al, 2019)

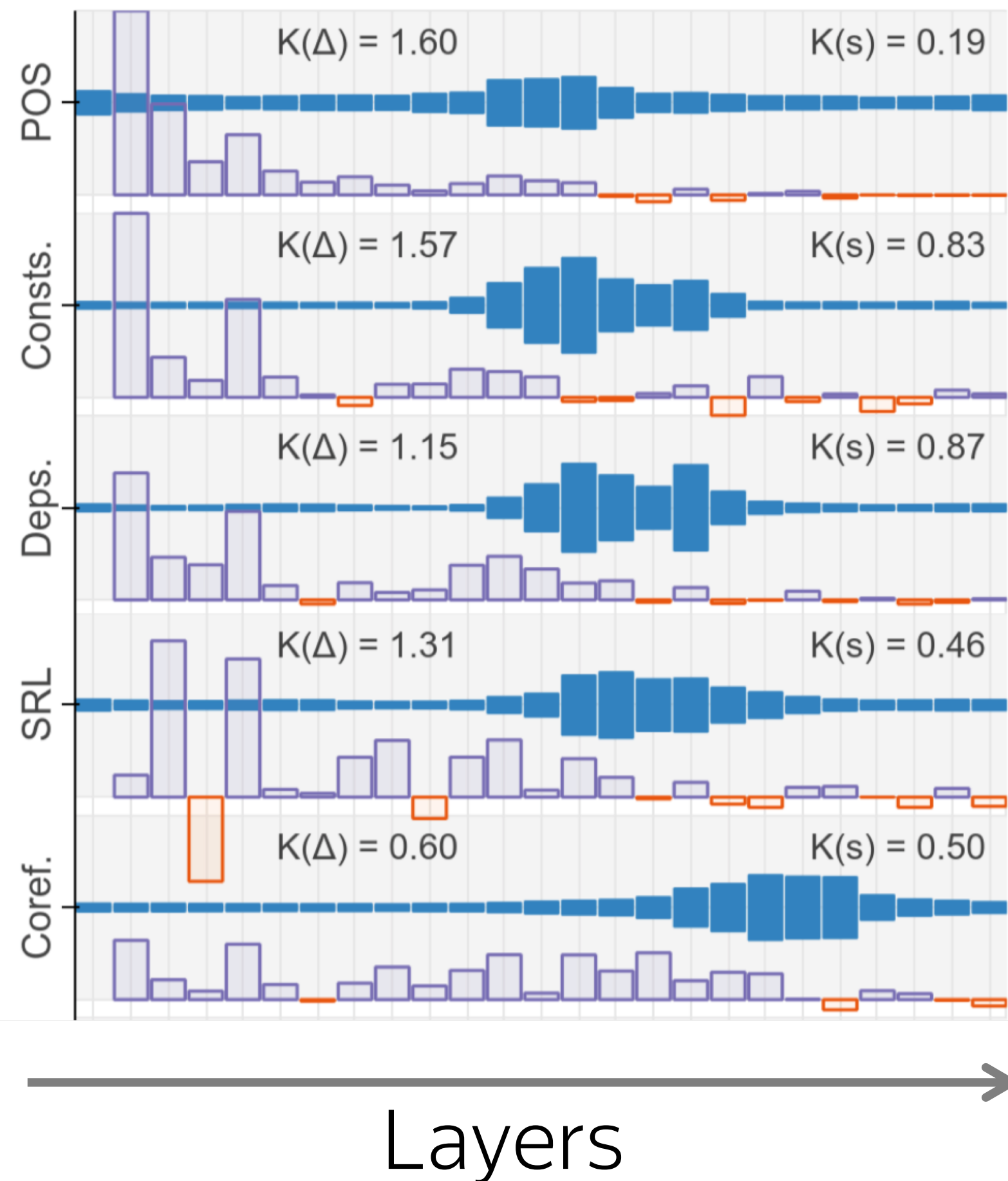
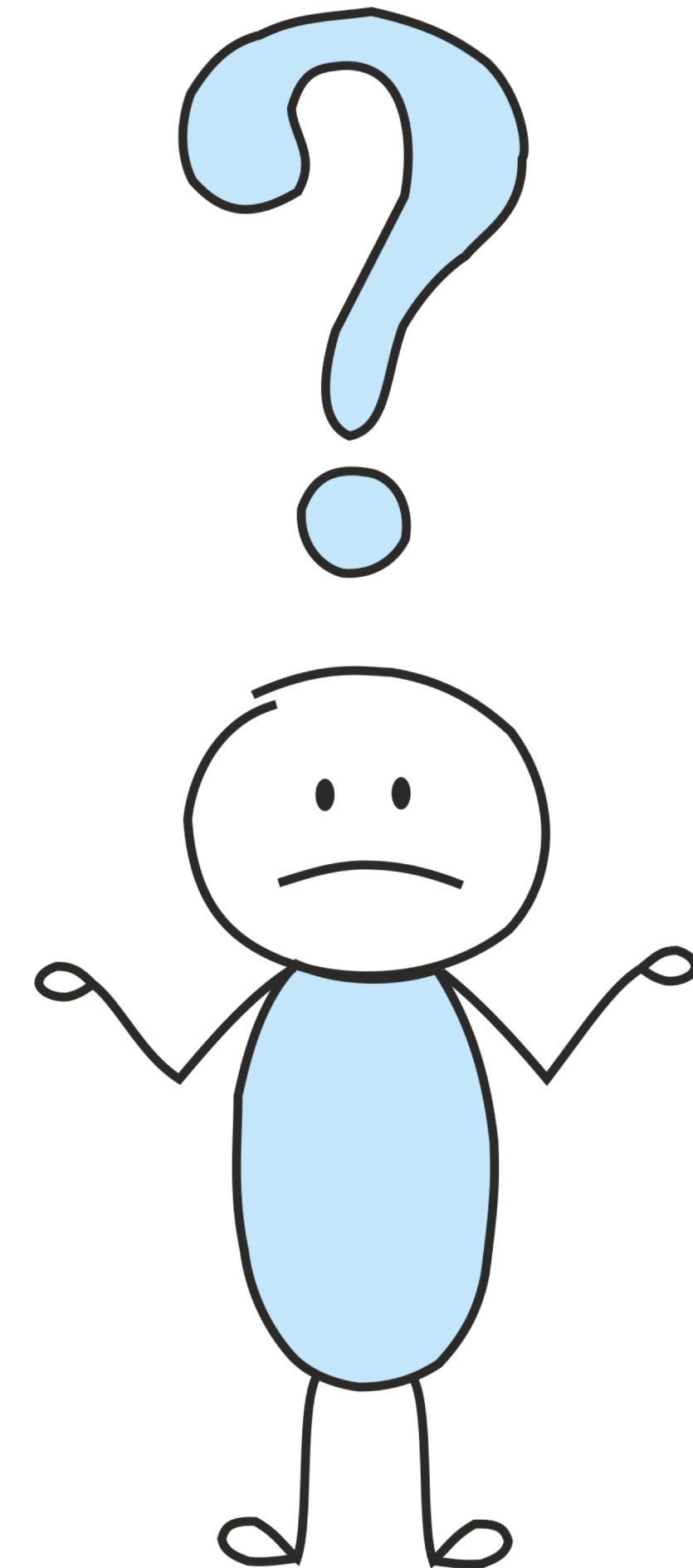


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# Why is this happening?

Problems:

- Evidence is somewhat anecdotal
- No explanation of the process behind such behavior



# Plan

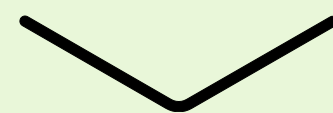
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# The Information- Bottleneck Viewpoint

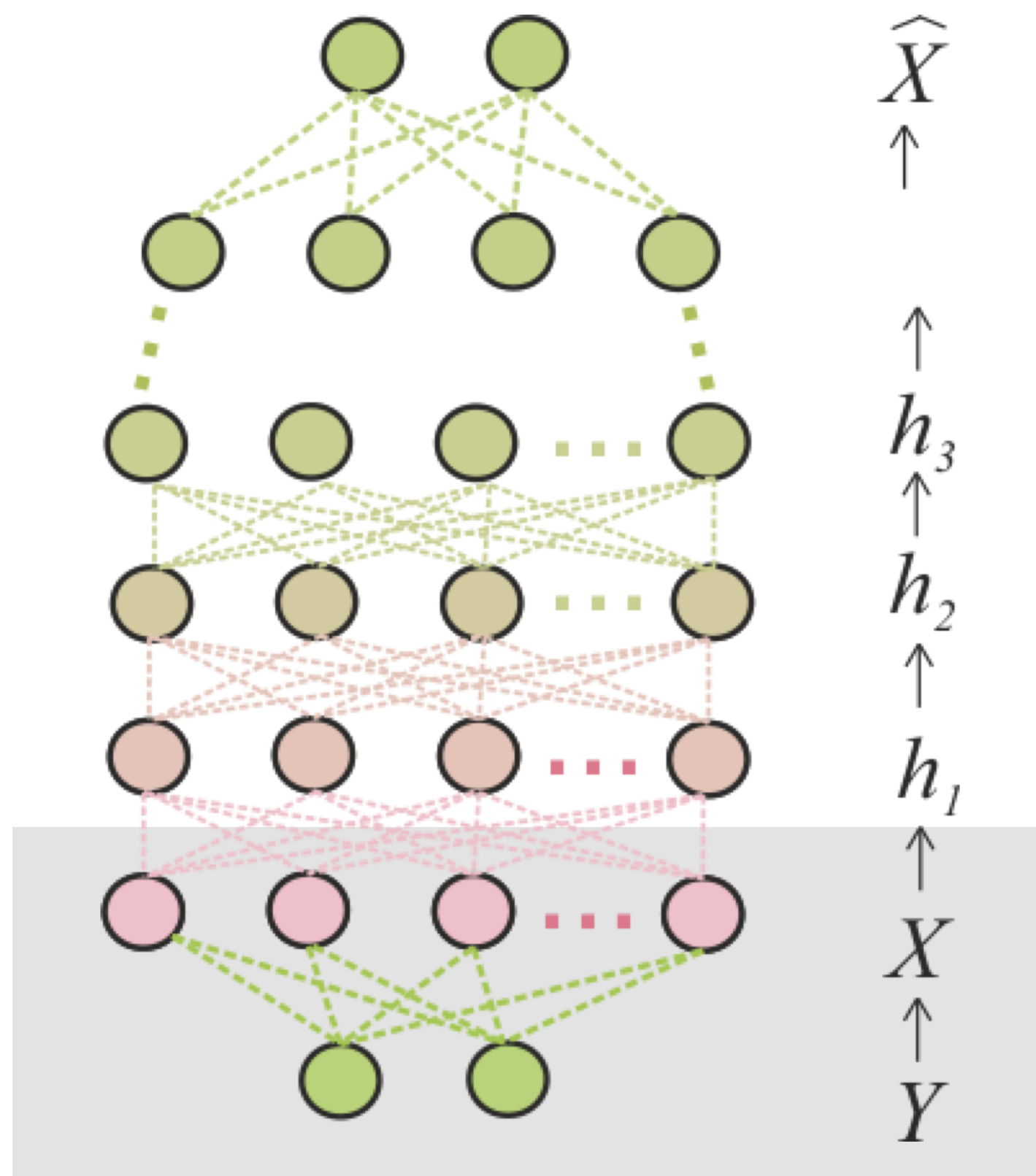


# Information Bottleneck

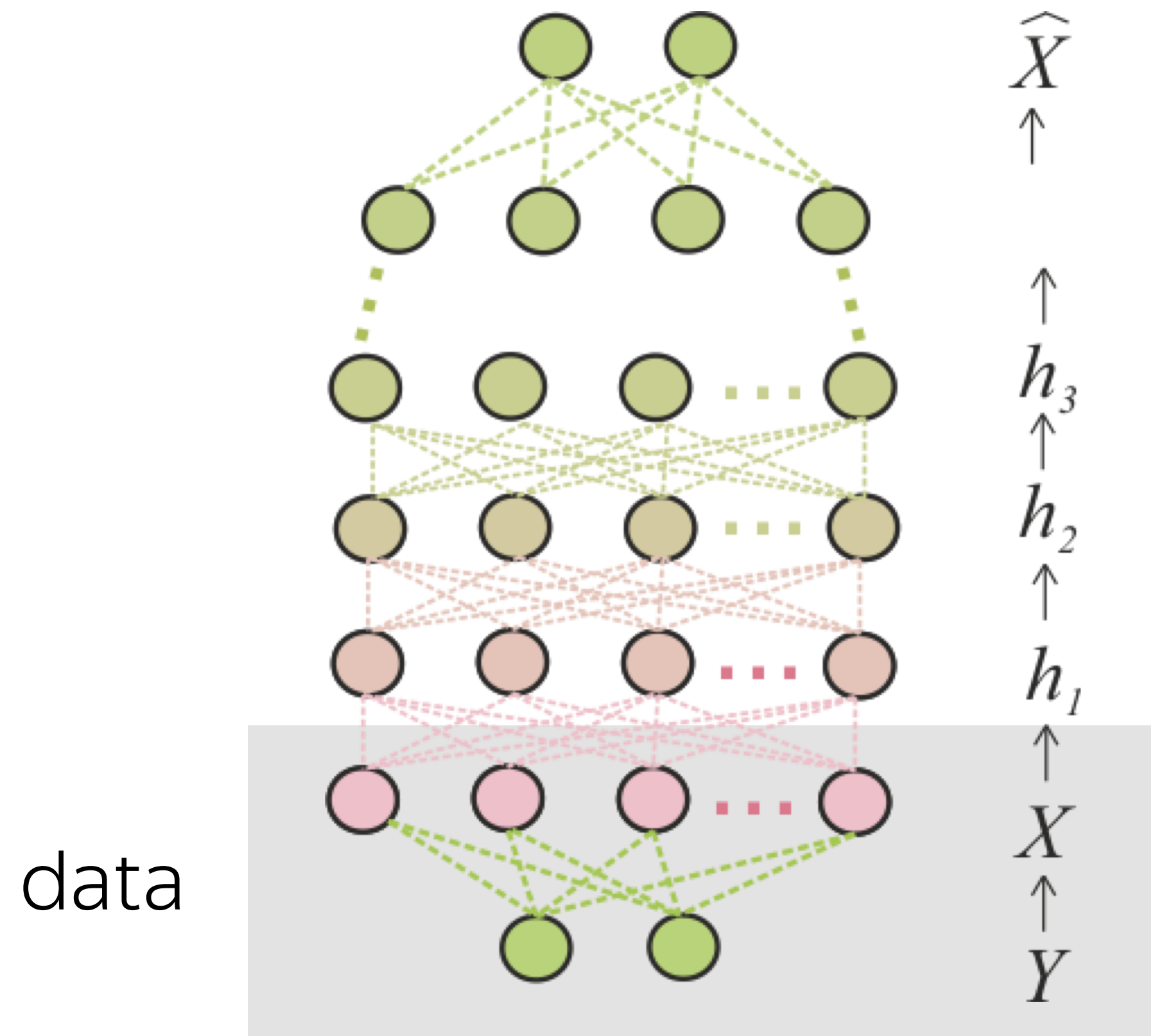
The IB method:

$$\hat{X} : I(\hat{X}, X) - \beta I(\hat{X}, Y) \rightarrow \min, \beta > 0$$

data



# Information Bottleneck



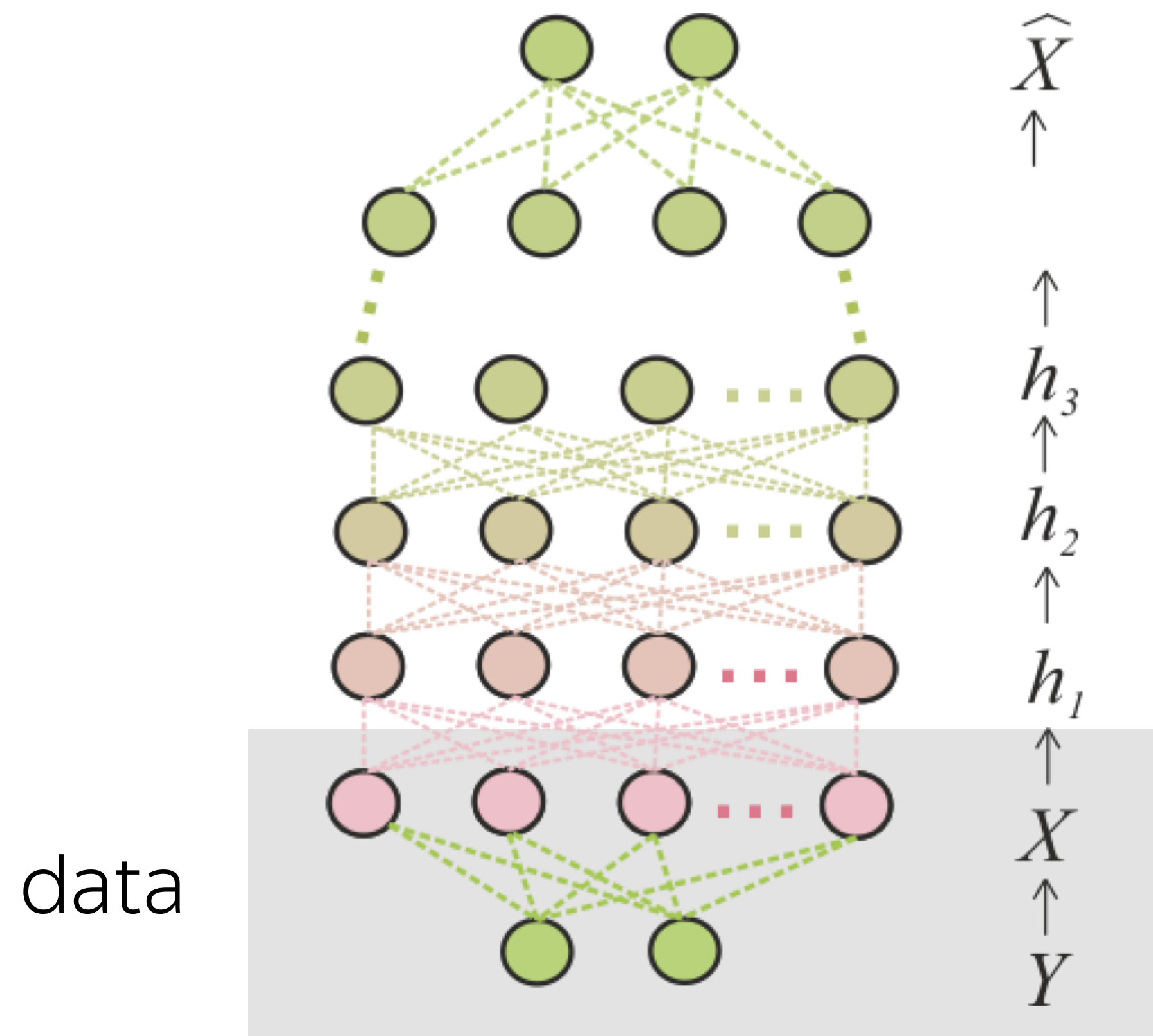
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In neural networks:

Evolution towards the theoretical optimum of the IB objective

# Information Bottleneck



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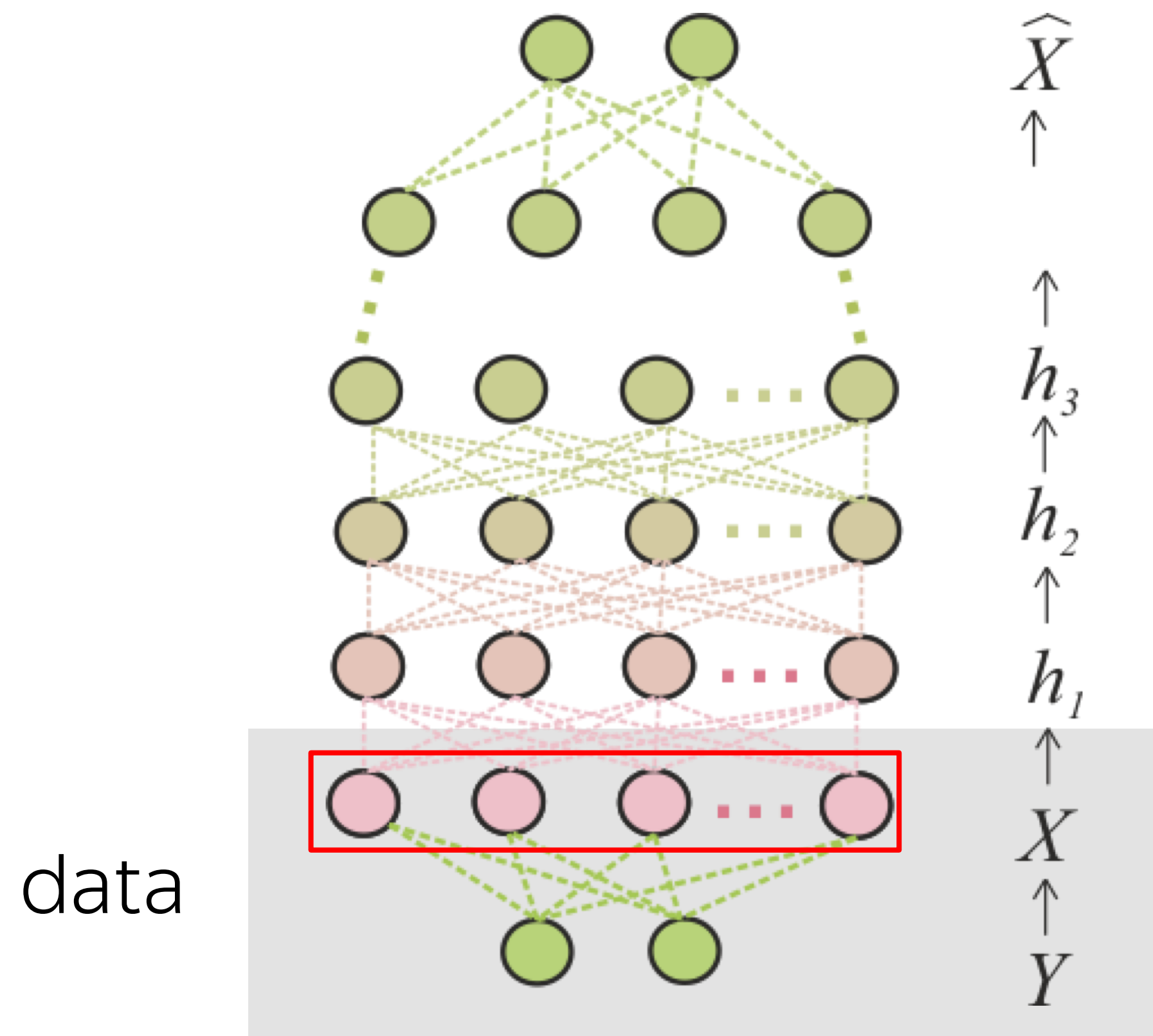
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- a sequence of layers is a Markov chain
- squeeze irrelevant to  $Y$  information while retaining relevant

# Information Bottleneck



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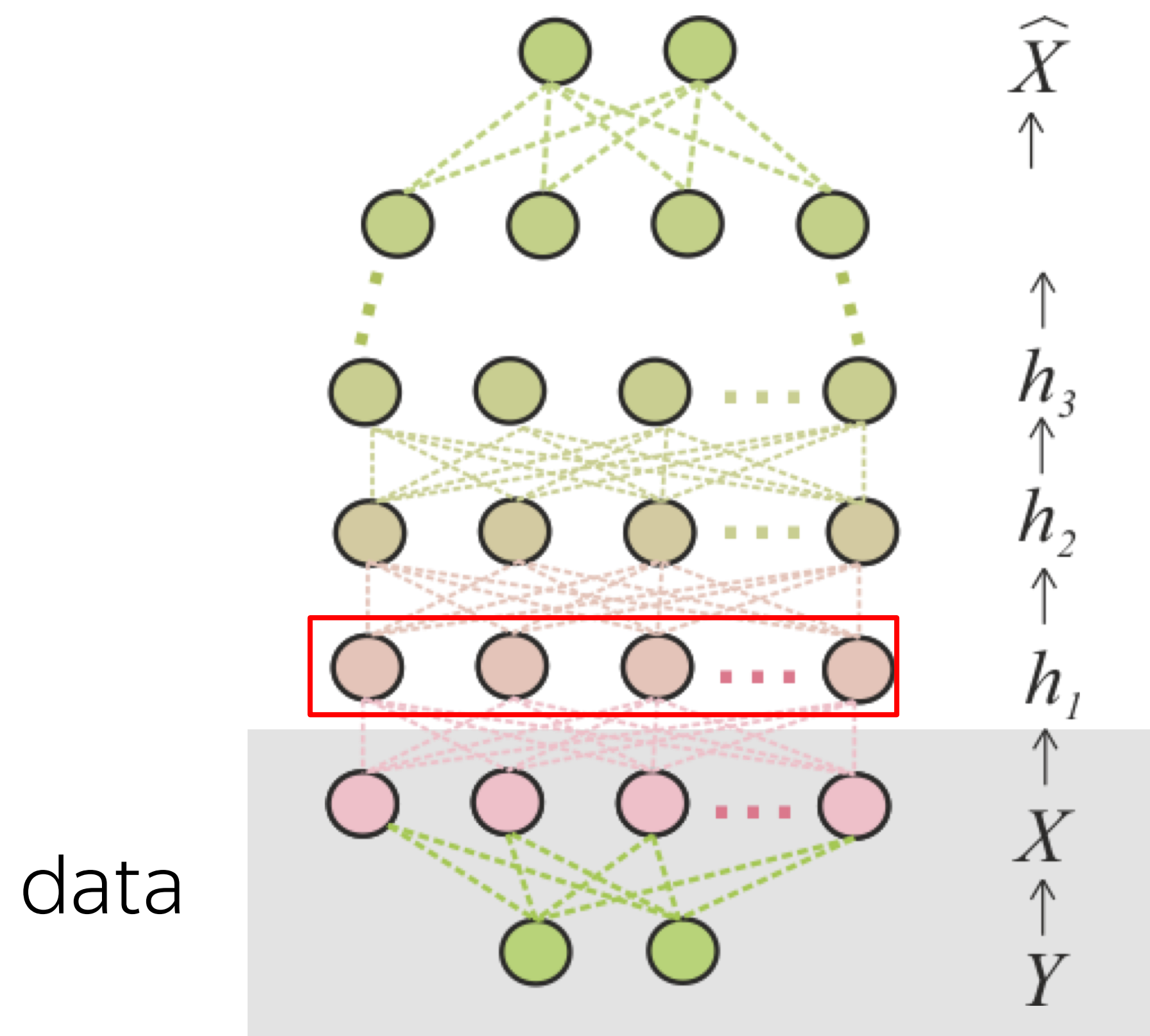
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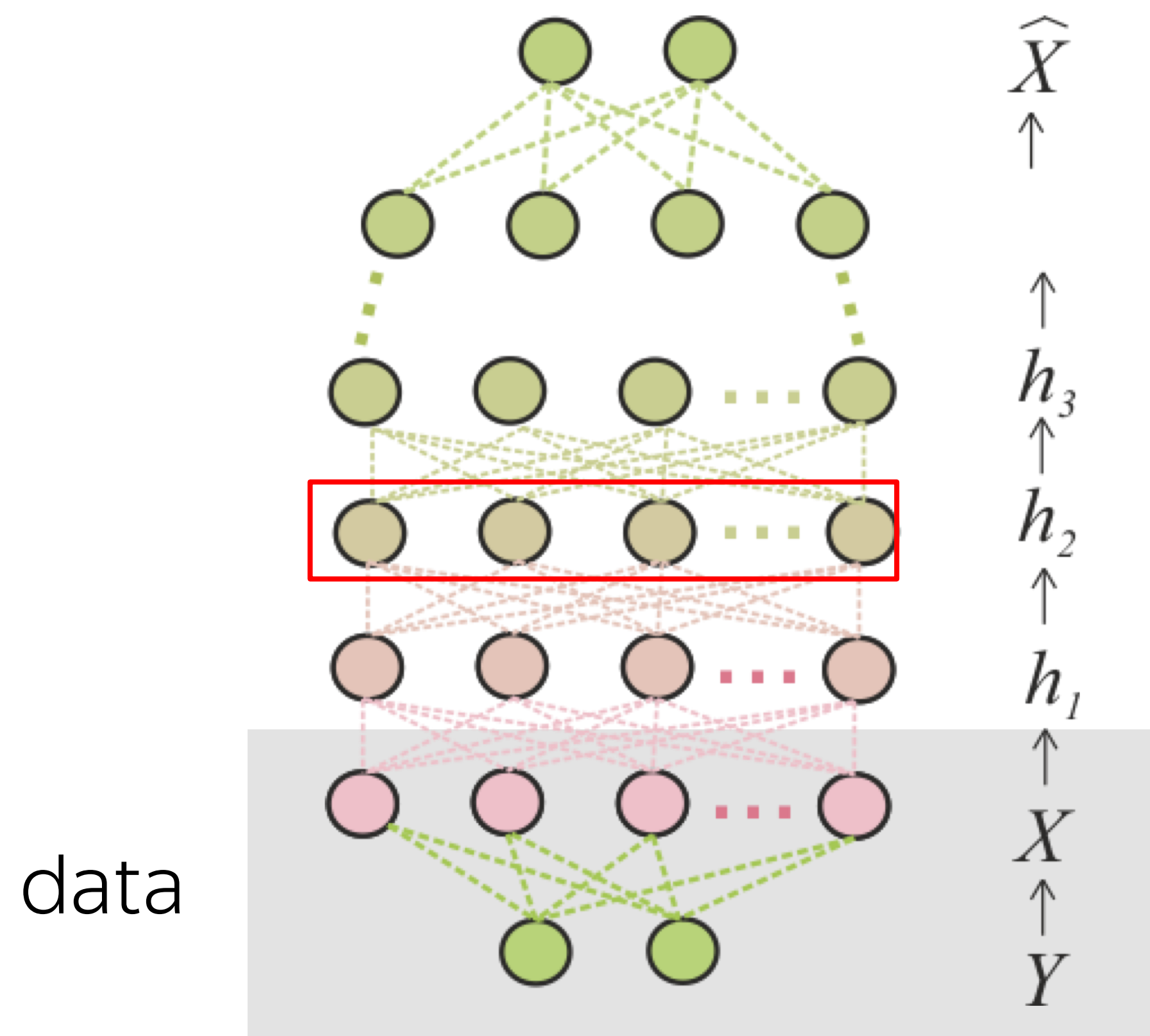
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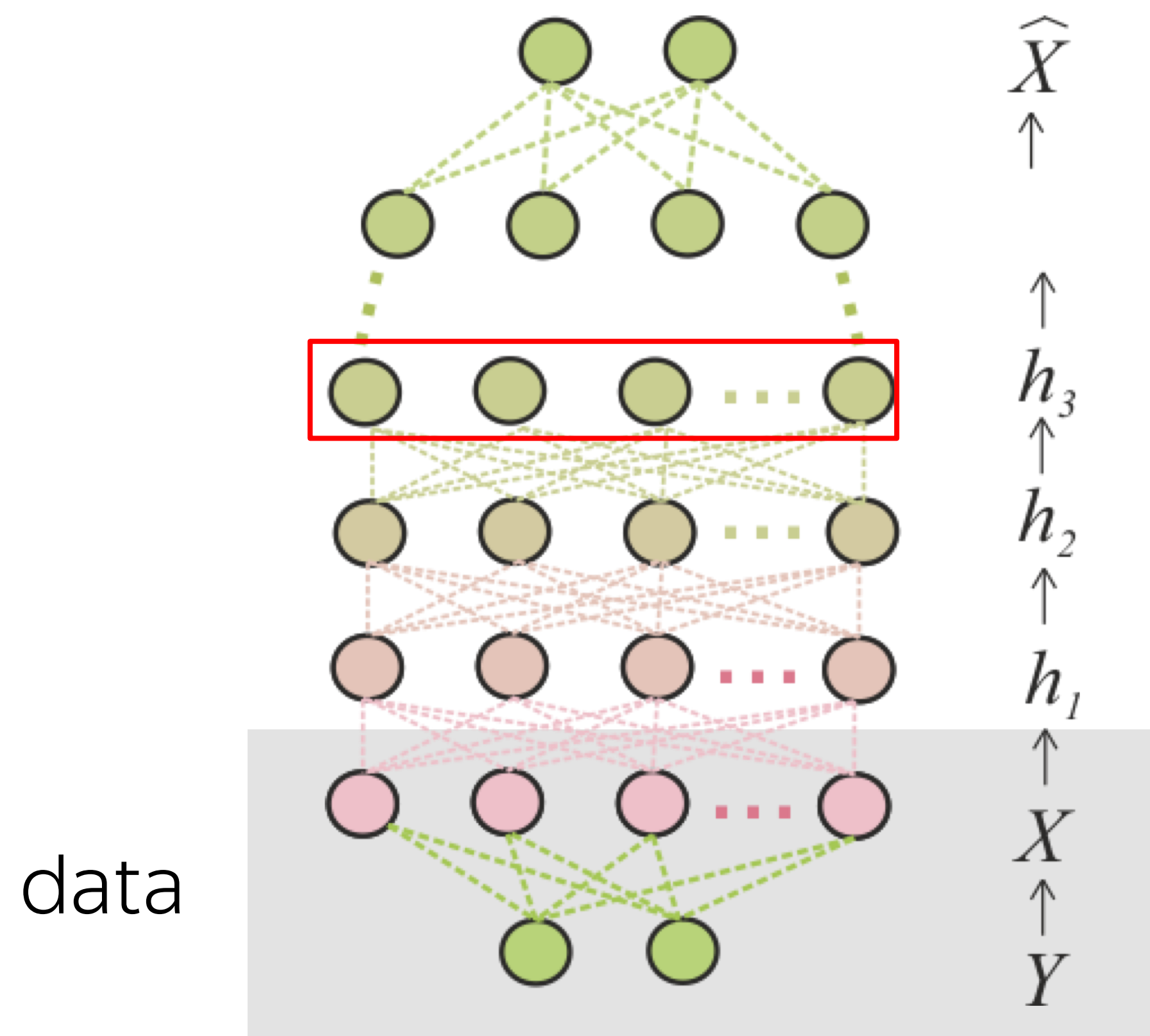
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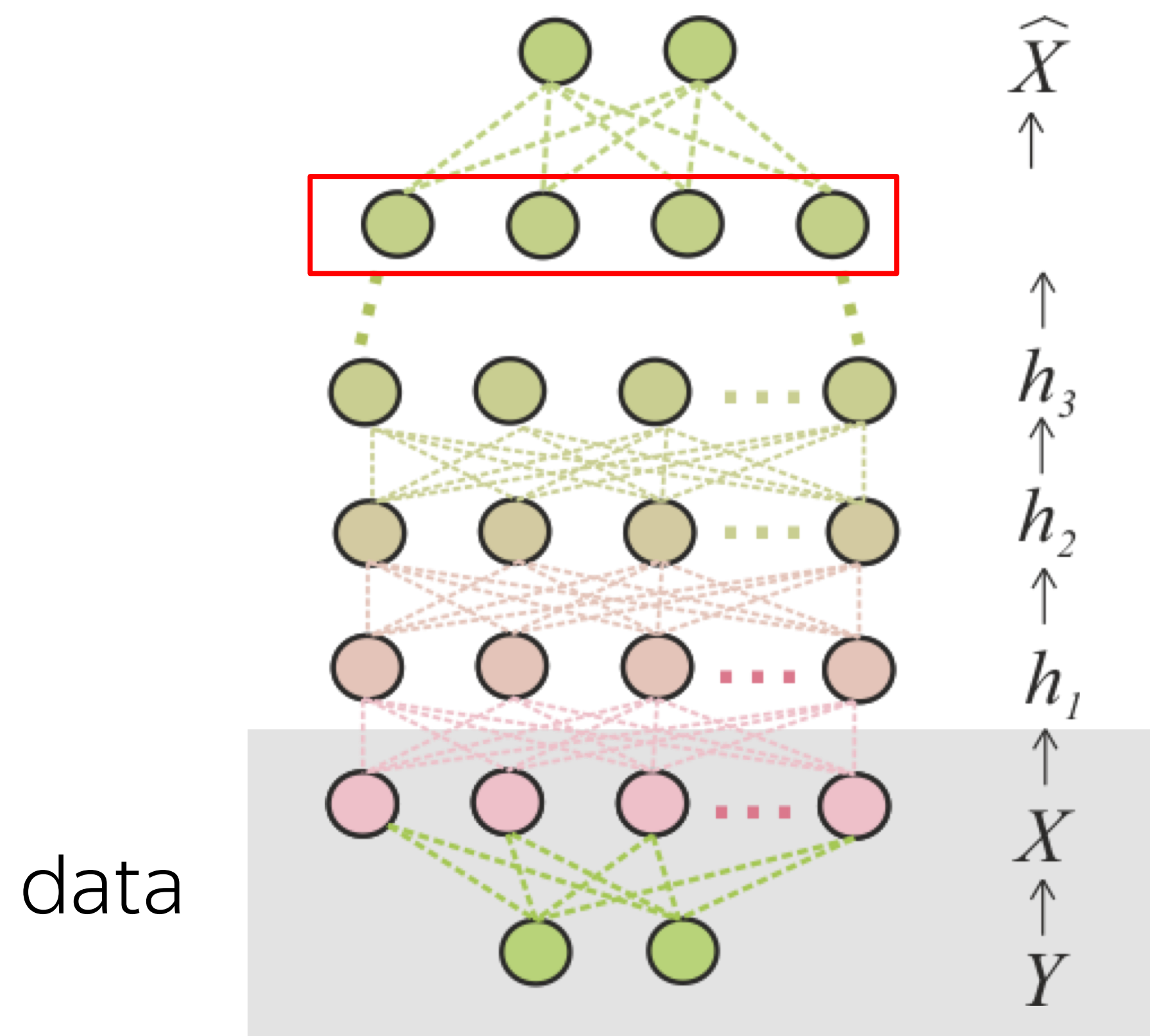
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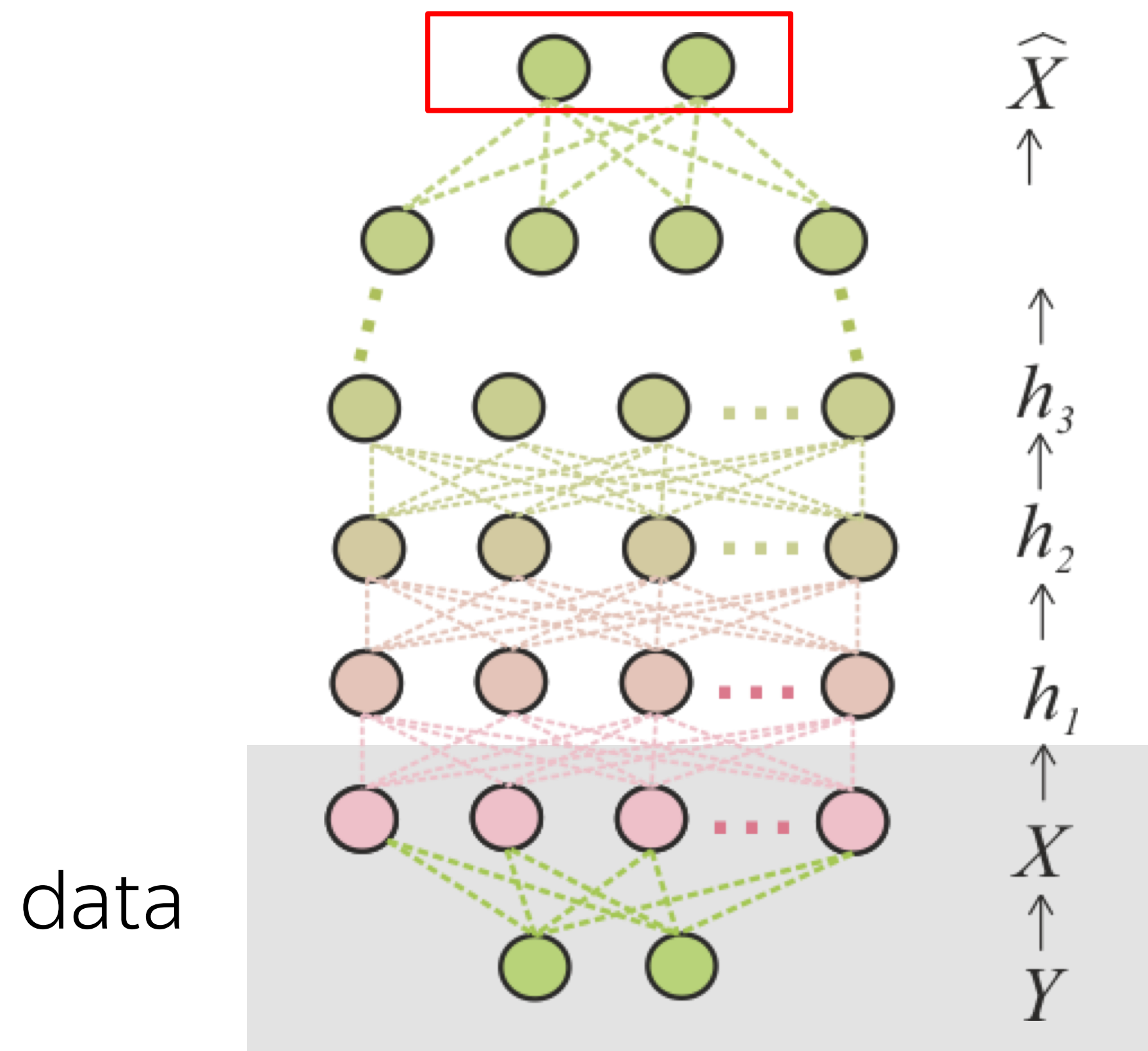
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- "Puzzles" from previous work
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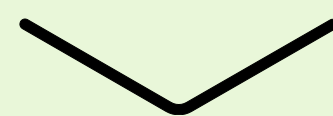
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- Information Bottleneck for token representations

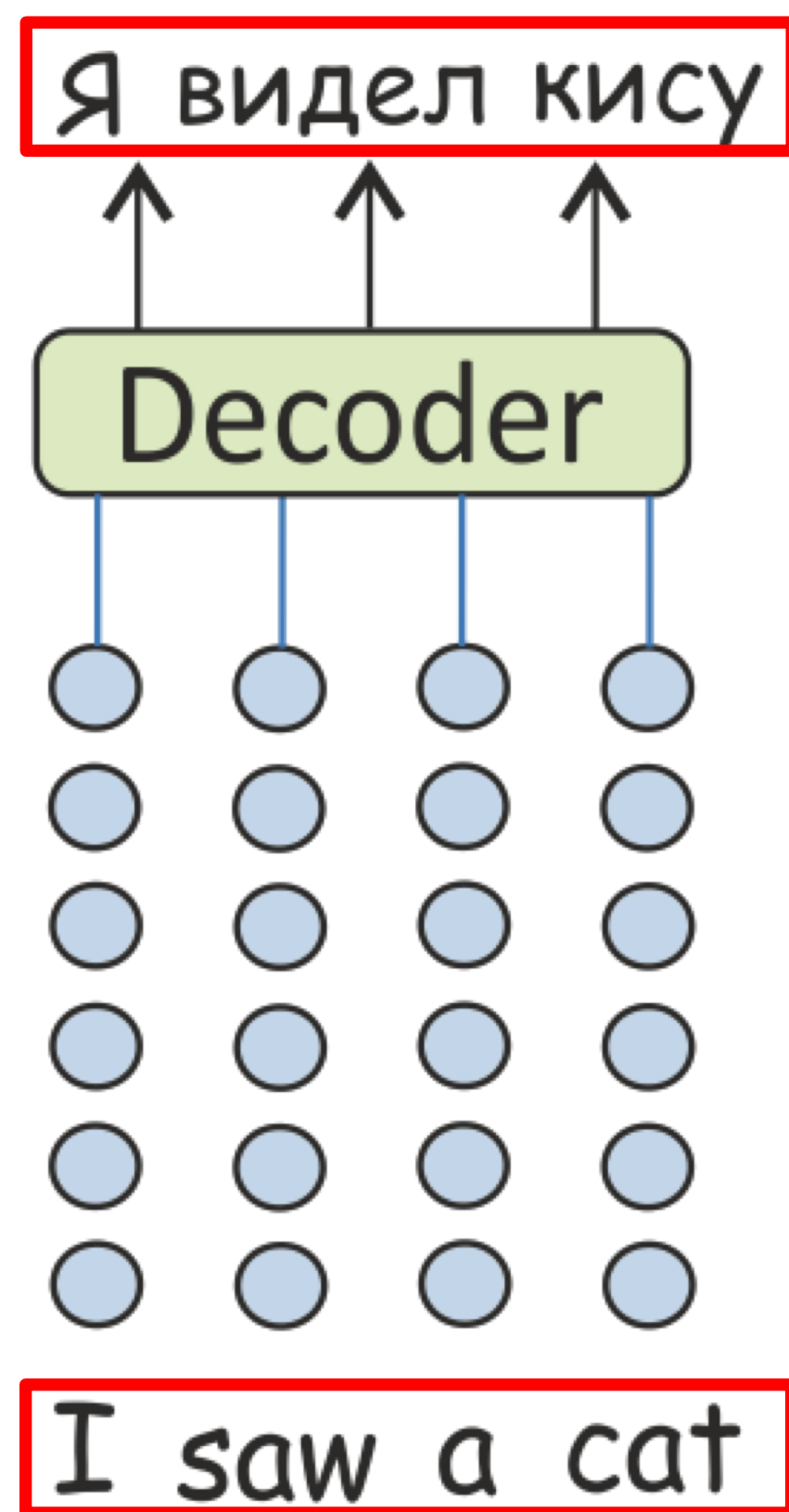
- ...

# Information Bottleneck for Token Representations

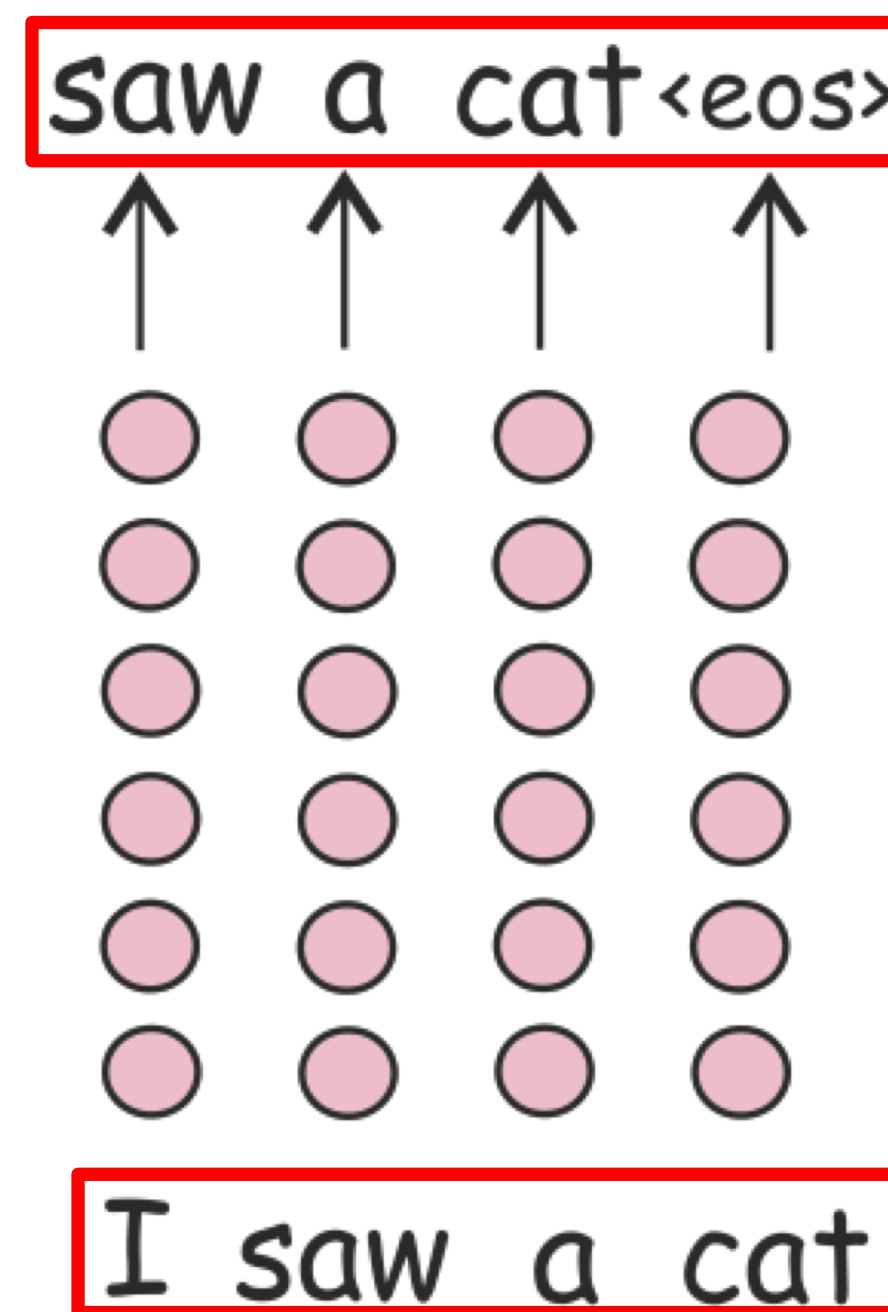


# Model as a function from input to output

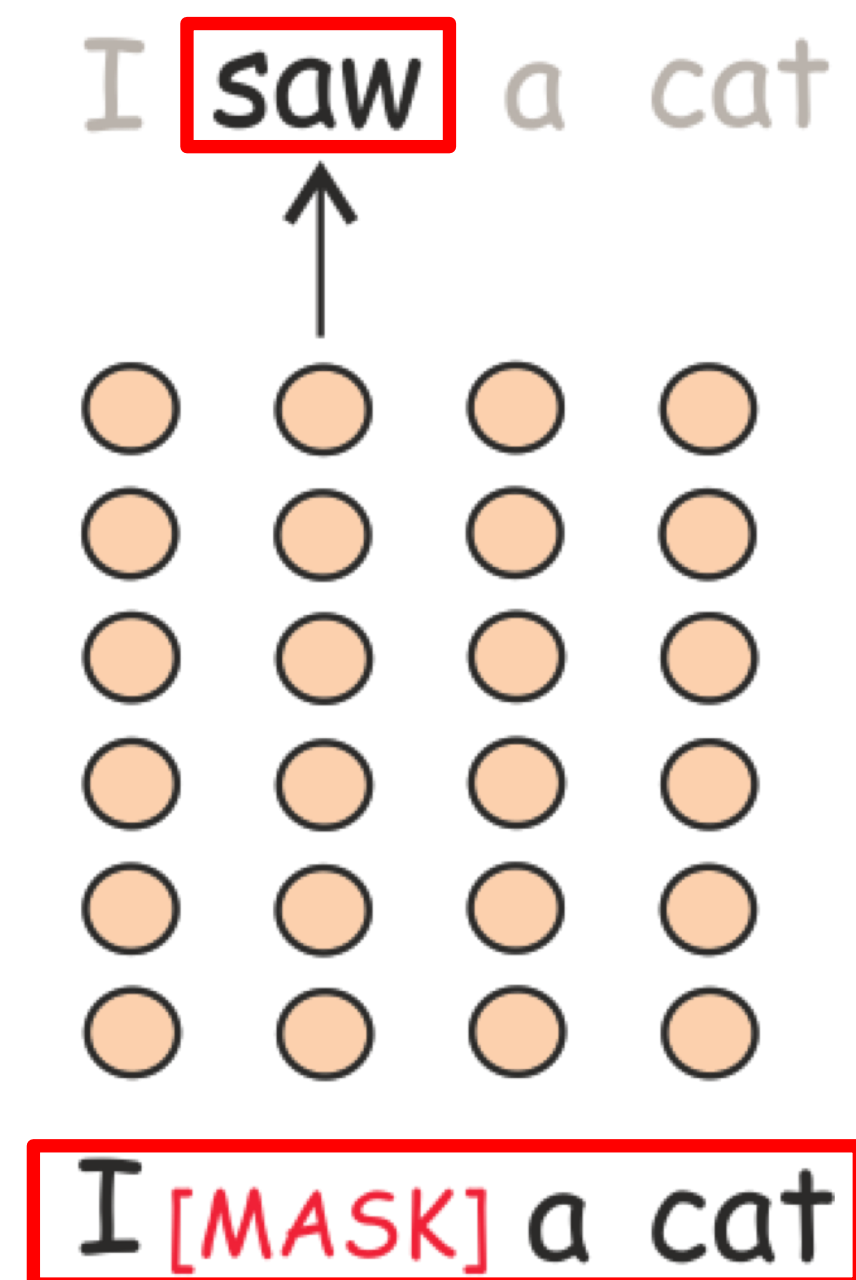
MT



LM



MLM

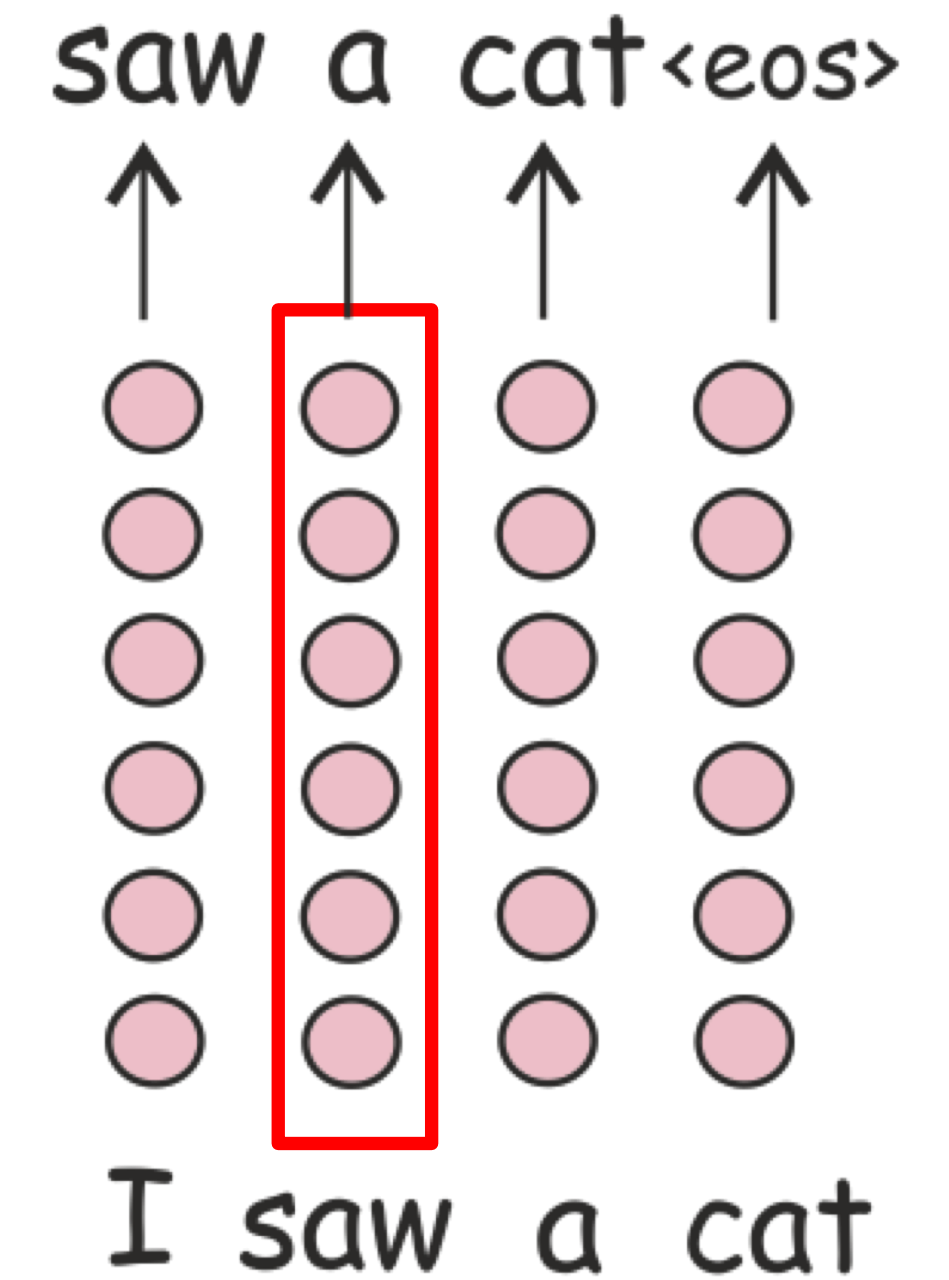


output

input

# Our setting: representations of individual tokens

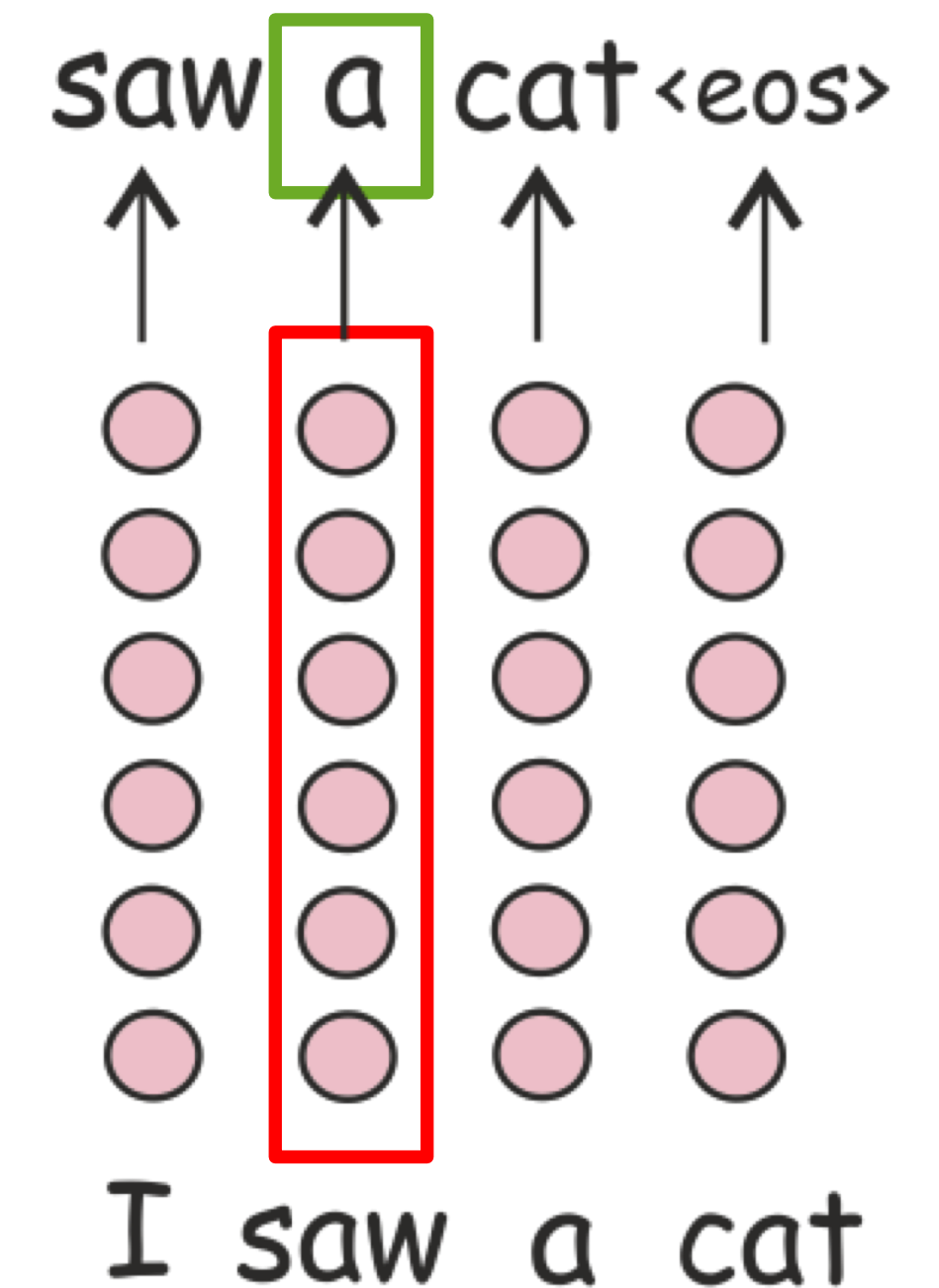
Two roles a token representation plays:



# Our setting: representations of individual tokens

Two roles a token representation plays:

- Predicting the **output label**

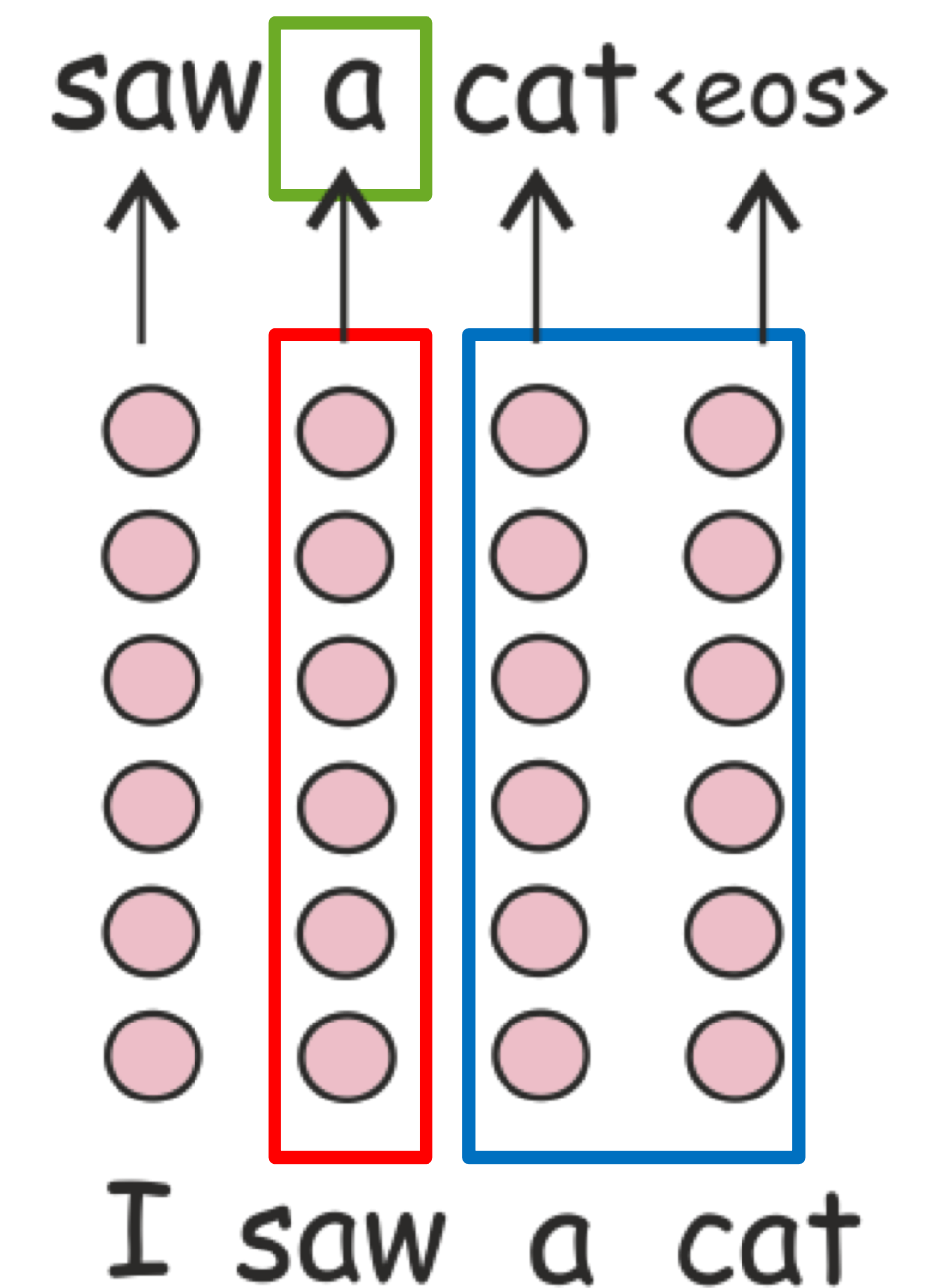




# Our setting: representations of individual tokens

Two roles a token representation plays:

- Predicting the **output label**
- Preserving information necessary to build **representations of other tokens**

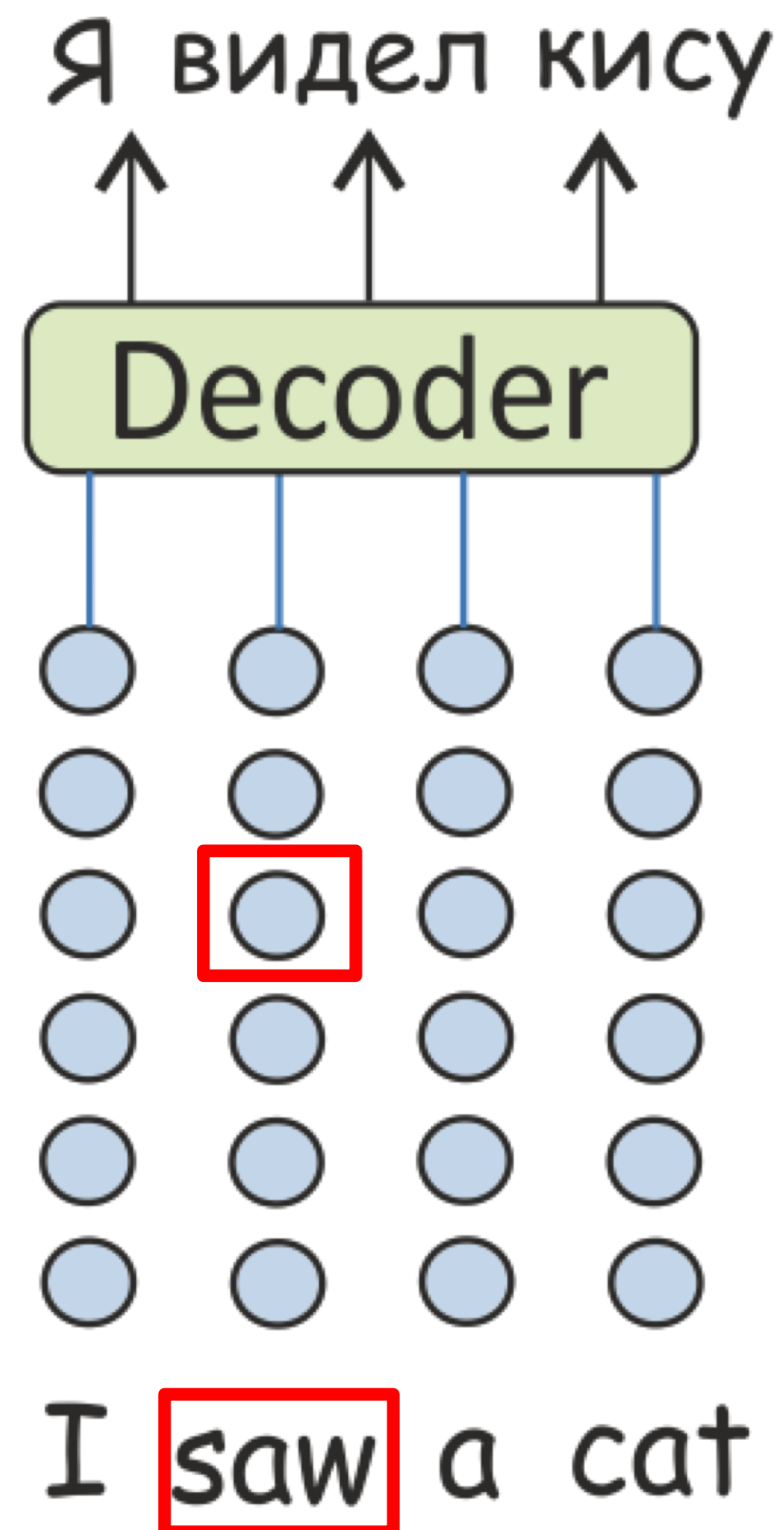


# The task defines:

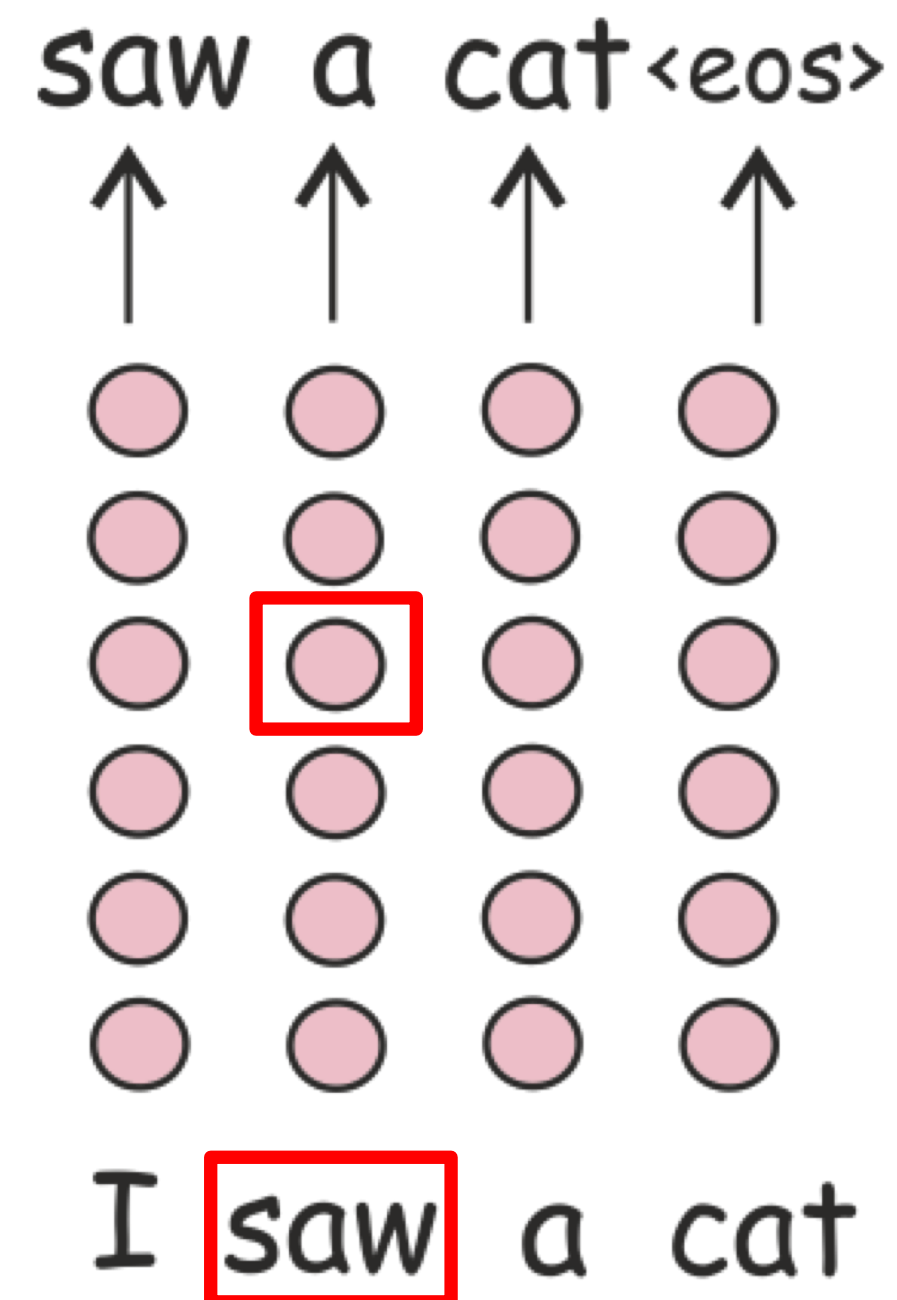
- the nature of changes a token representation undergoes, from layer to layer
- the process of interactions and relationships between tokens
- the type of information which gets lost and acquired by a token representation in these interactions

# MI between an input token and a representation

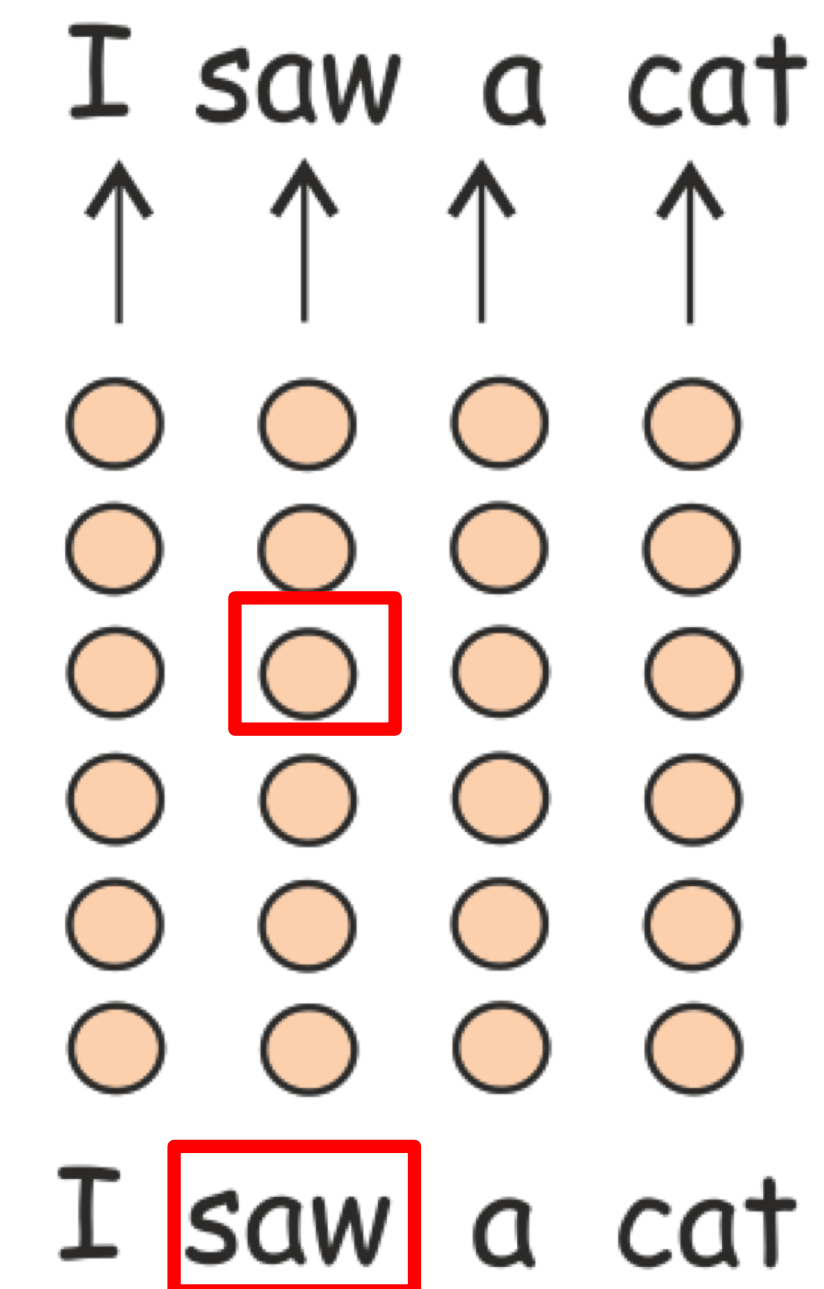
MT



LM

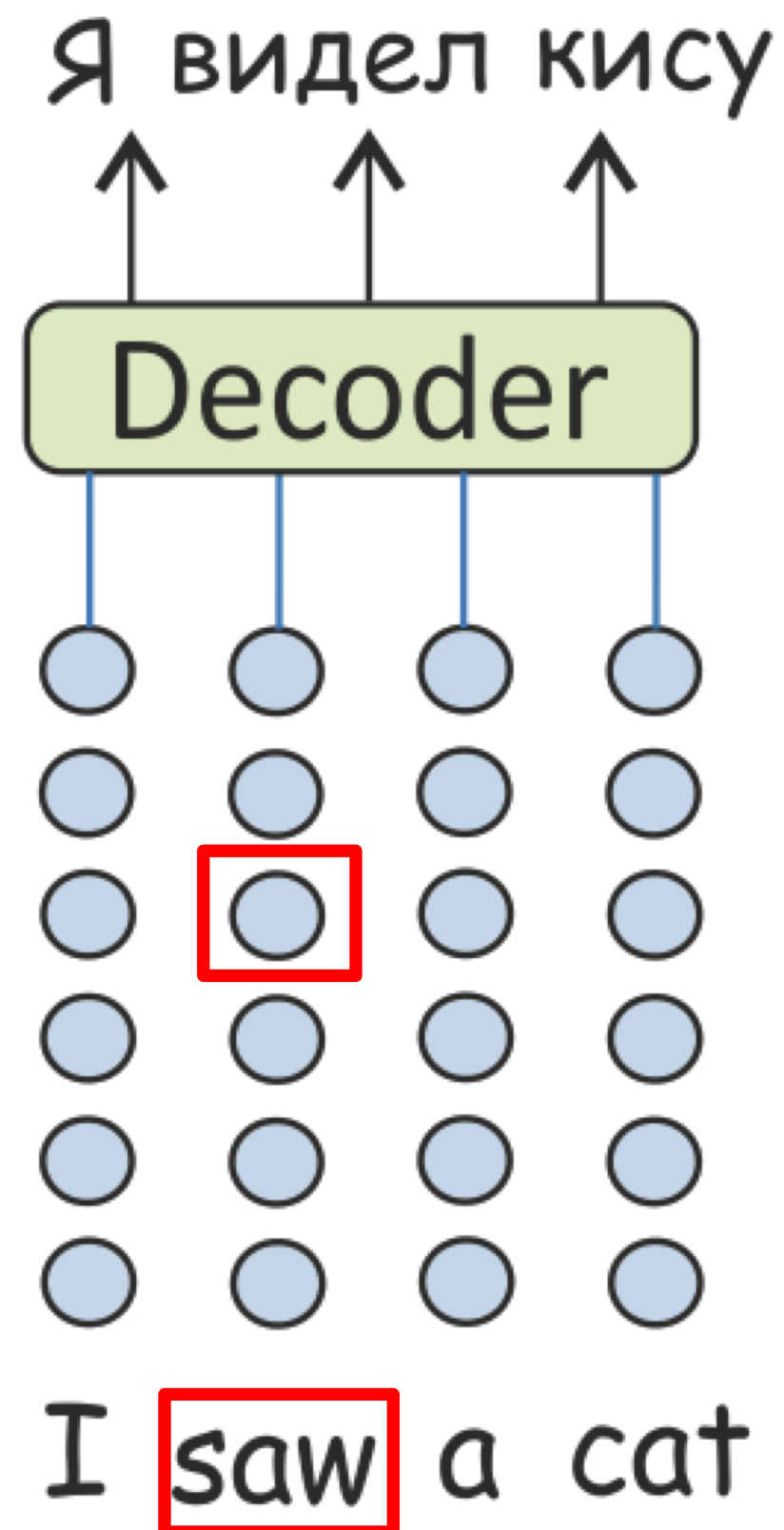


MLM

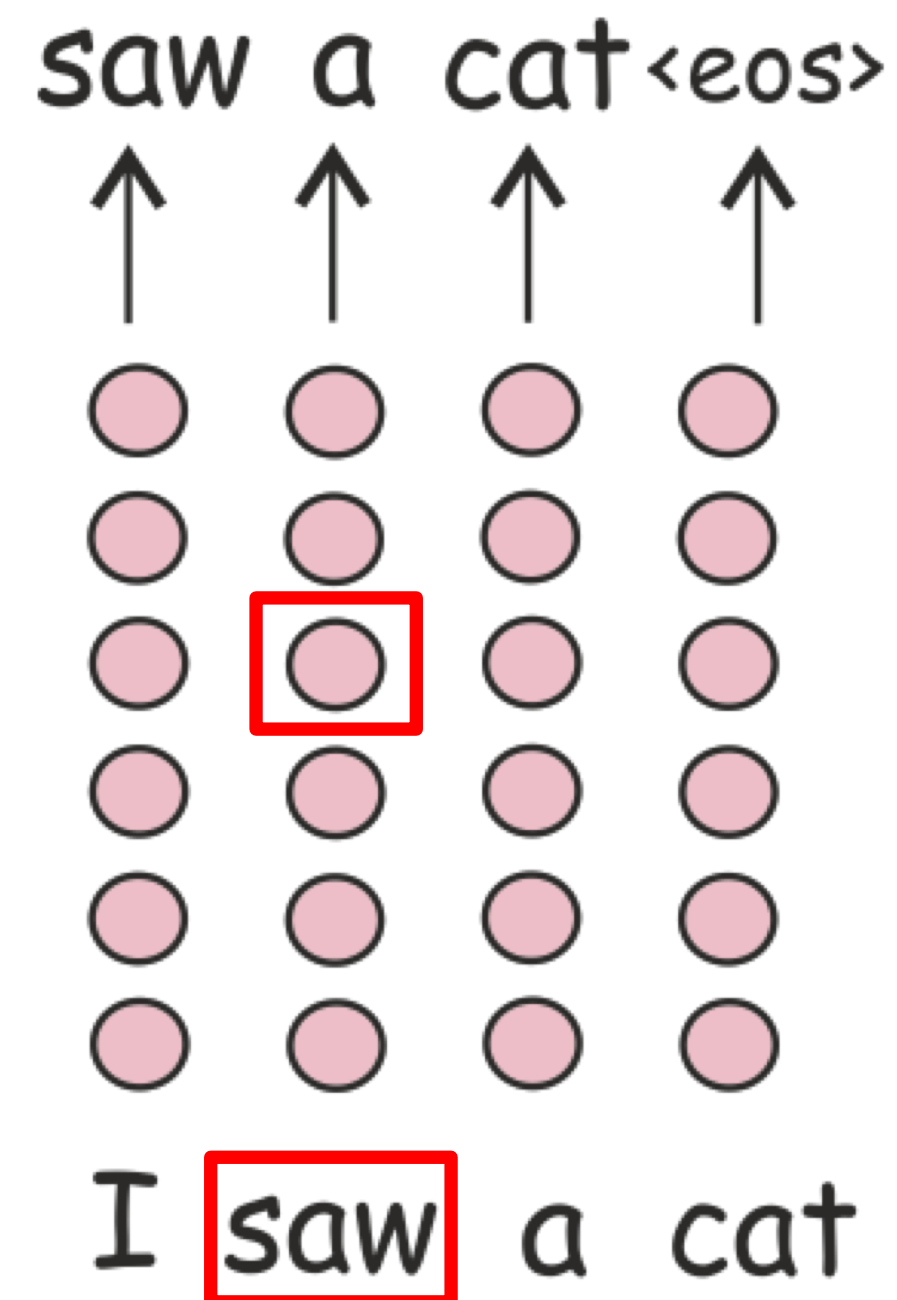


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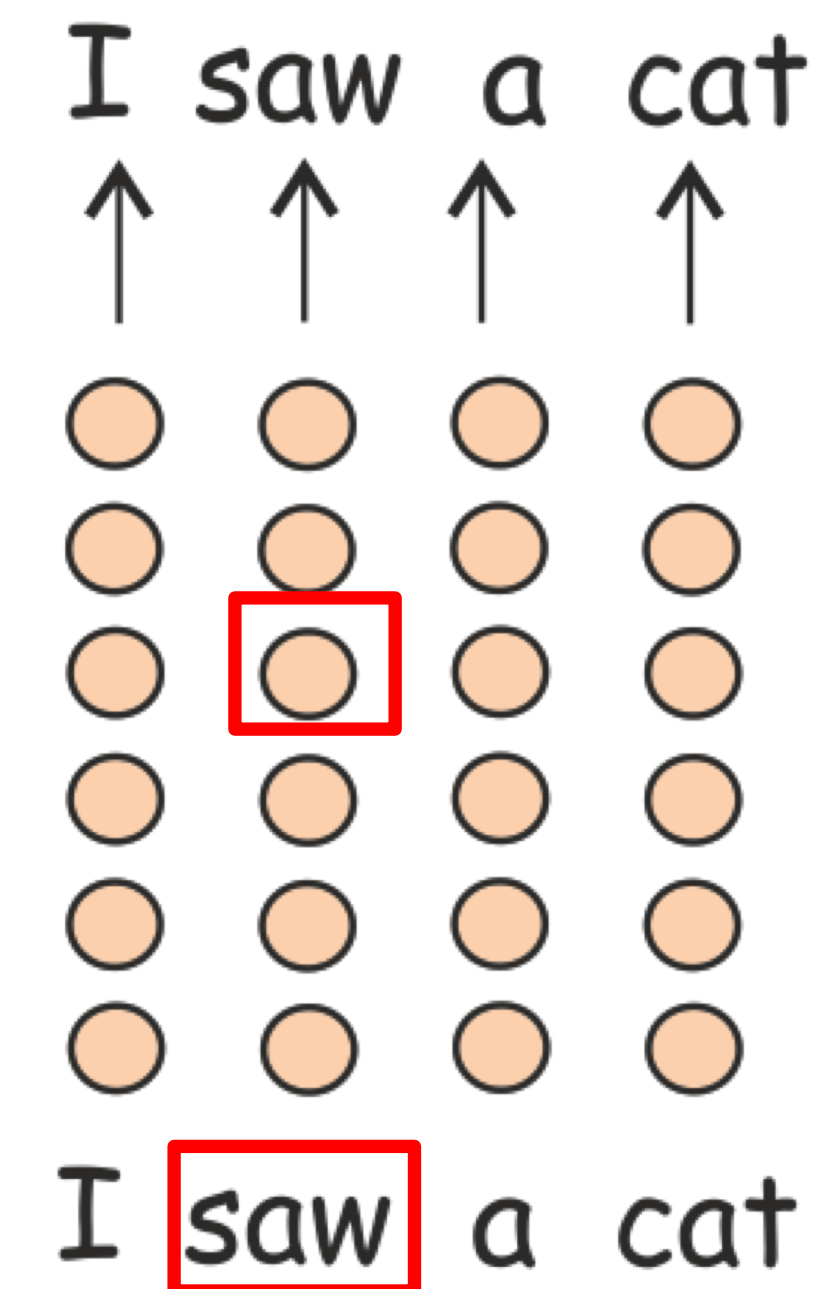
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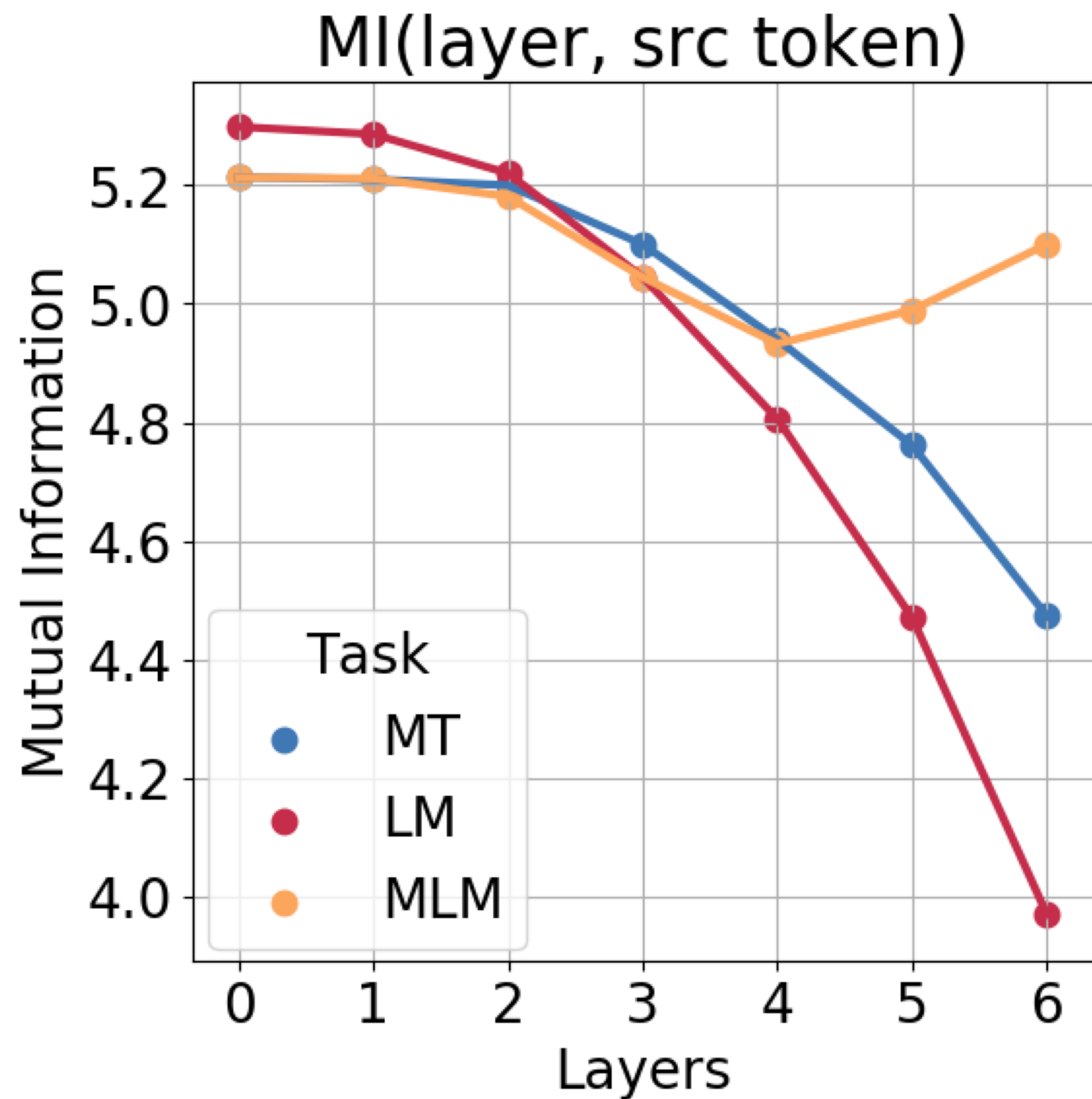


MLM

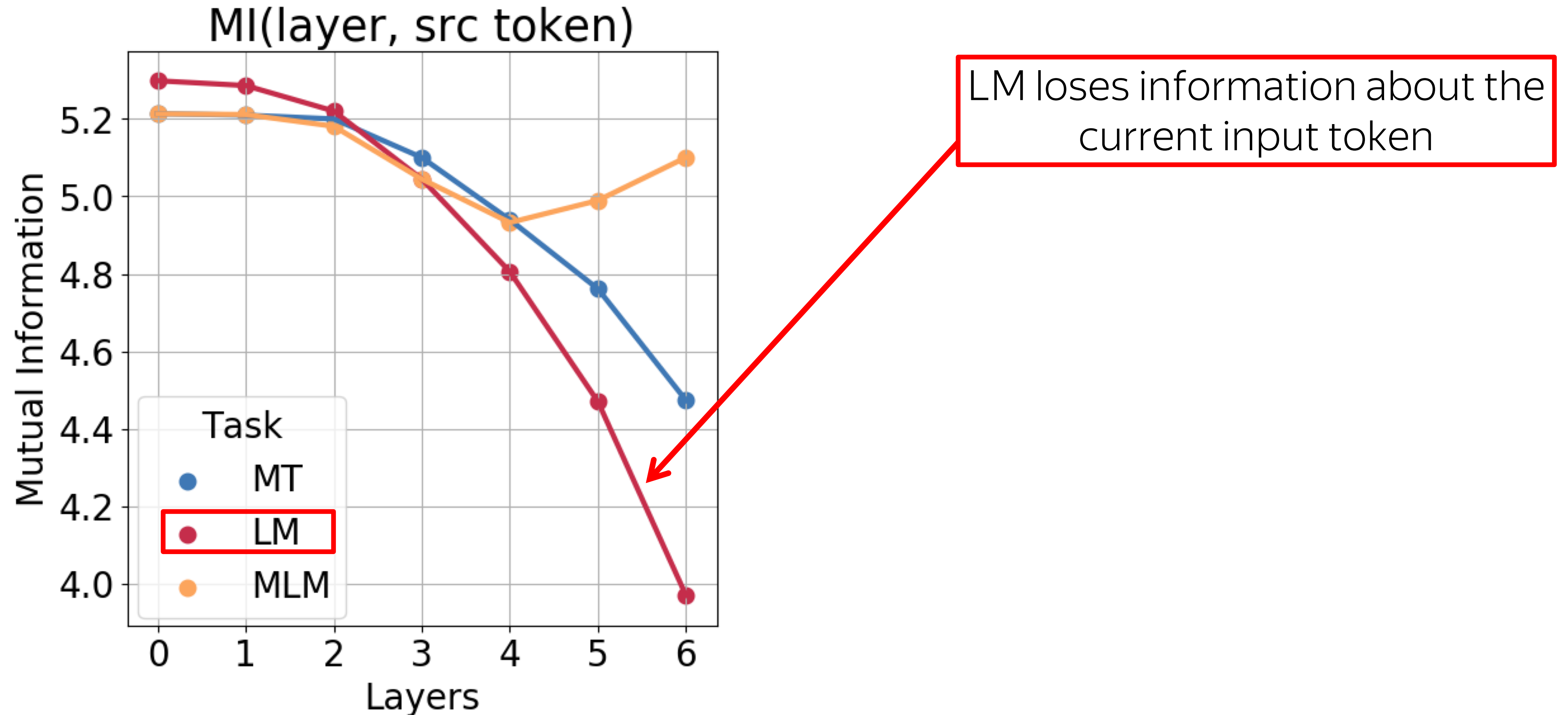


As at test time:  
No masking

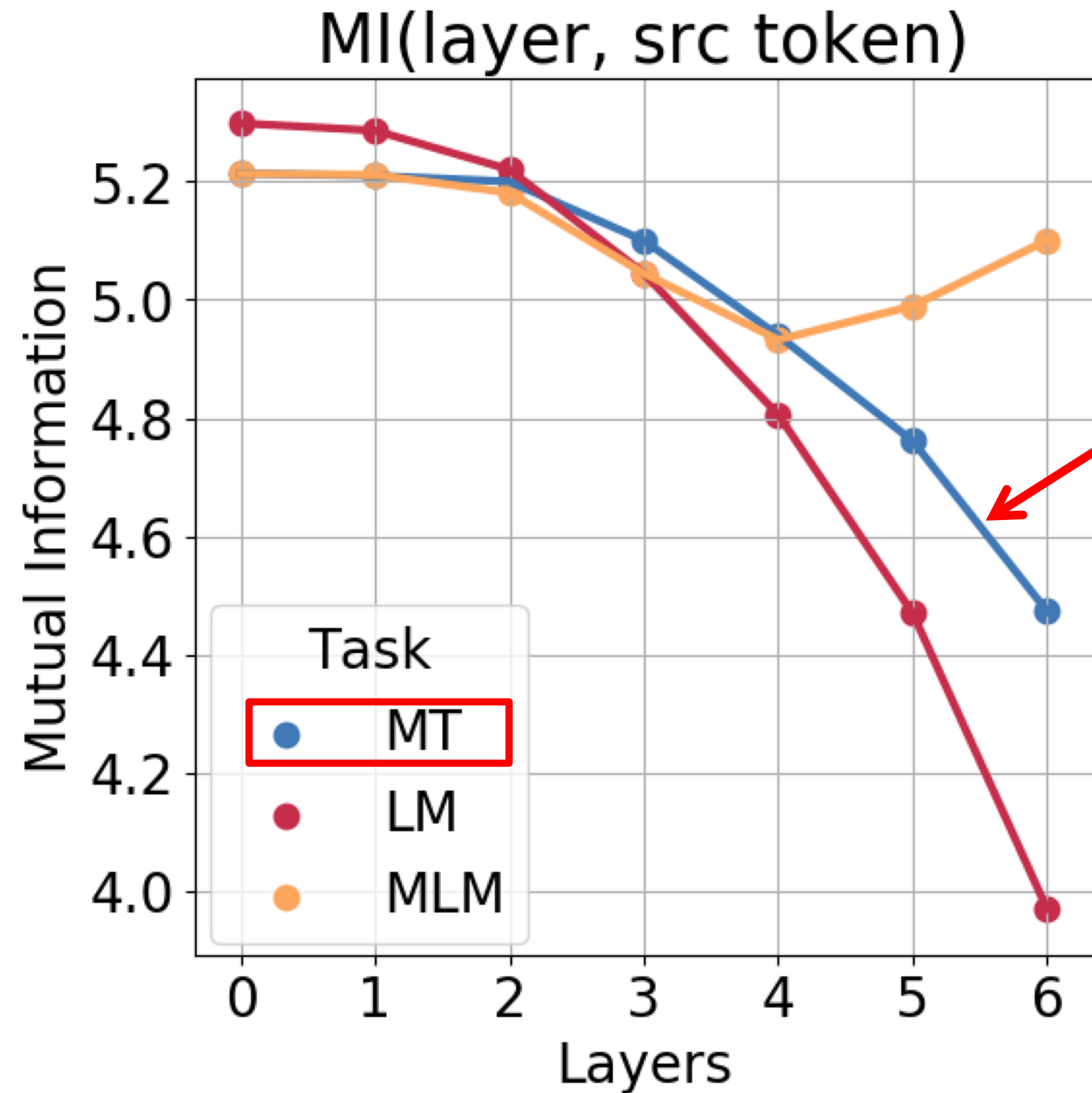
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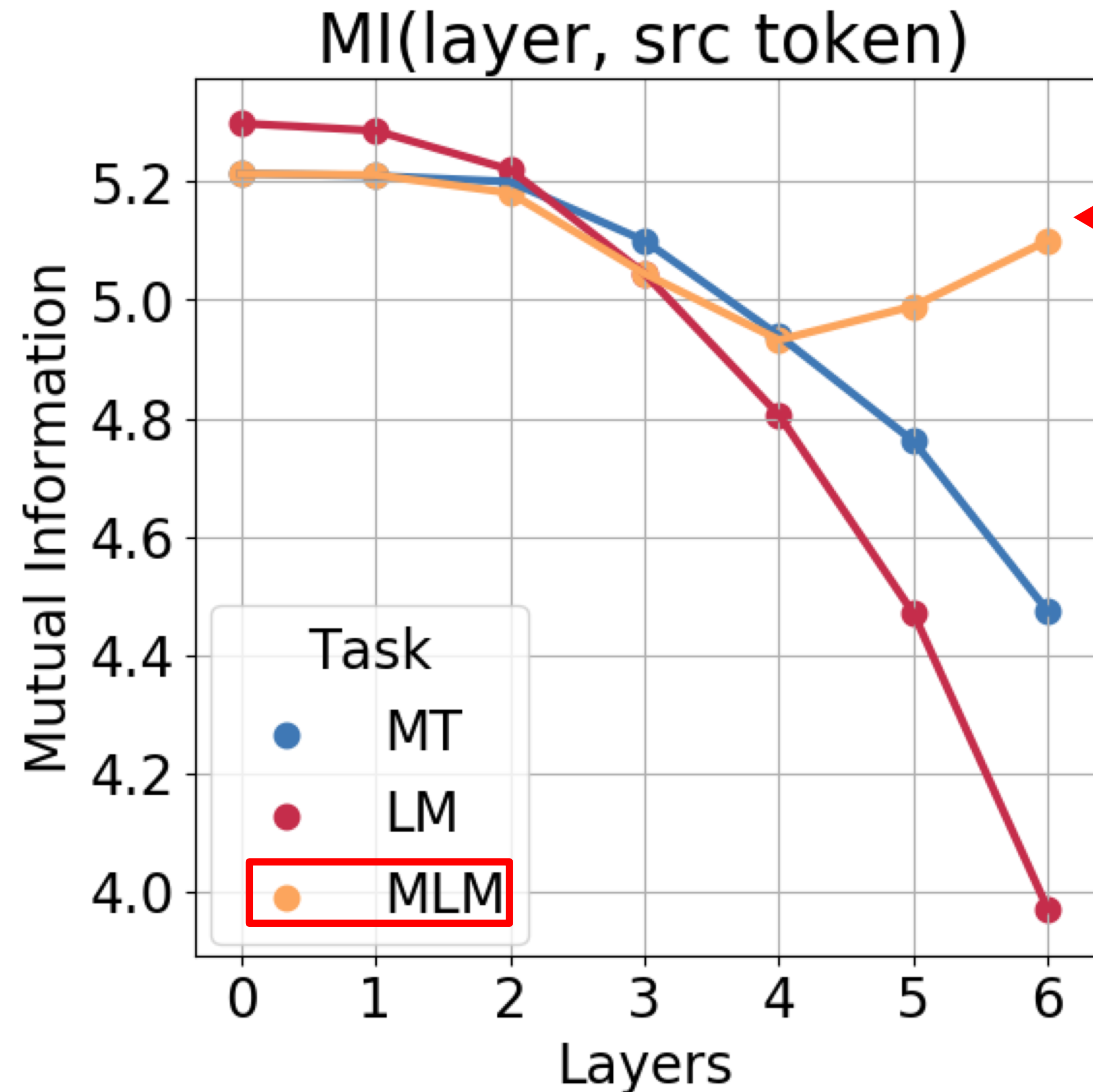


# MI between an input token and a representation



For MT, the behavior is similar, but to lesser extent

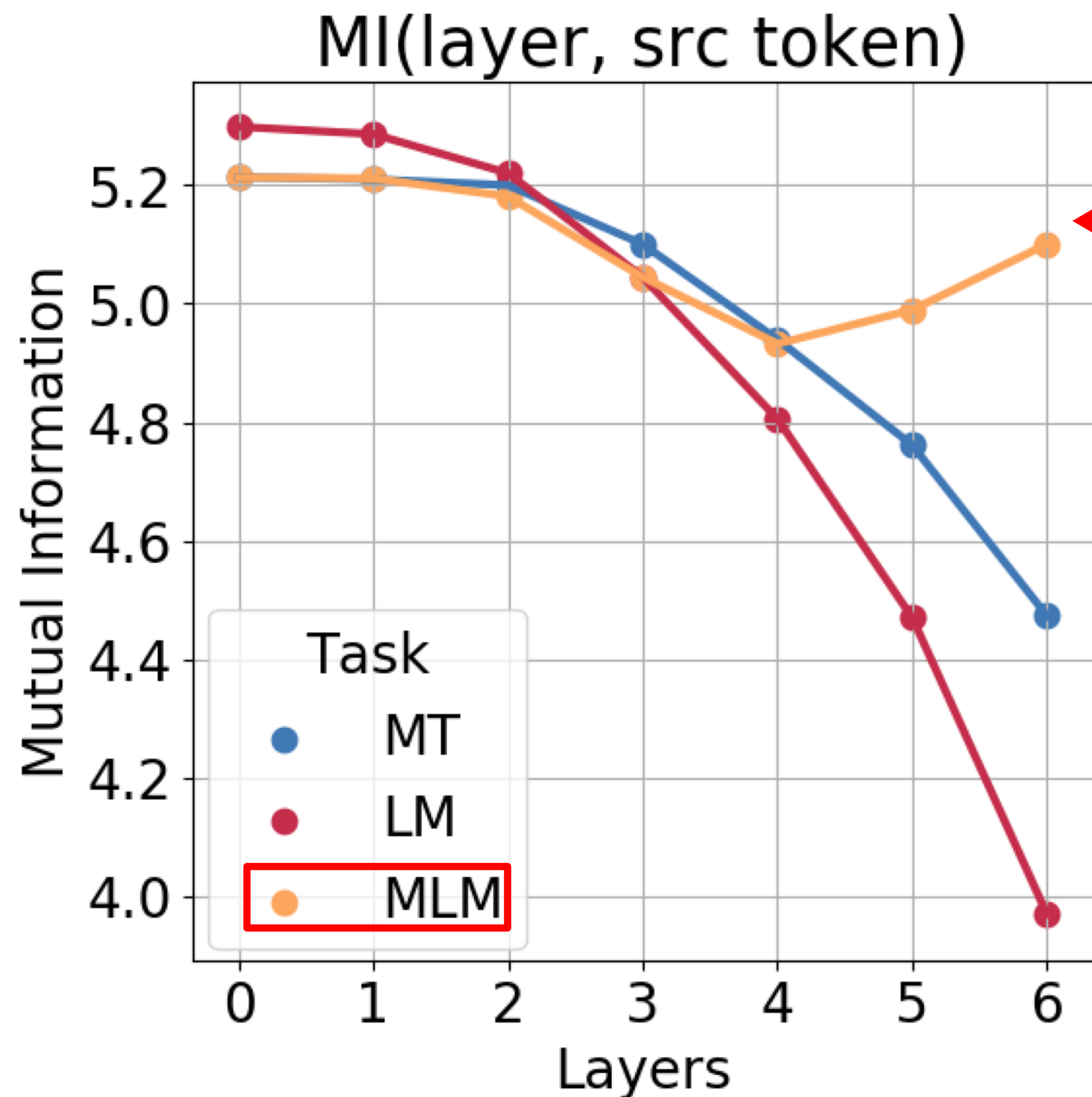
# MI between an input token and a representation



For MLM, the information about input token gets lost, then recovered



# MI between an input token and a representation

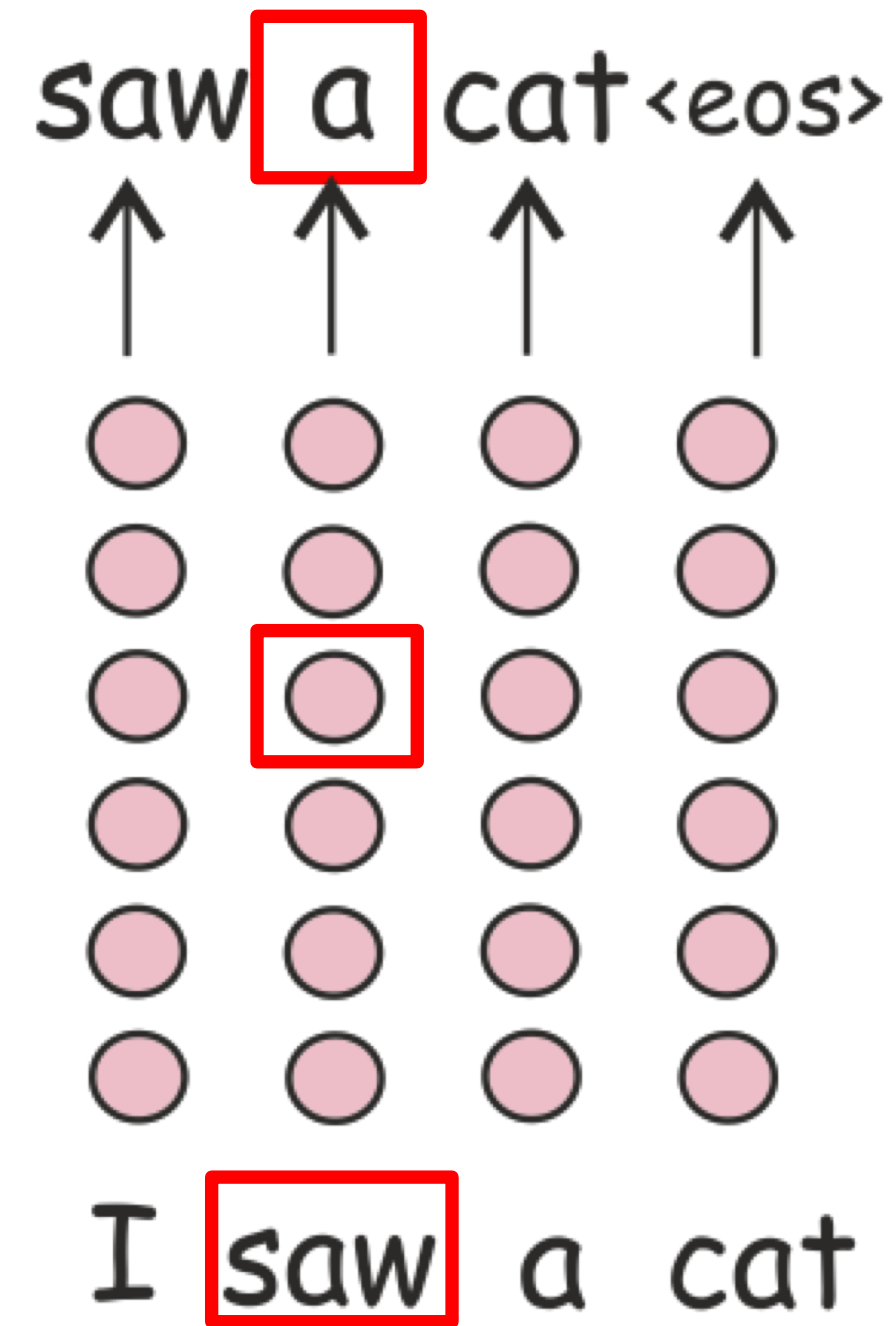


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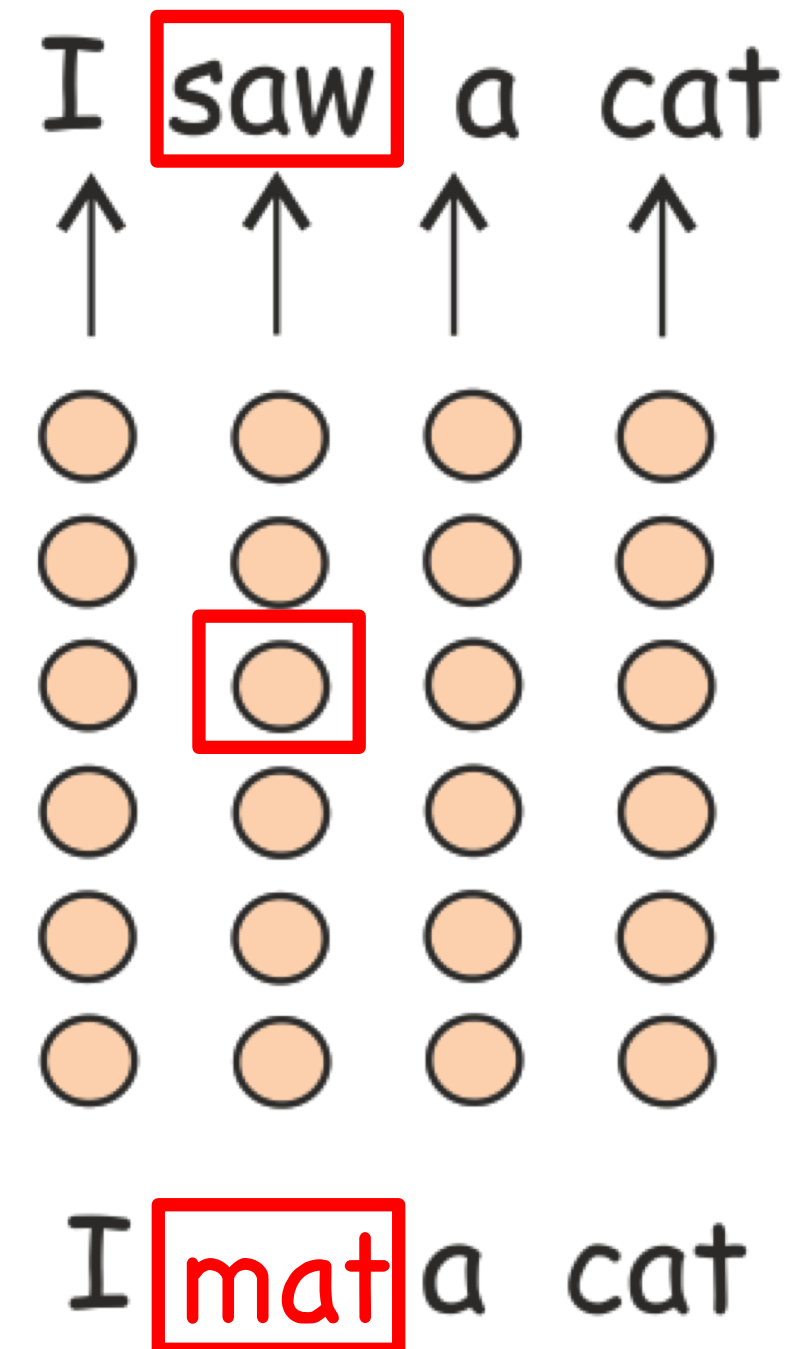
Two stages:  
'context encoding' and  
'token reconstruction'

# MI between a representation and both input and output

LM

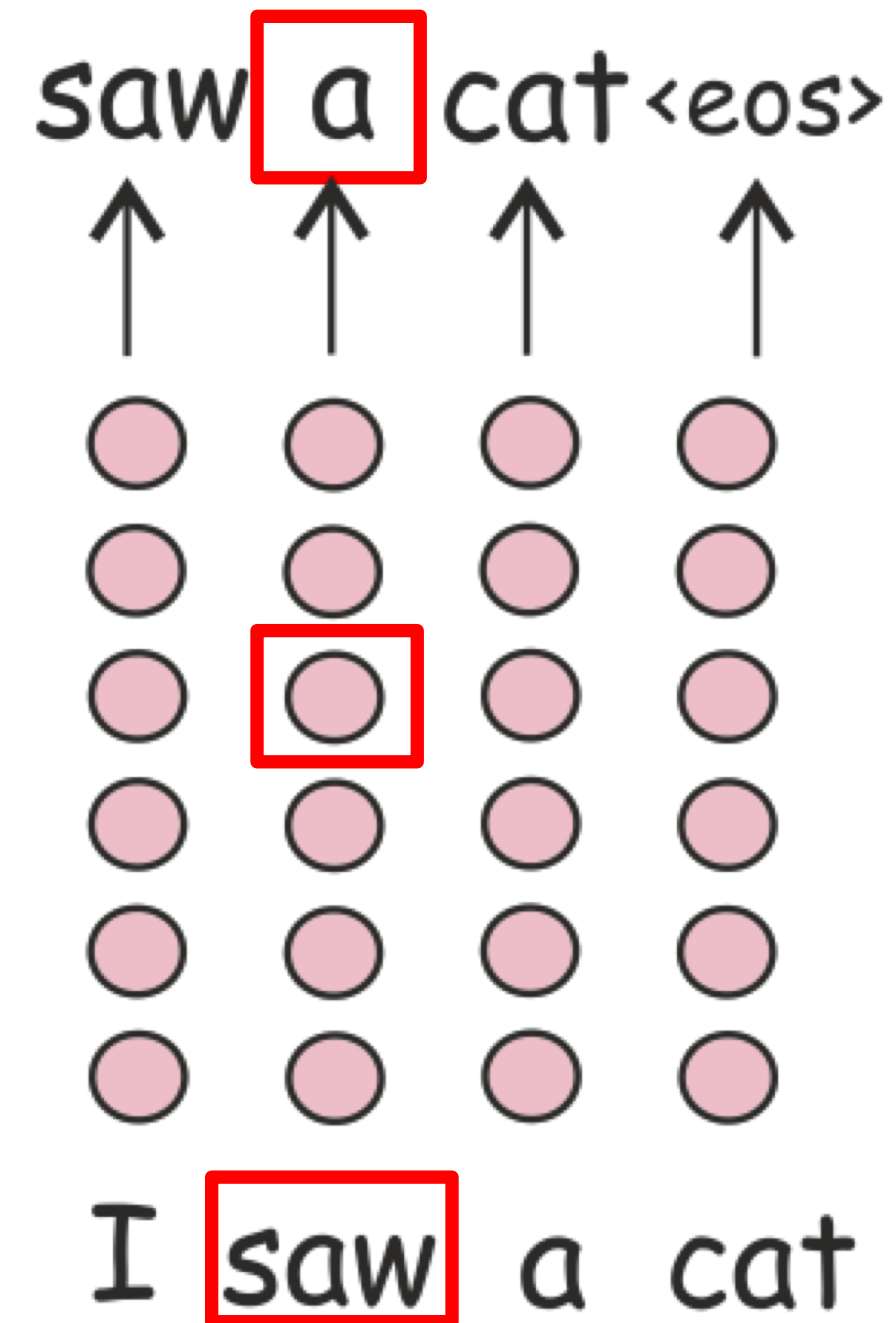


MLM

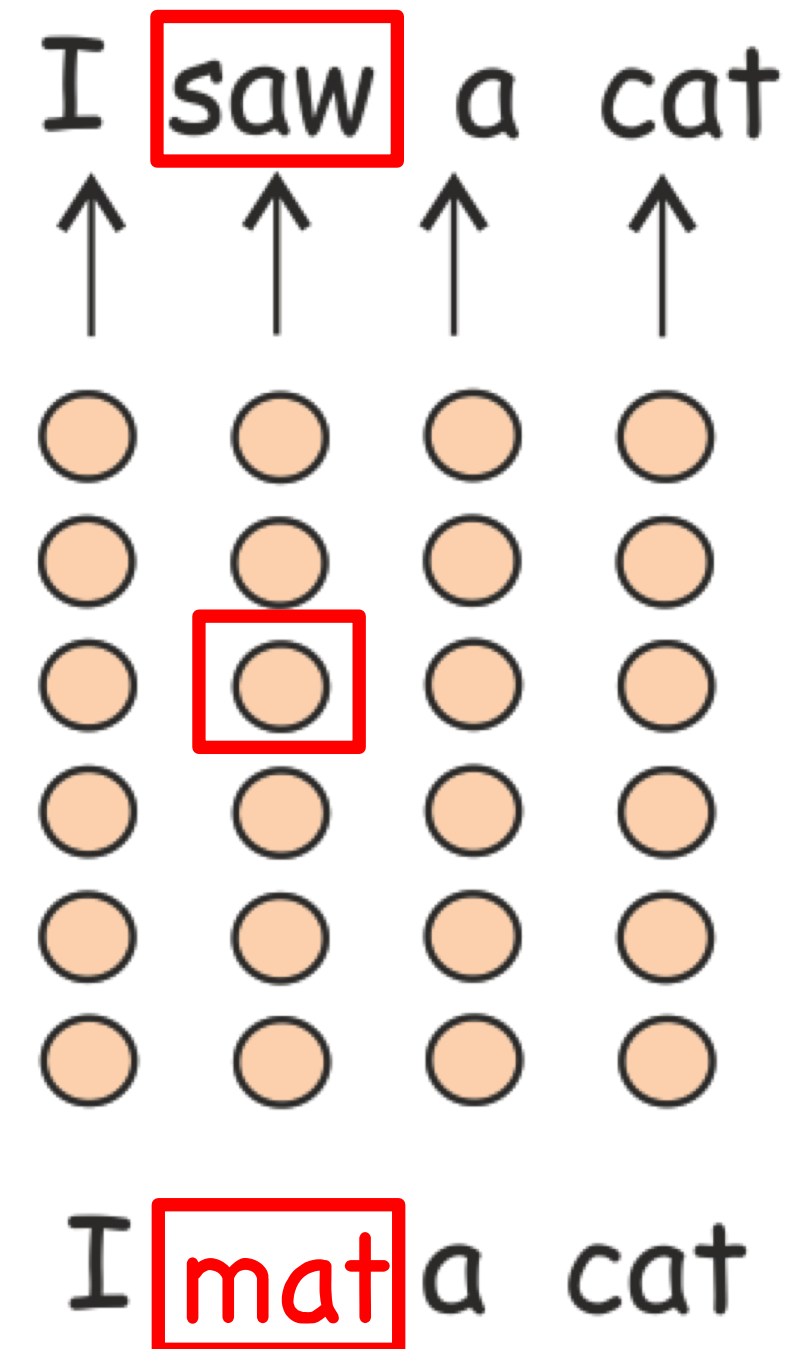


# MI between a representation and both input and output

LM



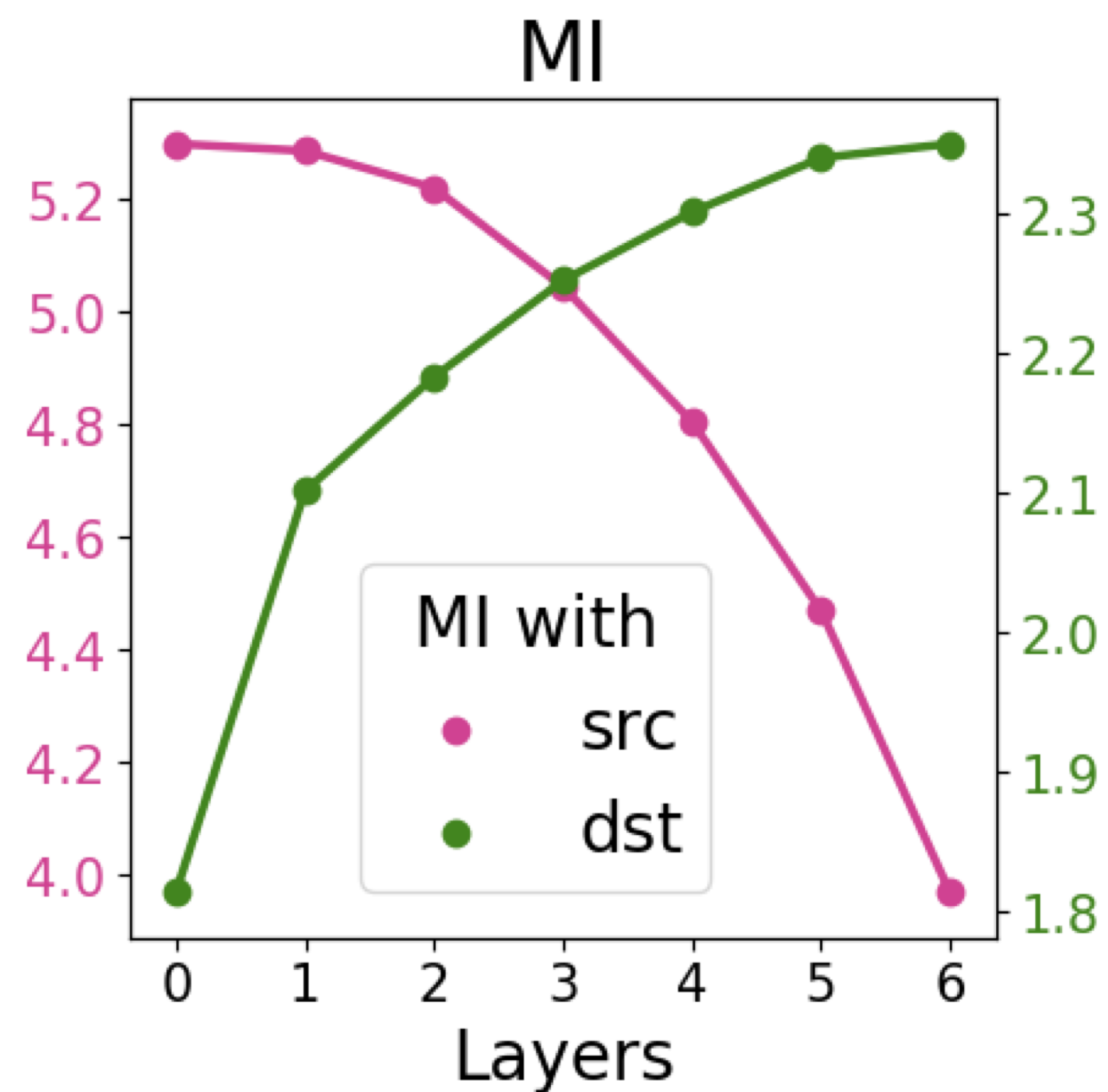
MLM



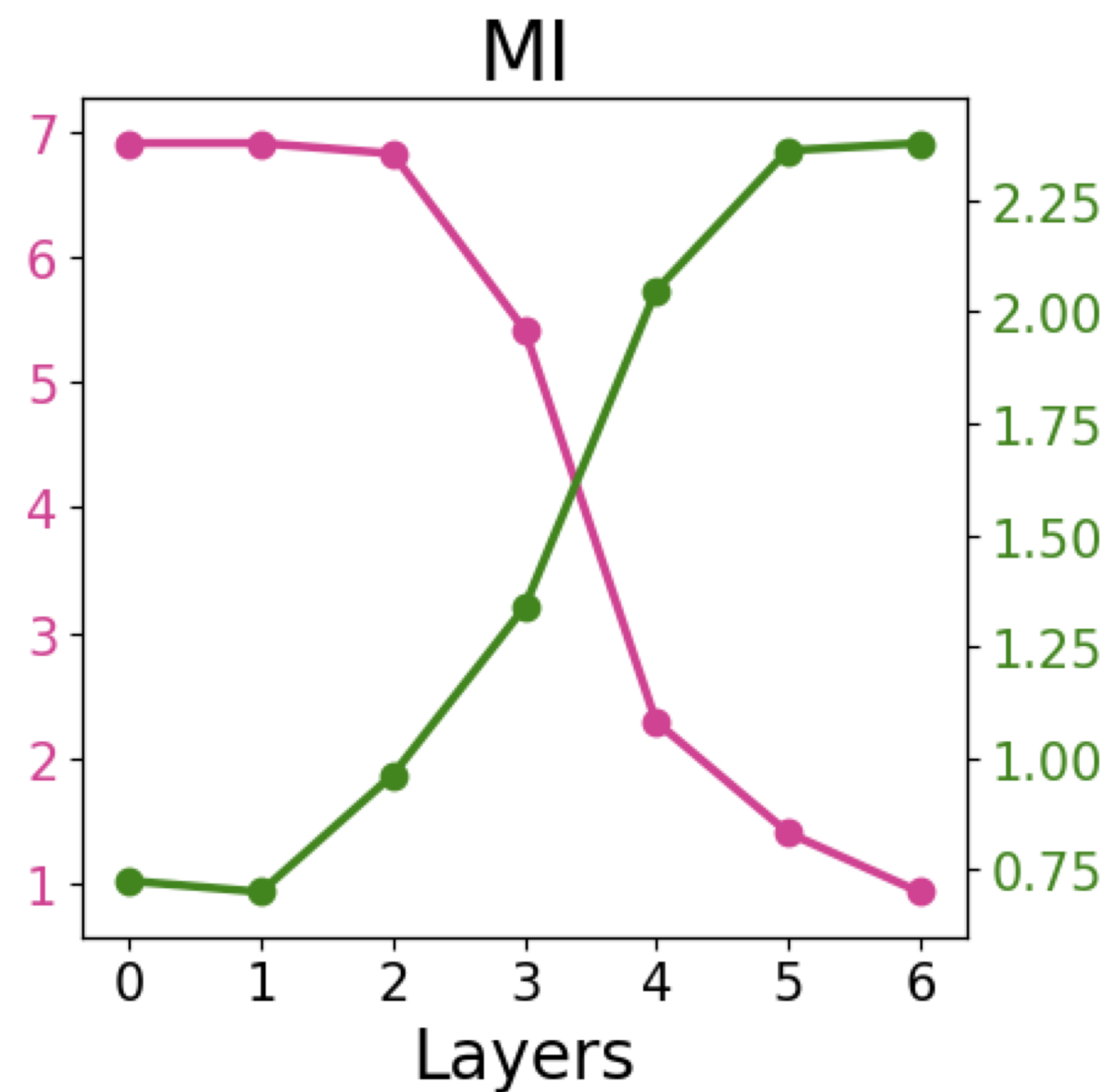
As in training:  
With masking and replacing

# MI with both input and output tokens

LM



MLM



For MLM:

'context encoding' and  
'token prediction' stages

# Plan

- Evolution of representations of individual tokens
- Training objectives: LM, MLM, MT
- "Puzzles" from previous work
- The Information-Bottleneck: our point of view
- Experiments

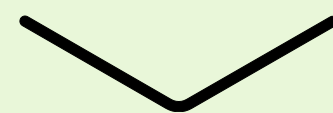
- Information Bottleneck for token representations

- ...

# Plan

- Evolution of representations of individual tokens
- Training objectives: LM, MLM, MT
- "Puzzles" from previous work
- The Information-Bottleneck: our point of view
- Experiments
  - Information Bottleneck for token representations
  - Analyzing changes and influences
  - ...

# Analyzing Changes and Influences



# Analyzing Changes and Influences

- how much change is happening in a given layer
- which tokens gain more information from other tokens
- which tokens influence other tokens most



# Analyzing Changes and Influences

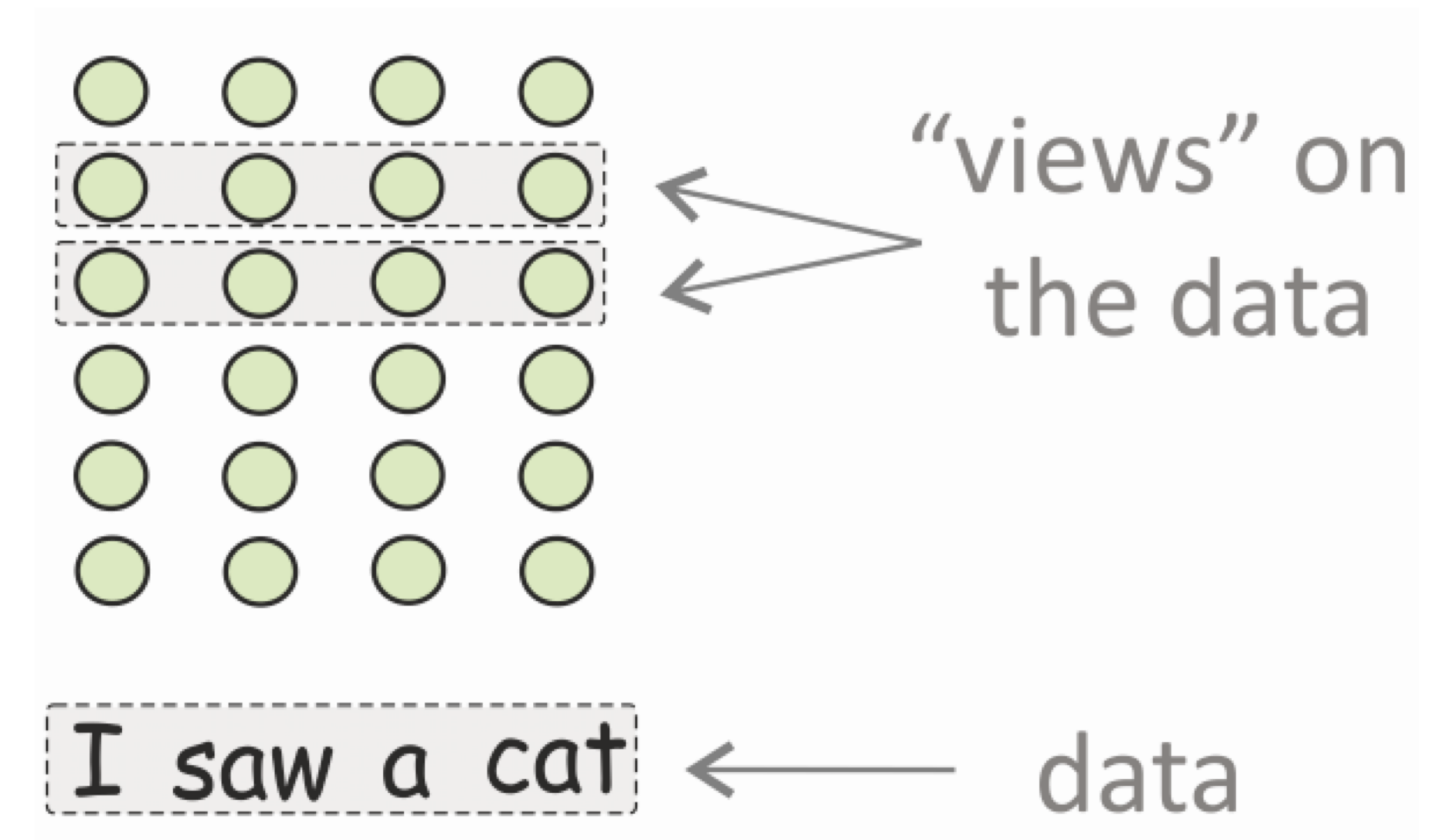
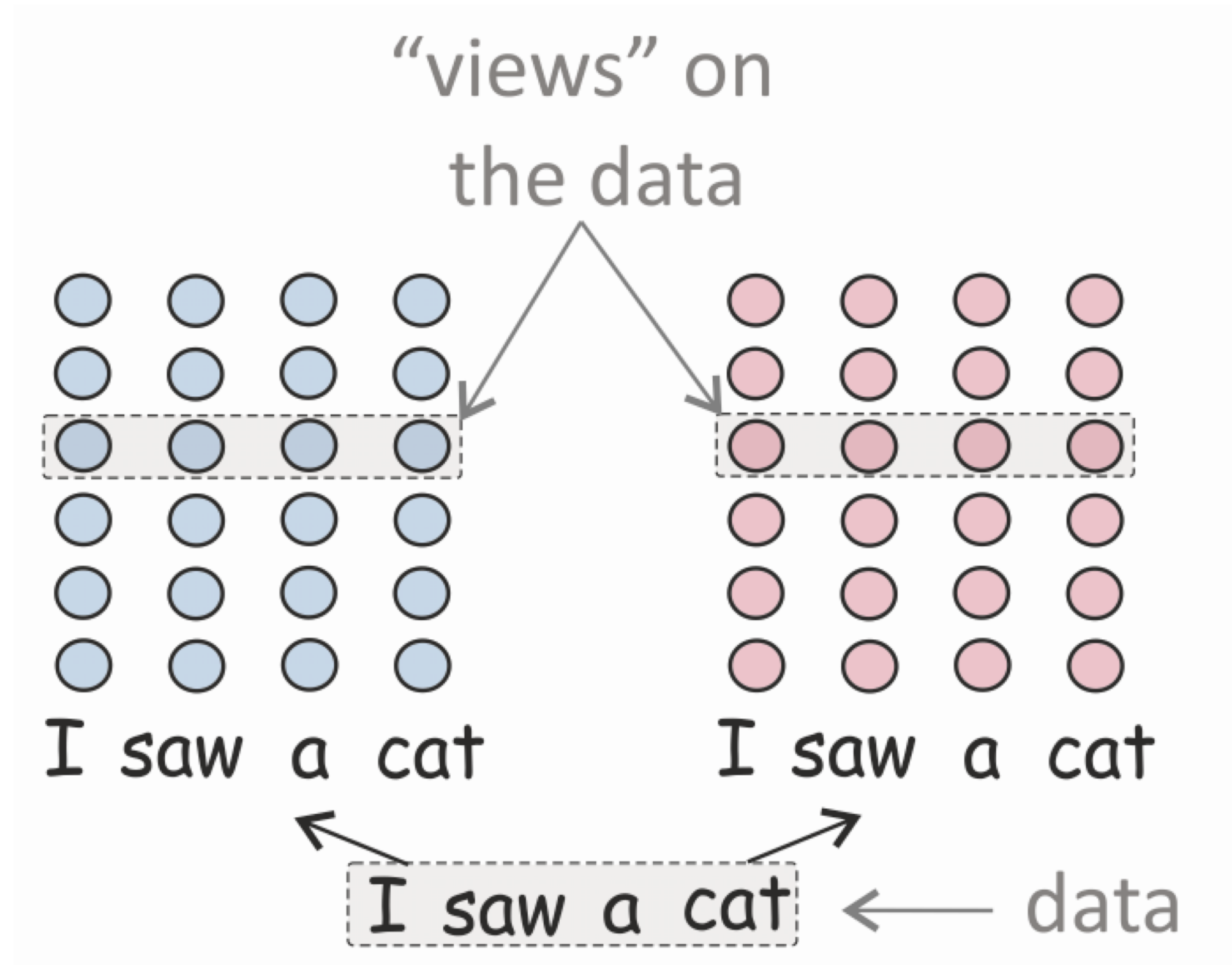
- how much change is happening in a given layer
- which tokens gain more information from other tokens
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Comparison  
between network  
representations

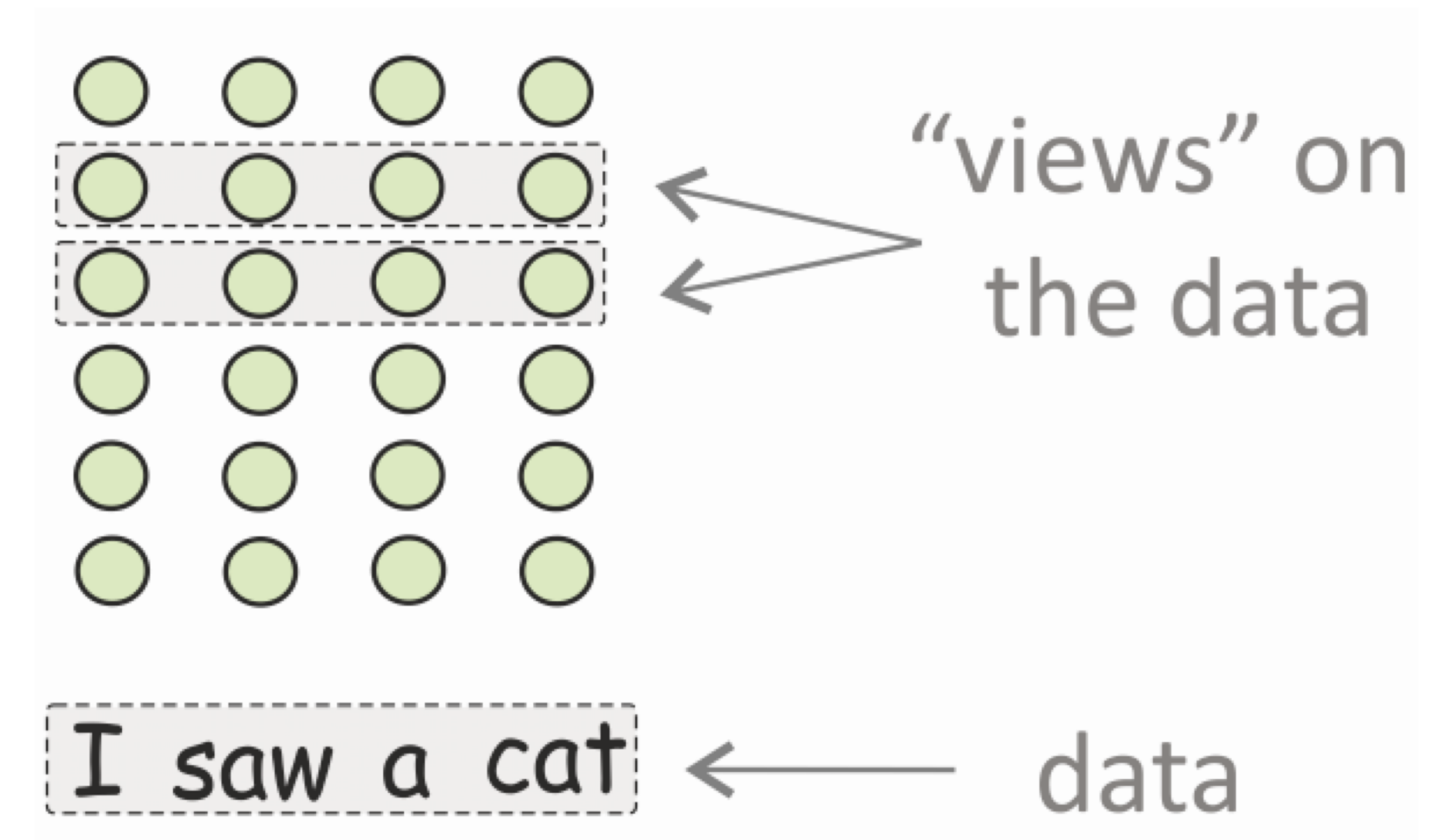
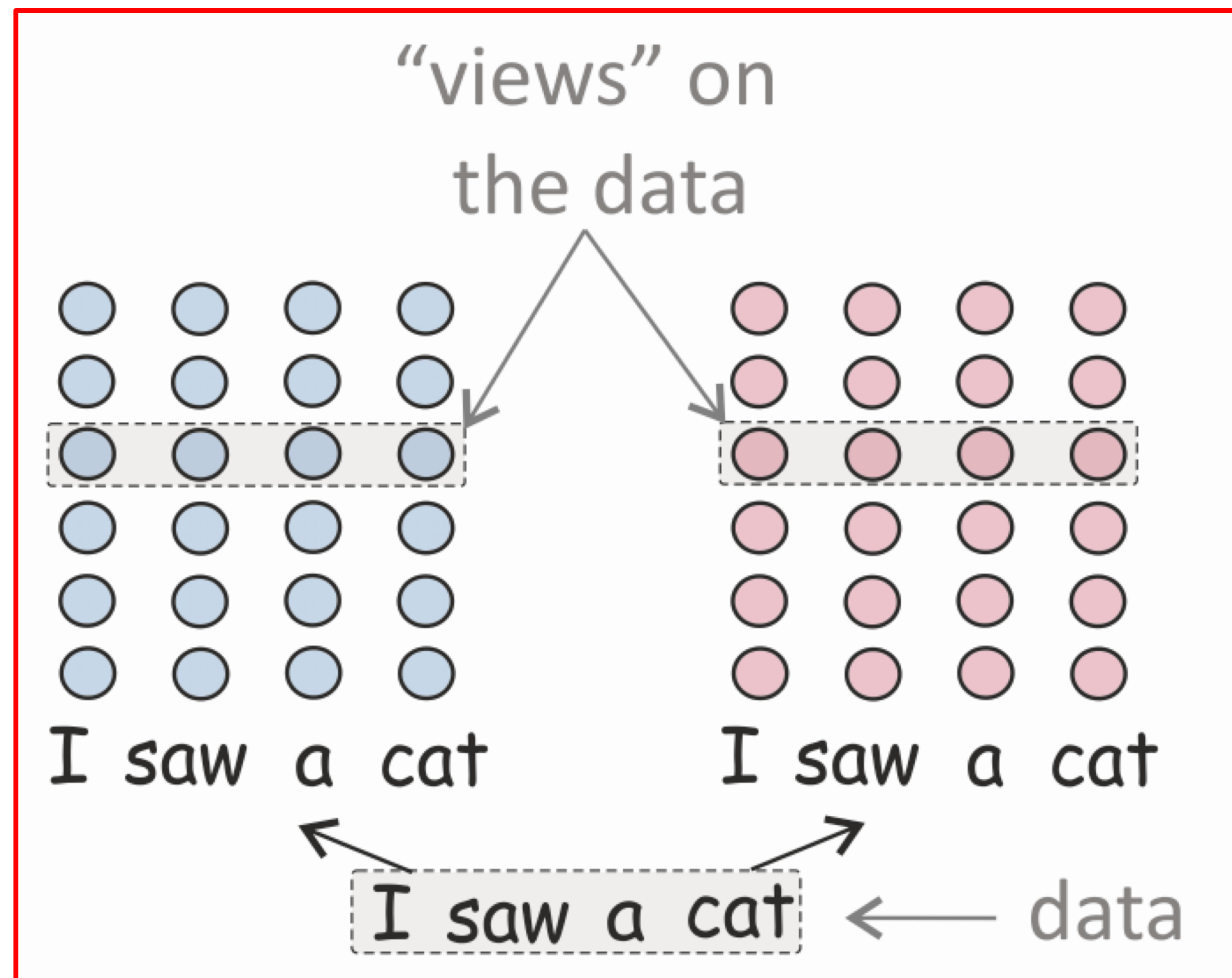
# Views on the data

- use PWCCA – a version of canonical correlation analysis (CCA)
- PWCCA measures similarity between pairs of ‘views’ on the data



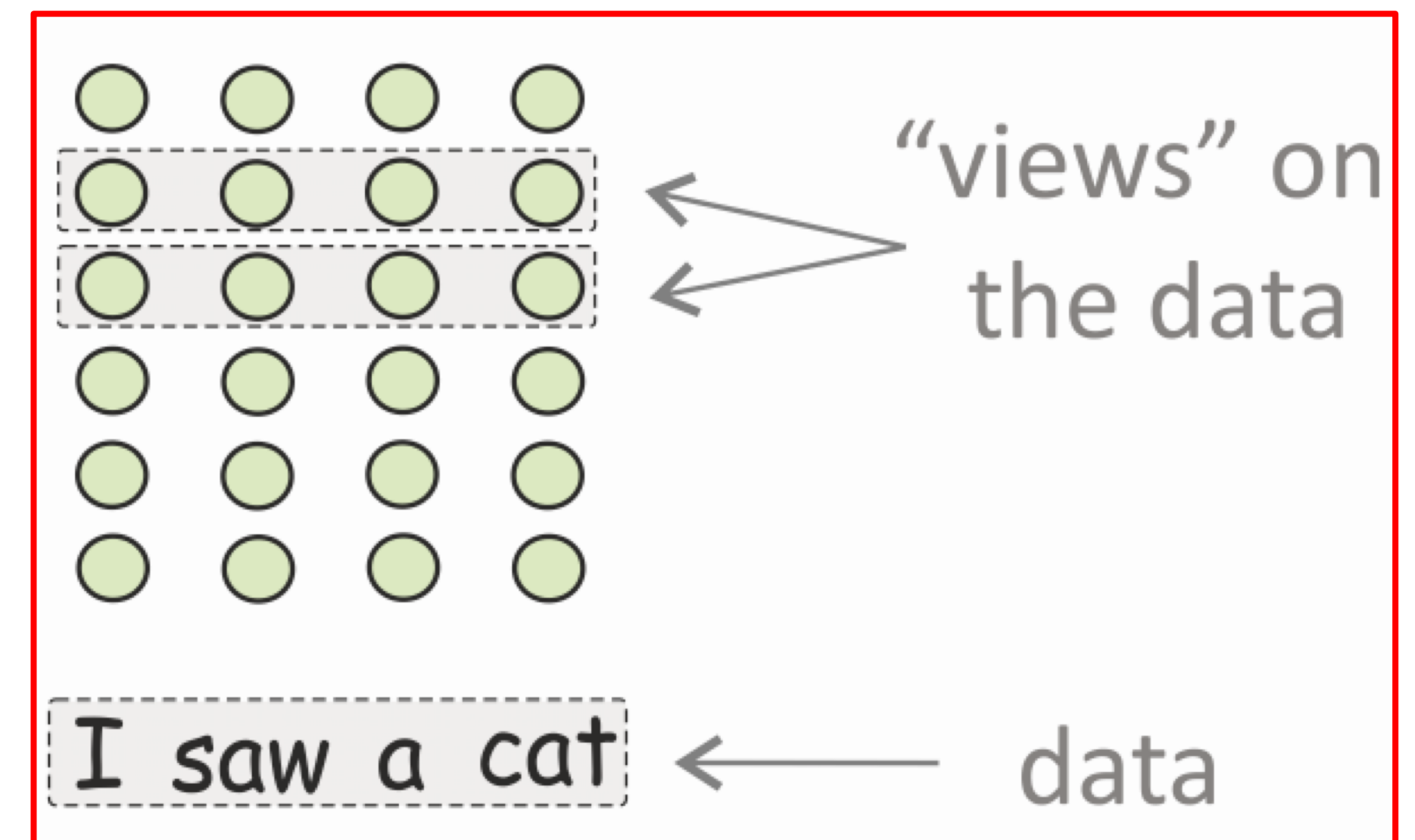
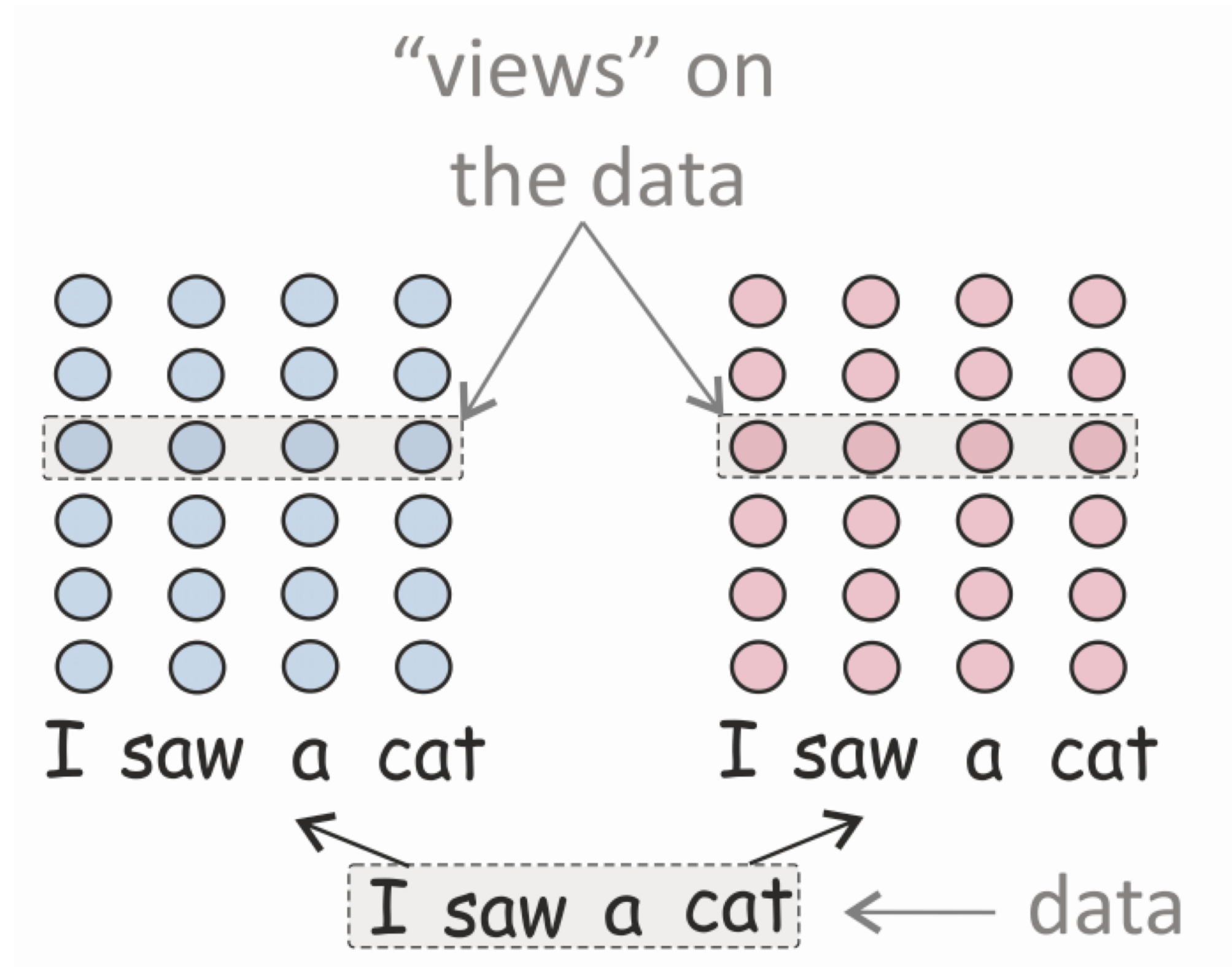
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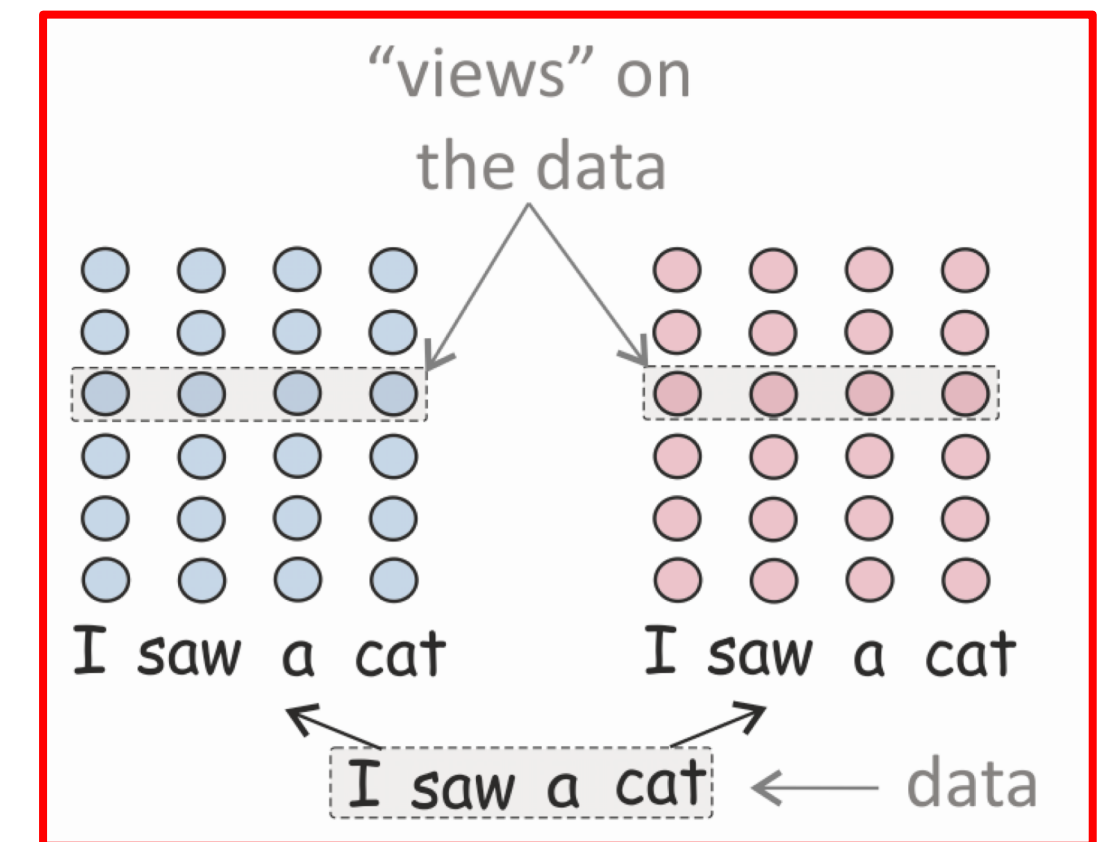
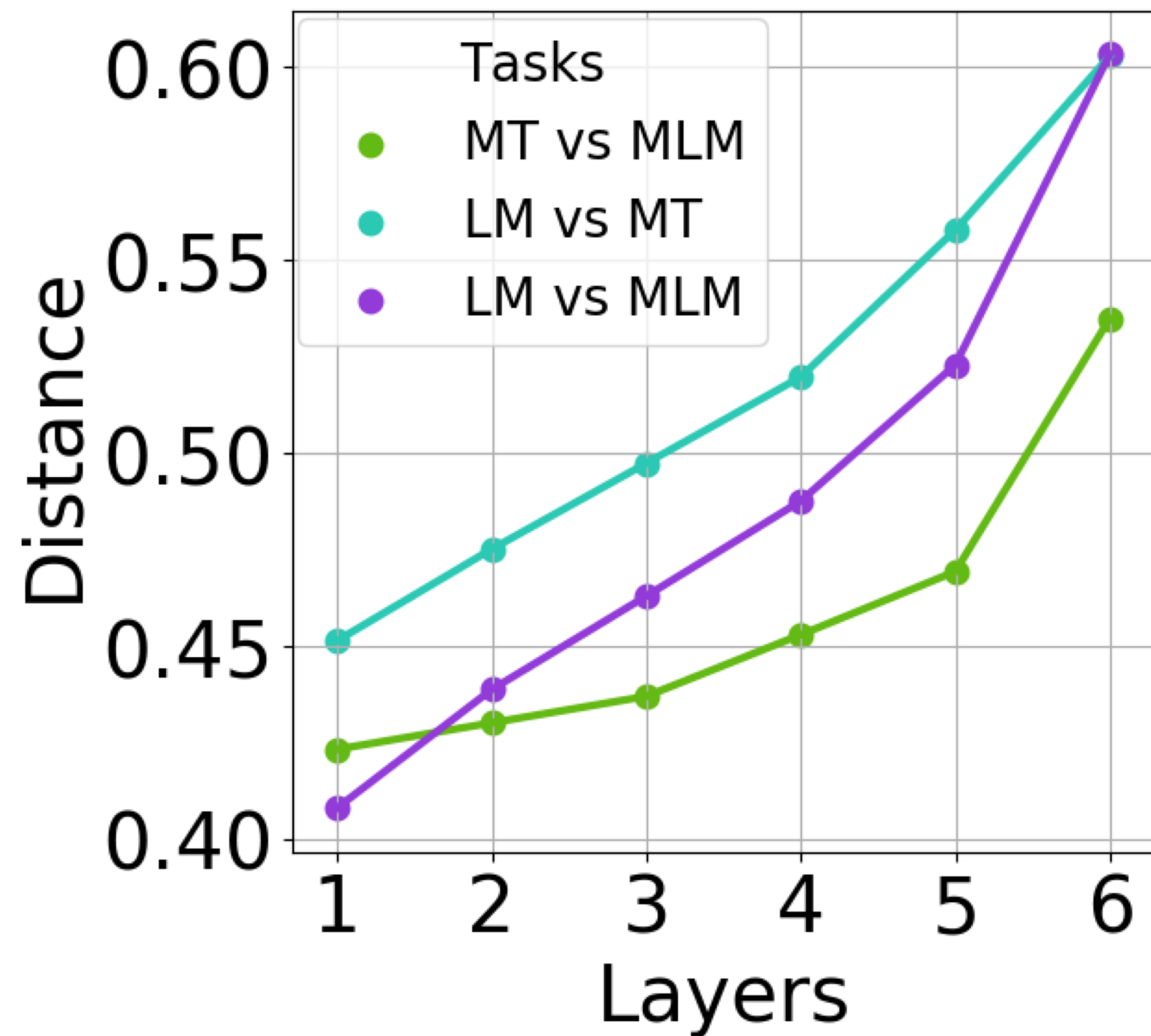


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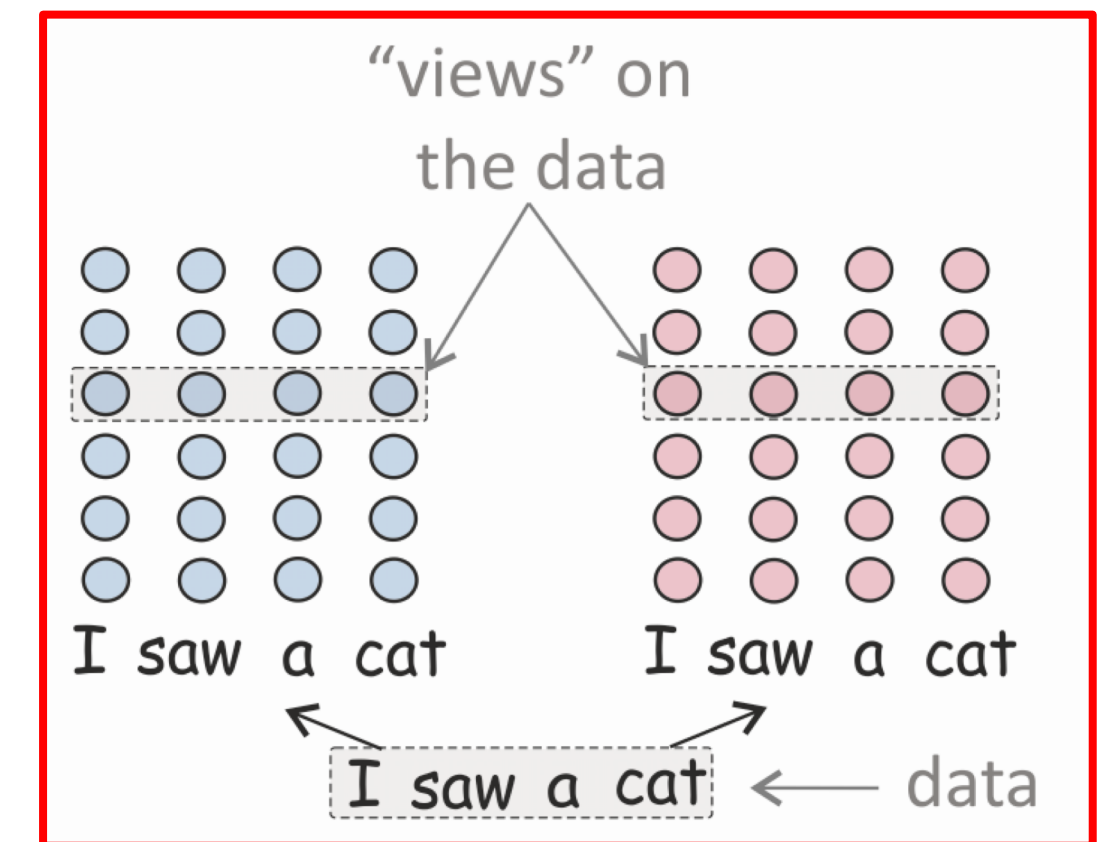
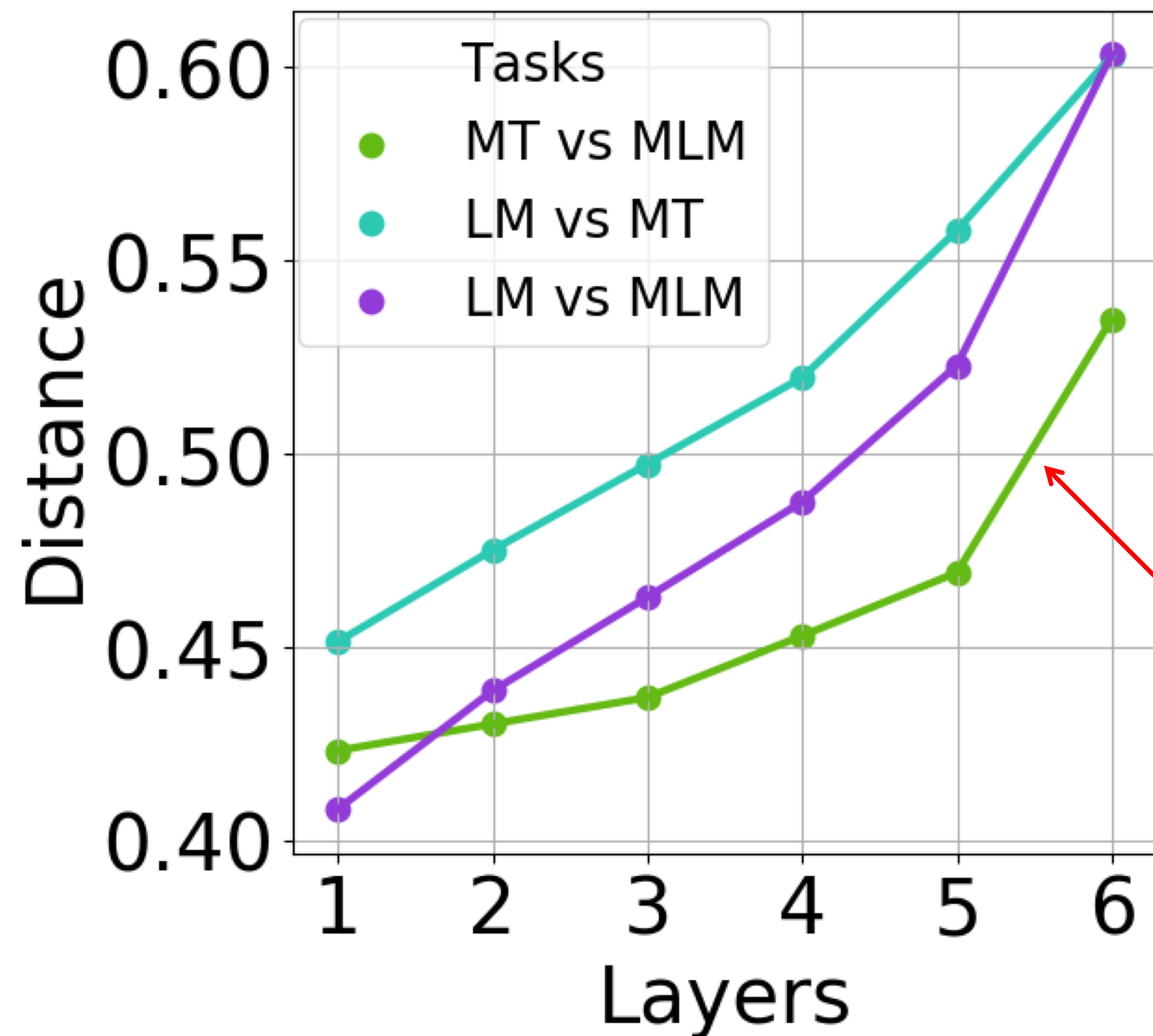
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# A coarse-grained view: Distance between tasks

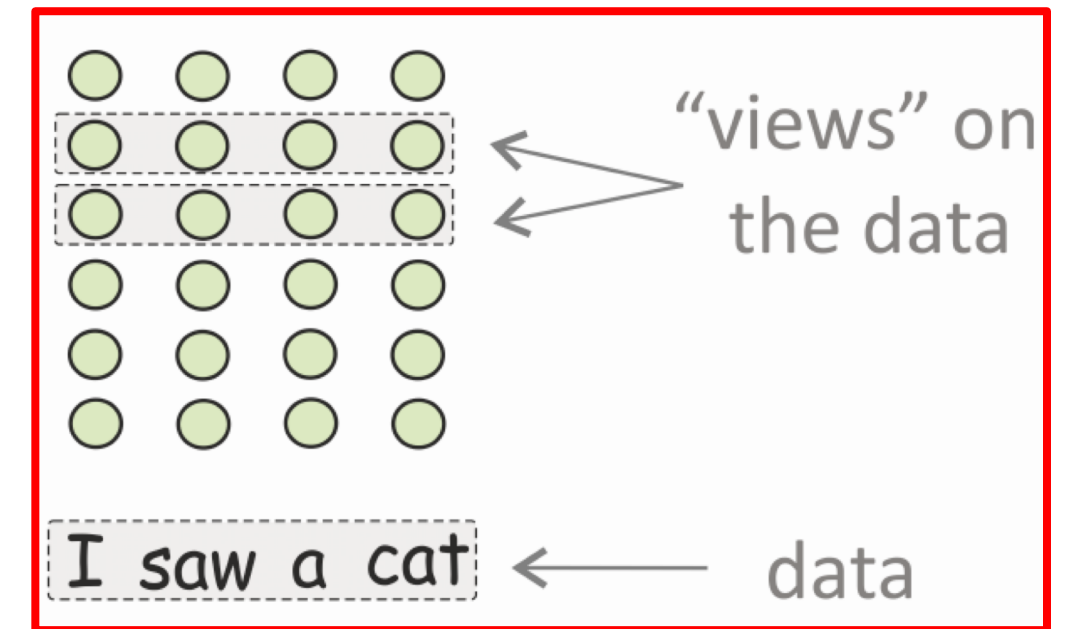
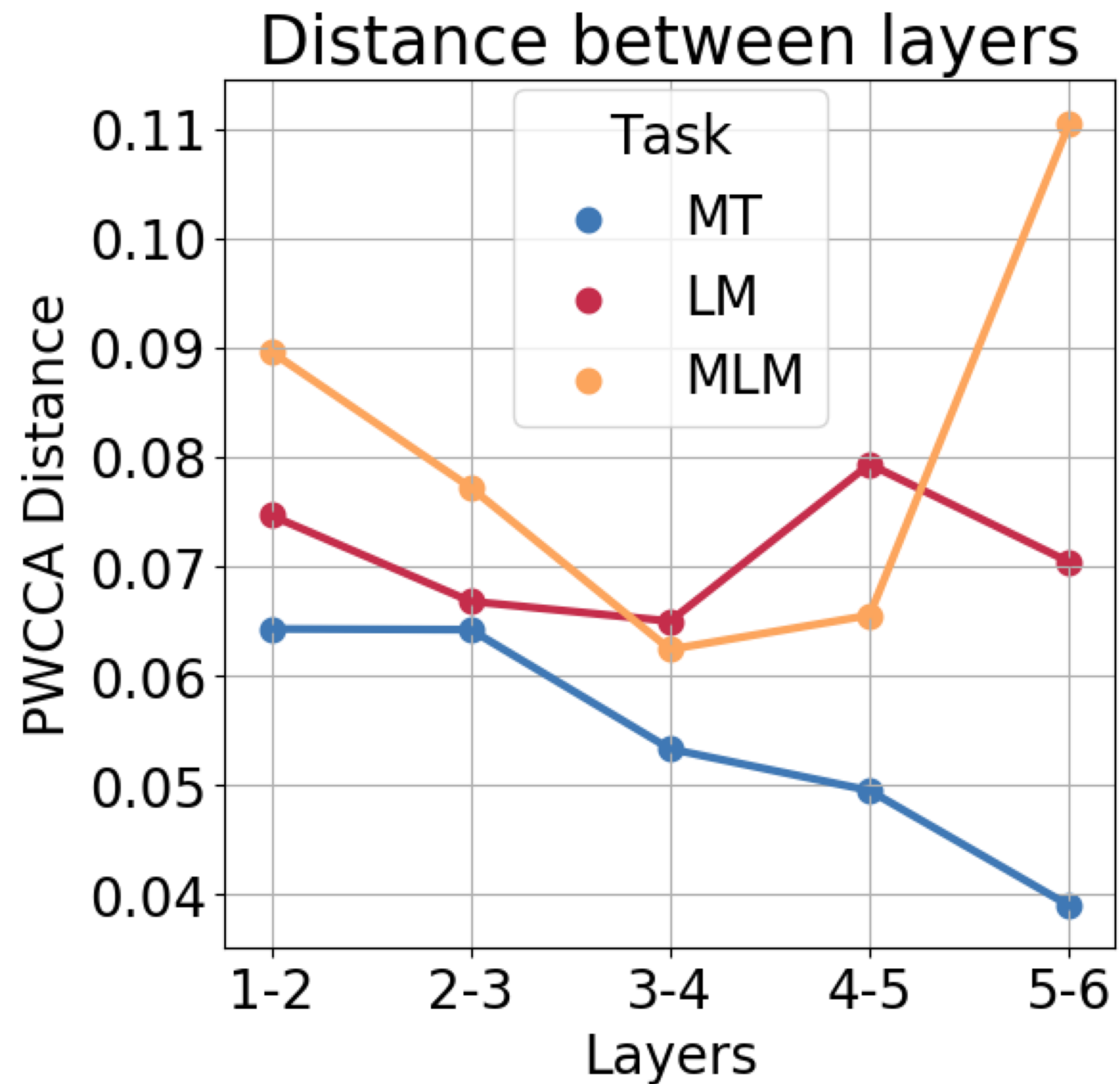


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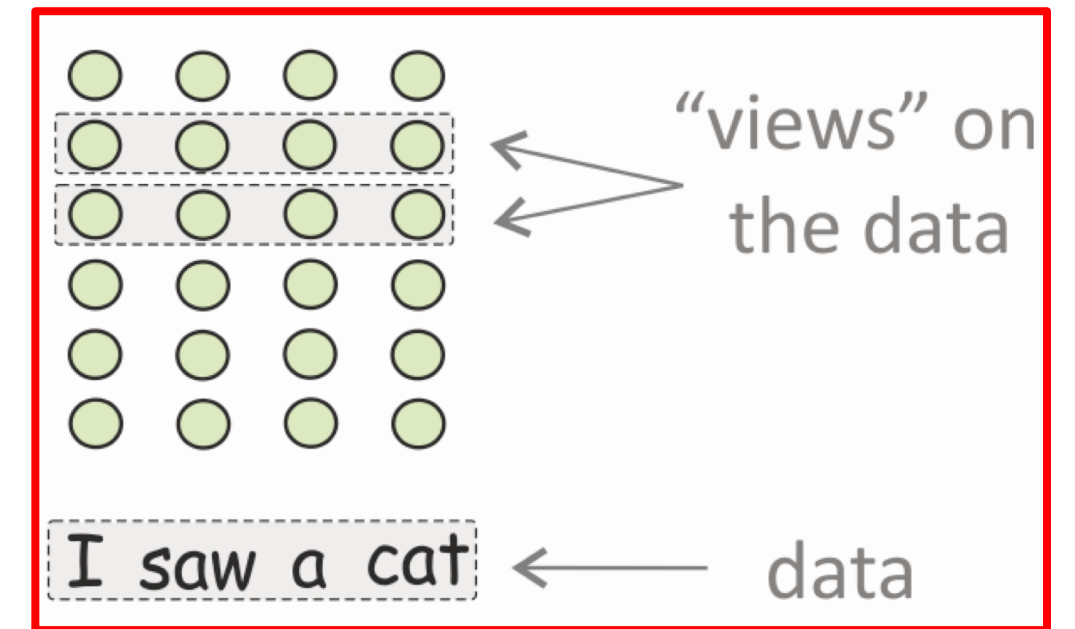
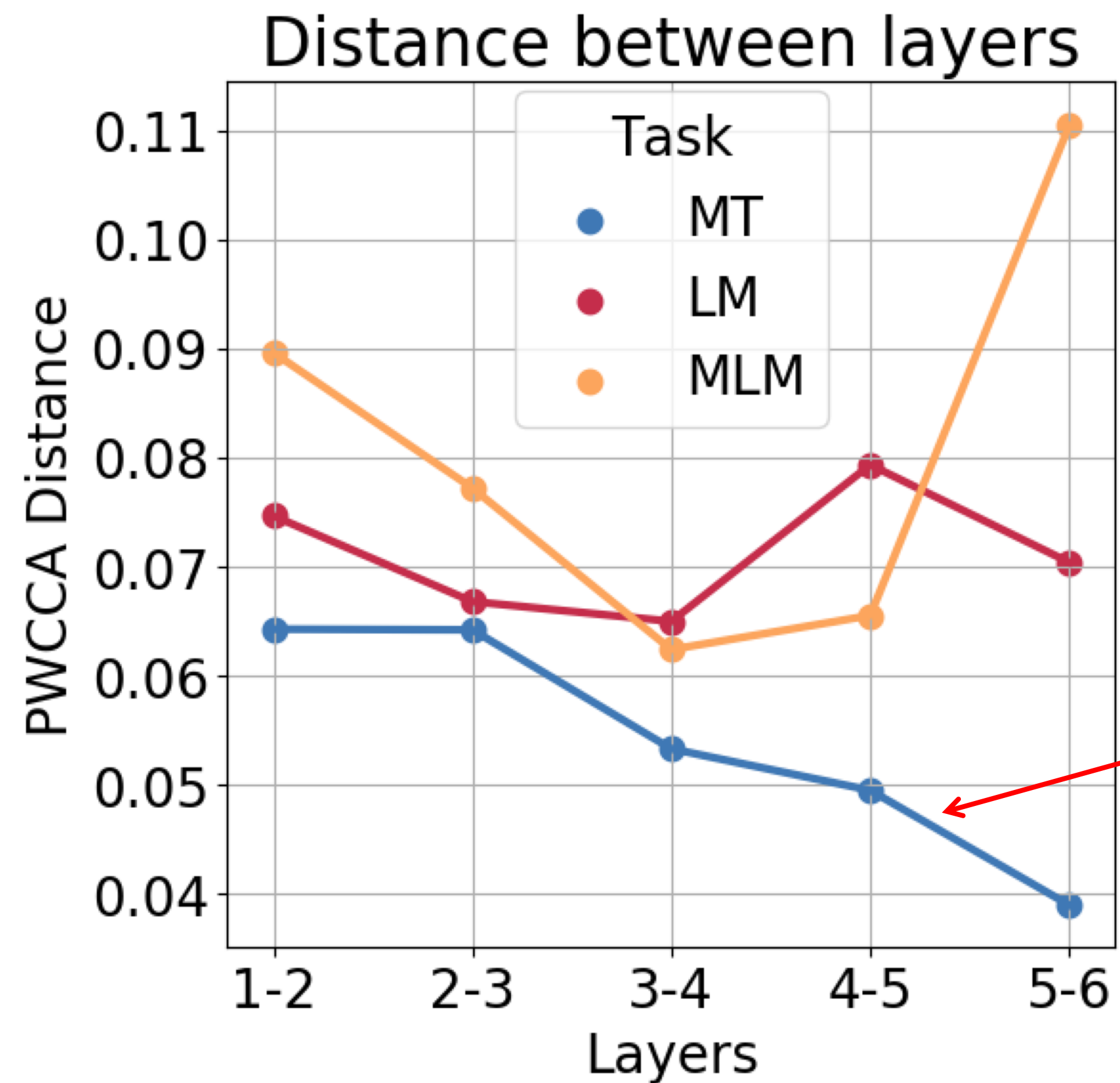


MT and MLM are closer to each other, than they are to LM

# A coarse-grained view: Changes between layers



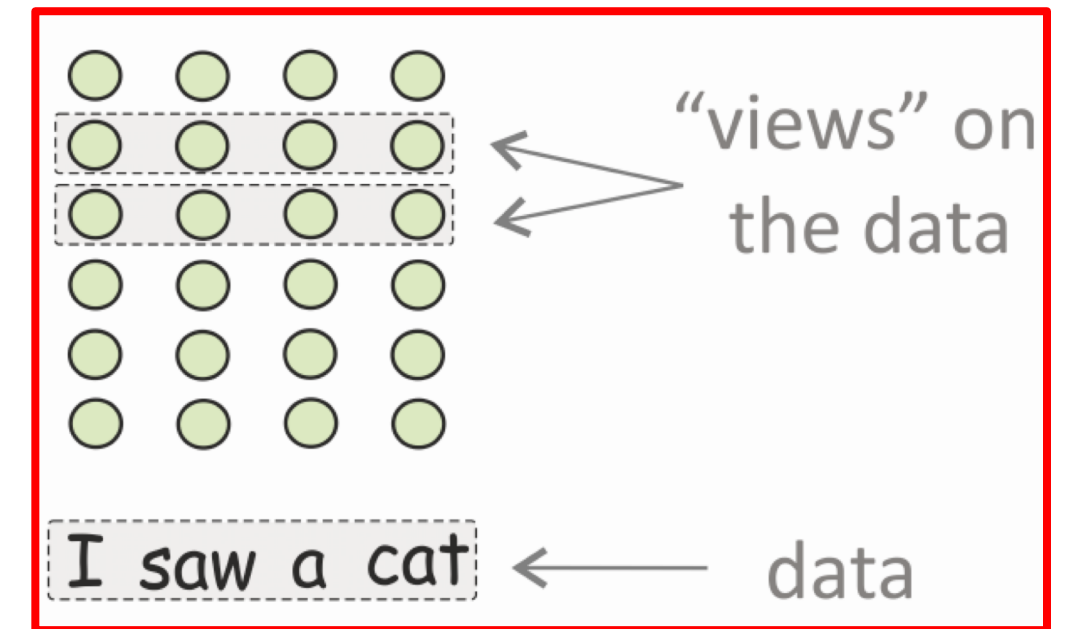
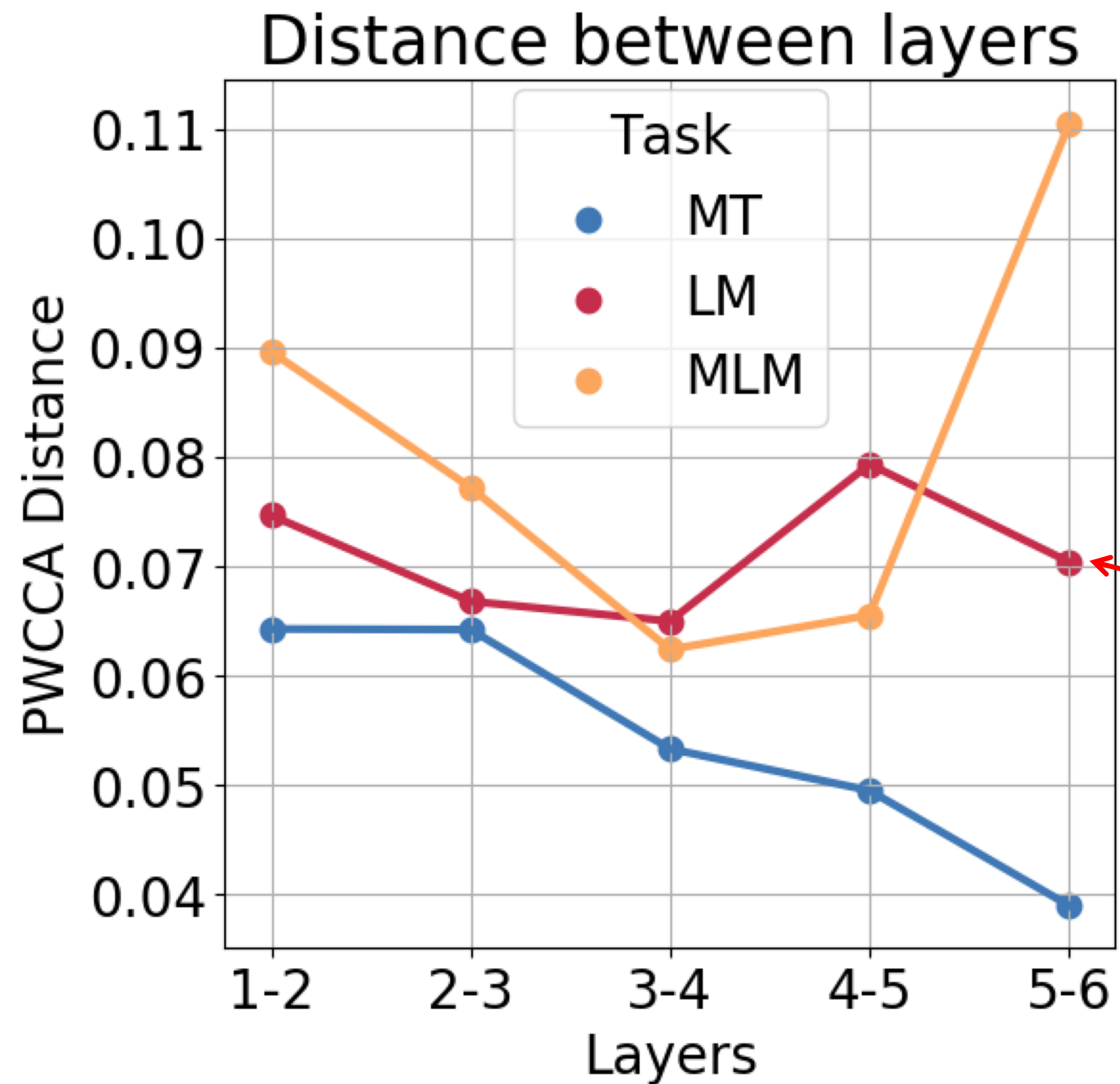
# A coarse-grained view: Changes between layers



decreasing change for MT

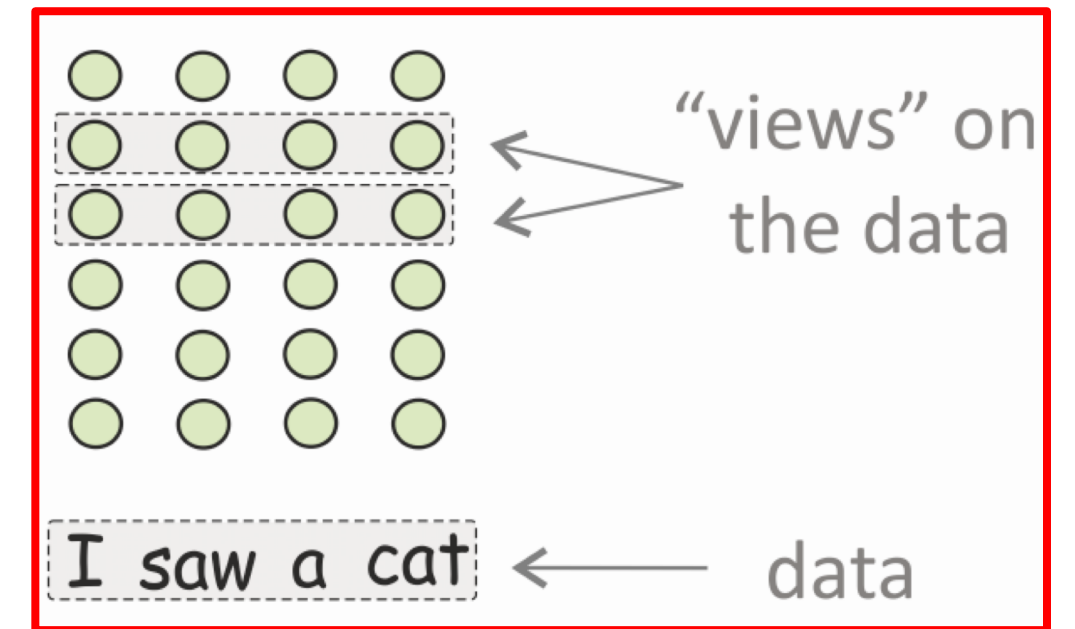
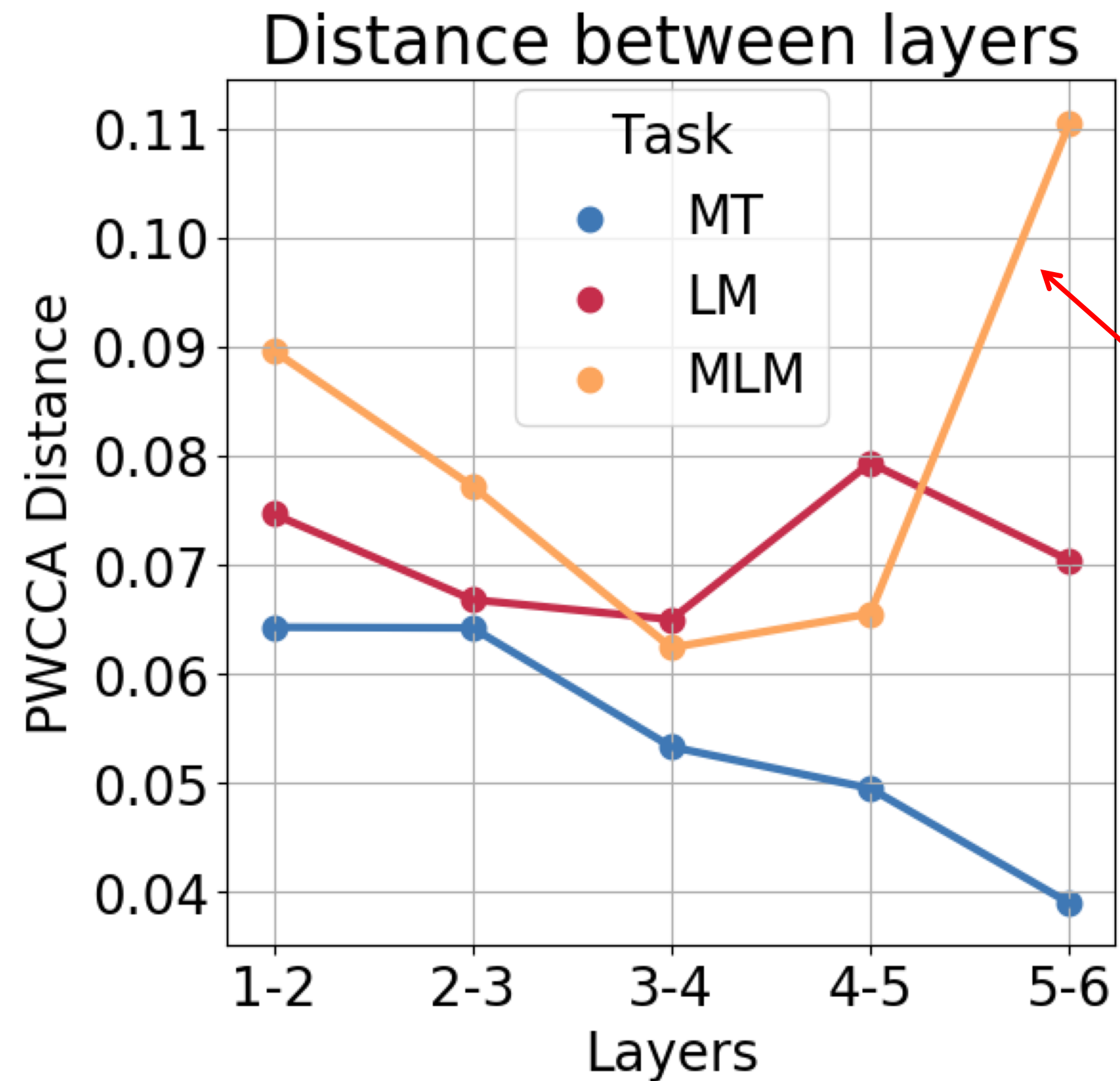


# A coarse-grained view: Changes between layers



a lot of change for LM

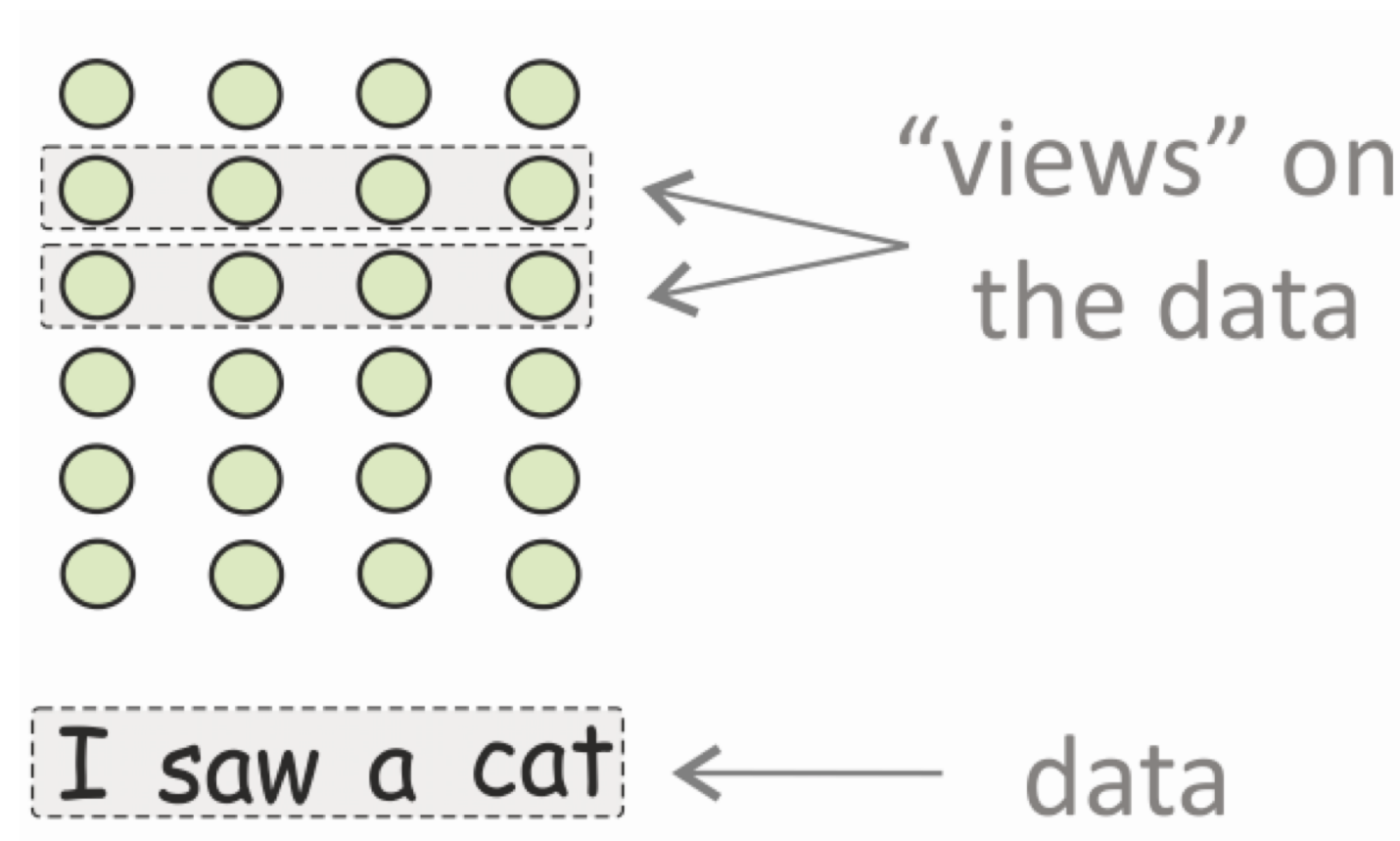
# A coarse-grained view: Changes between layers



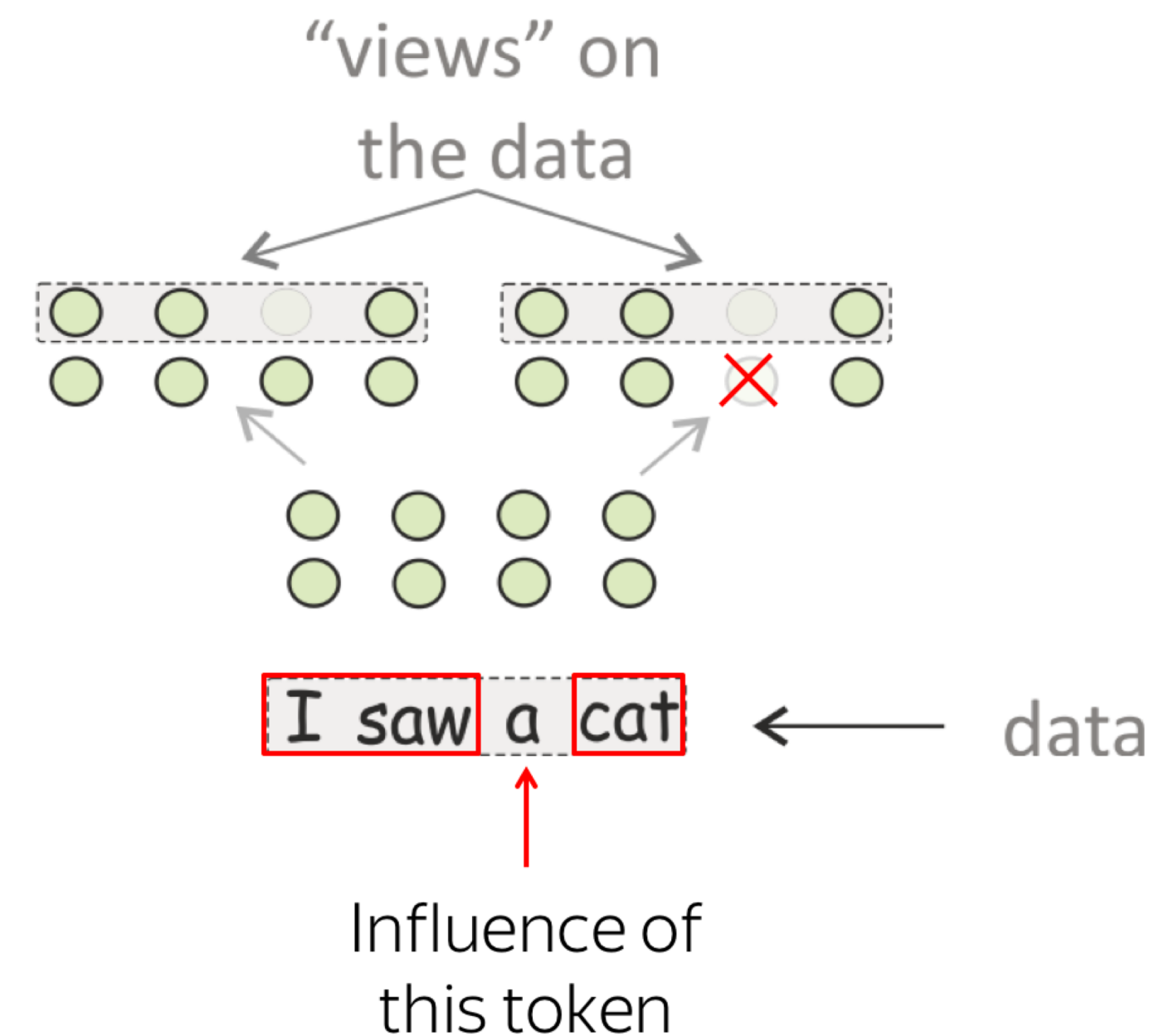
The two stages for MLM:  
'context encoding' and  
'token reconstruction'

# Amount of change and influence

- **Change:** how much representations of these tokens change between layers

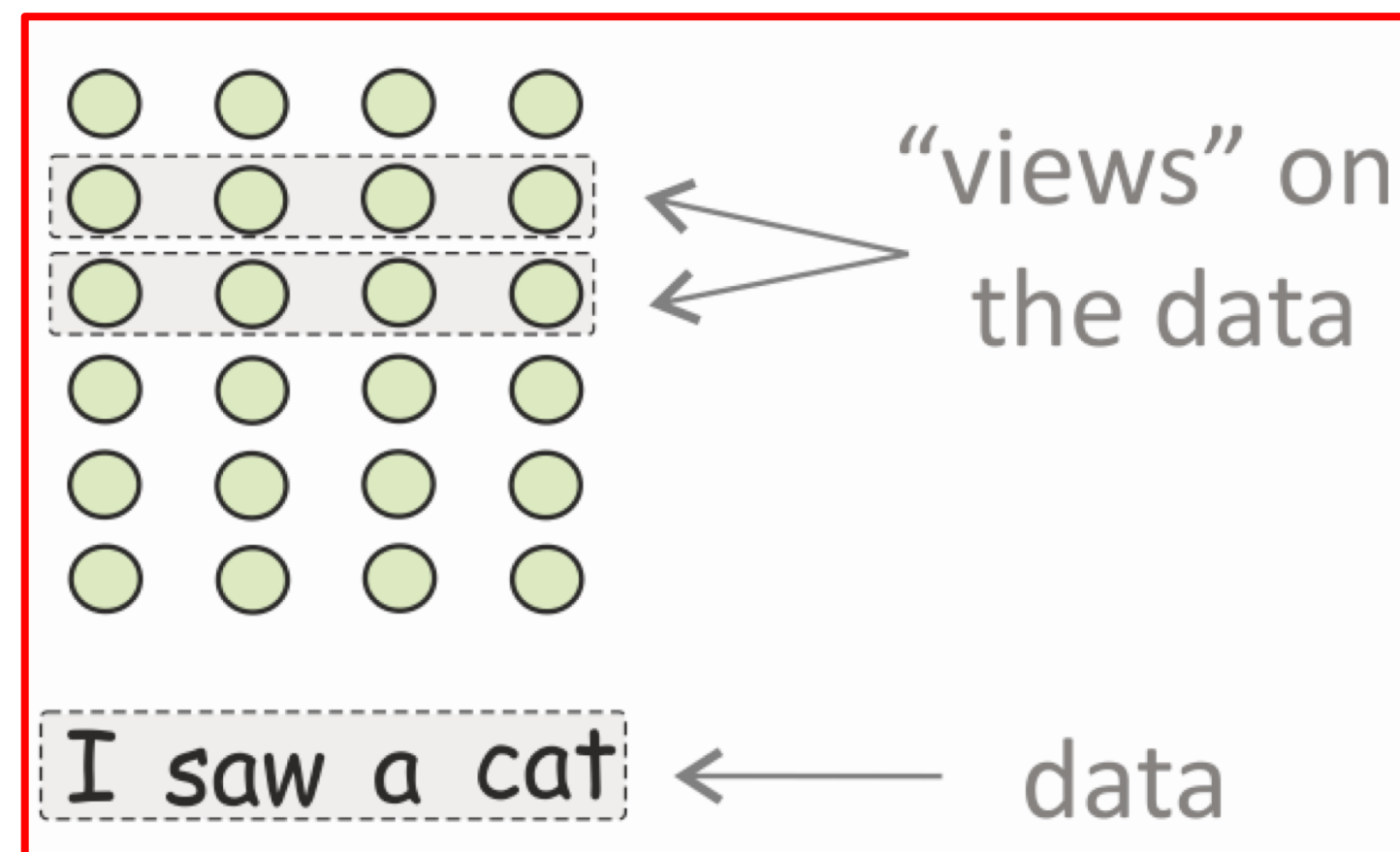


- **Influence:** how much representations of other tokens change if this token is not present

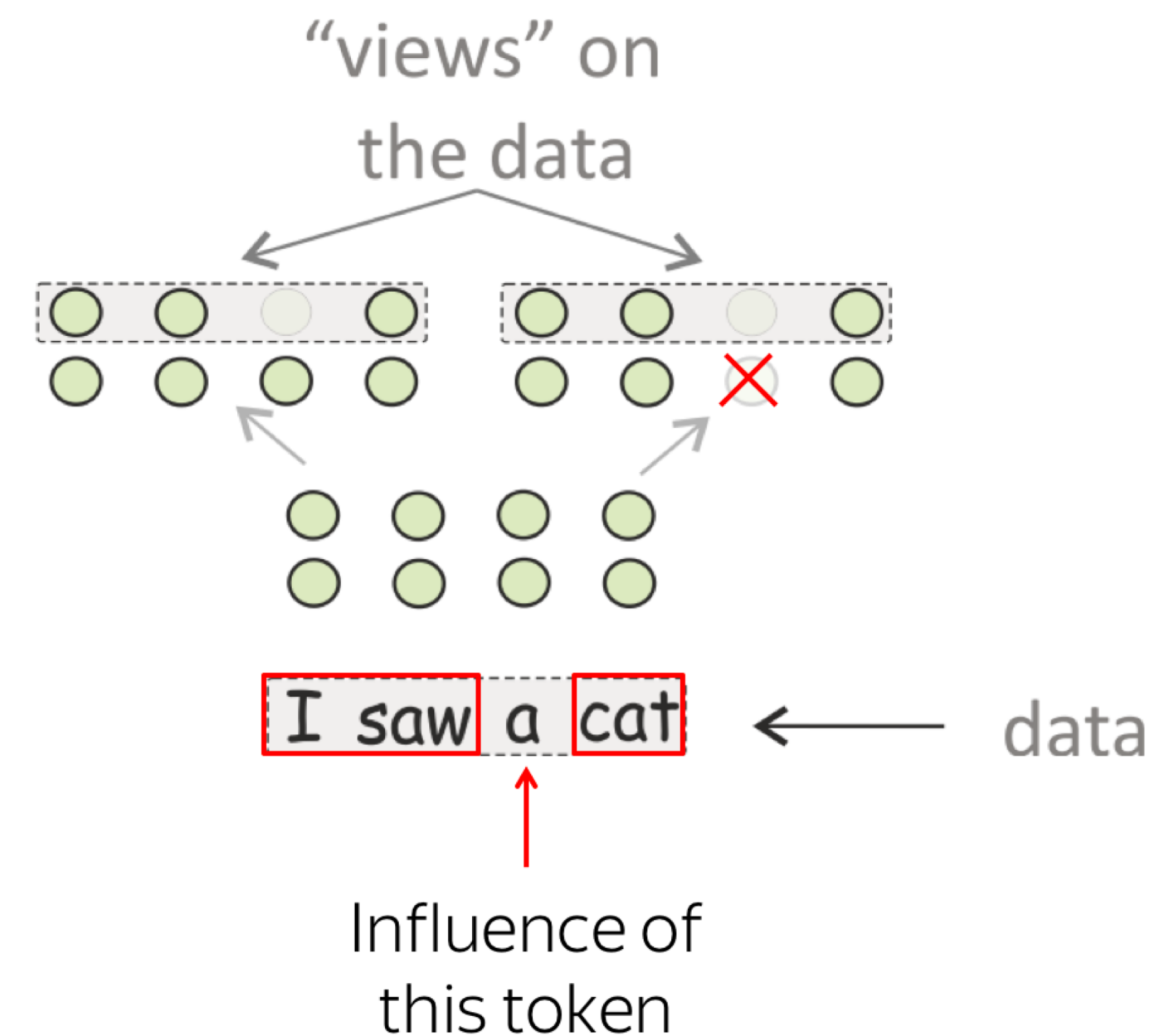


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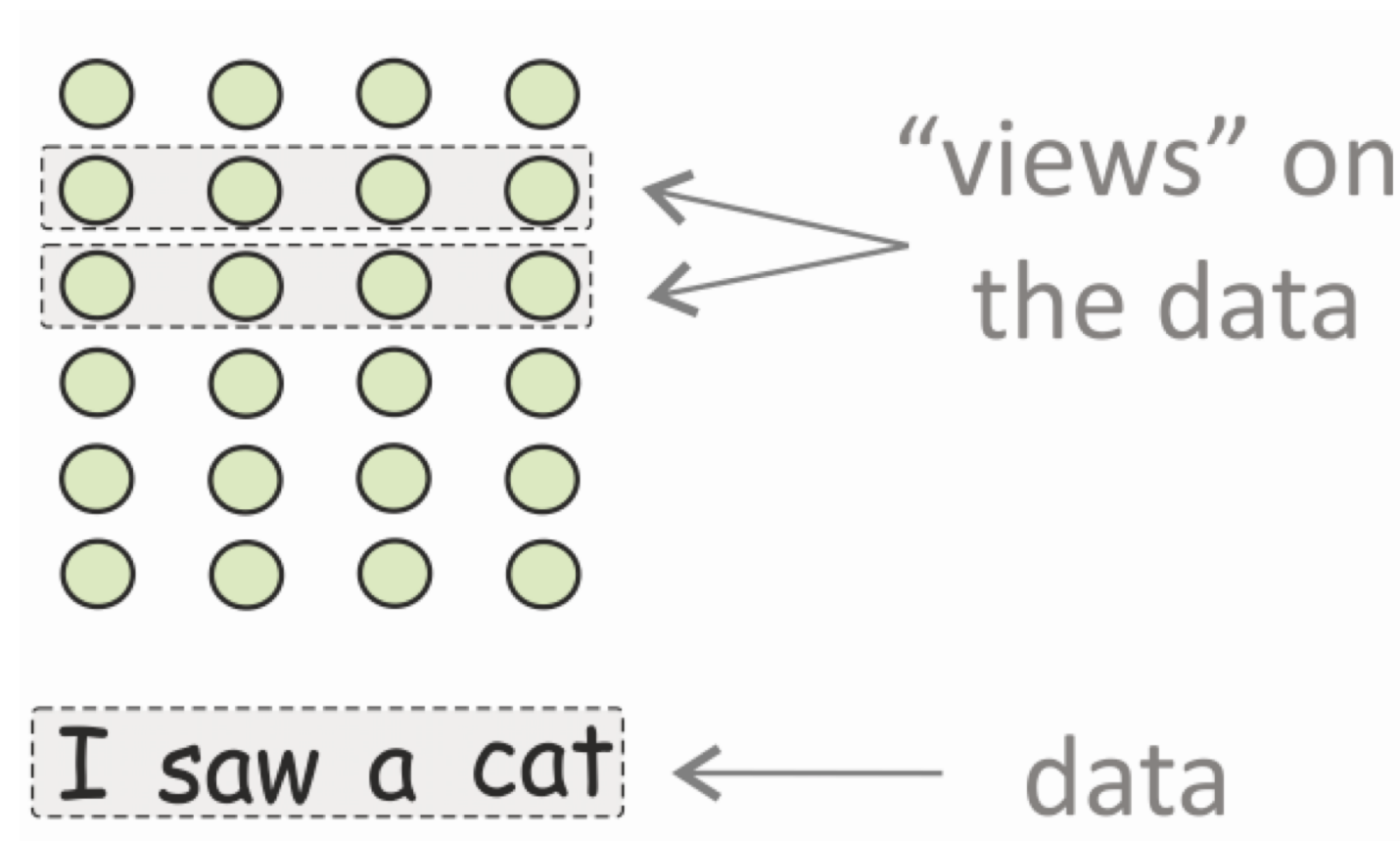


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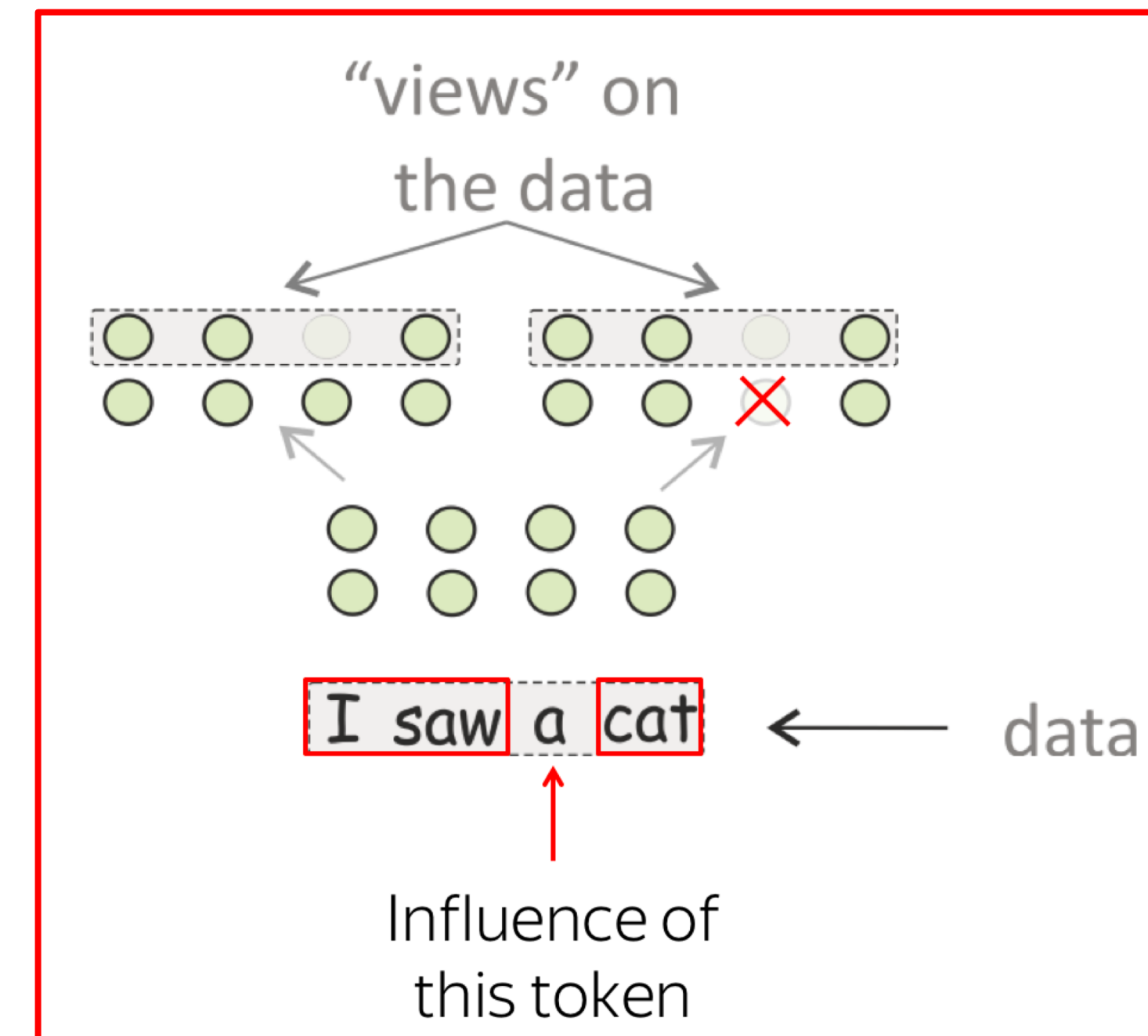


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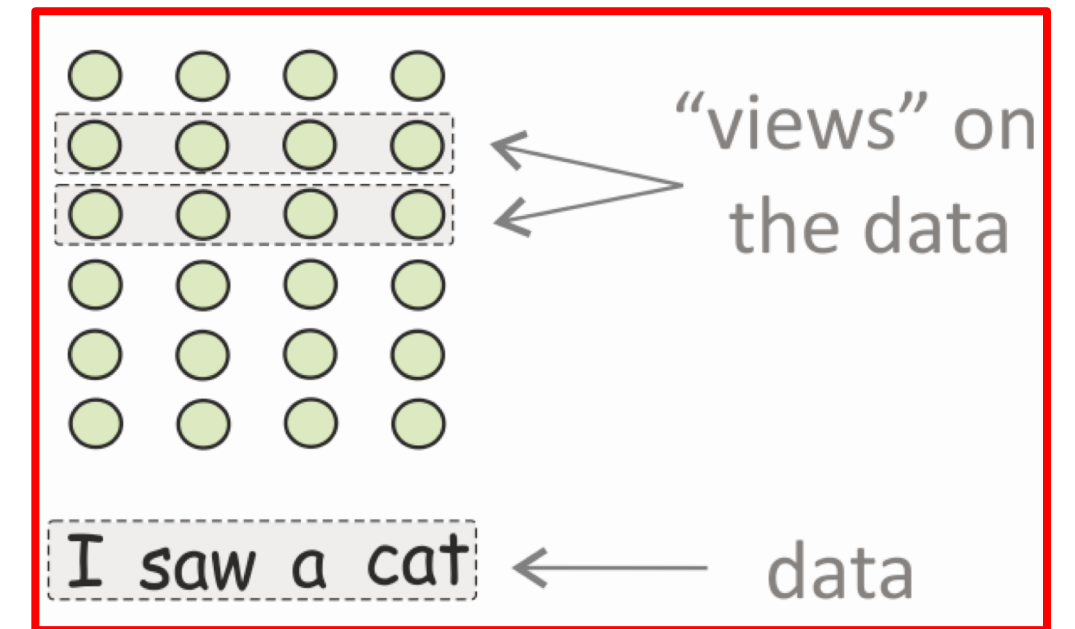


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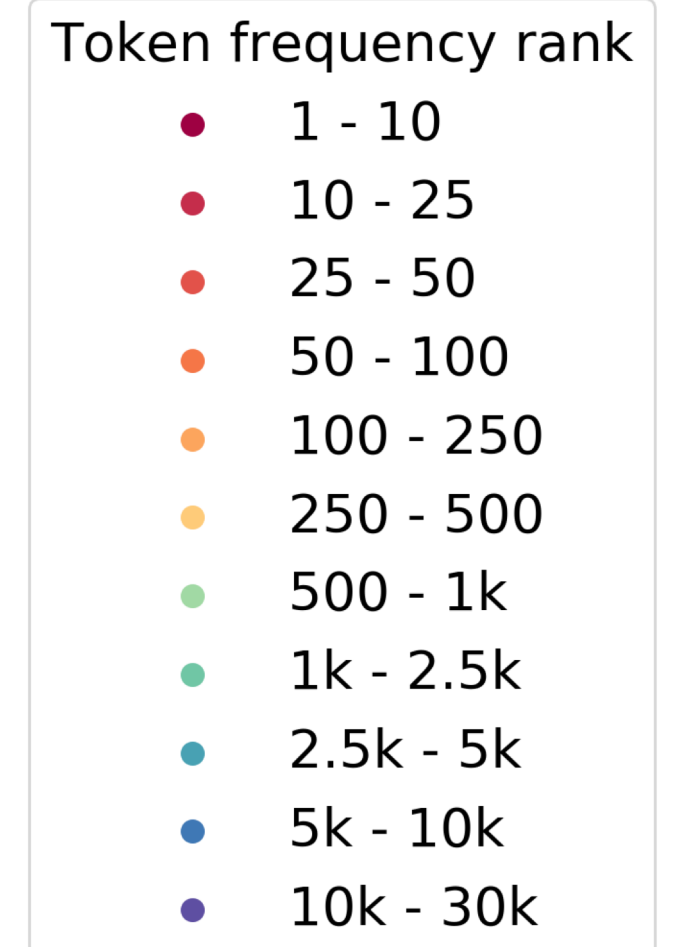
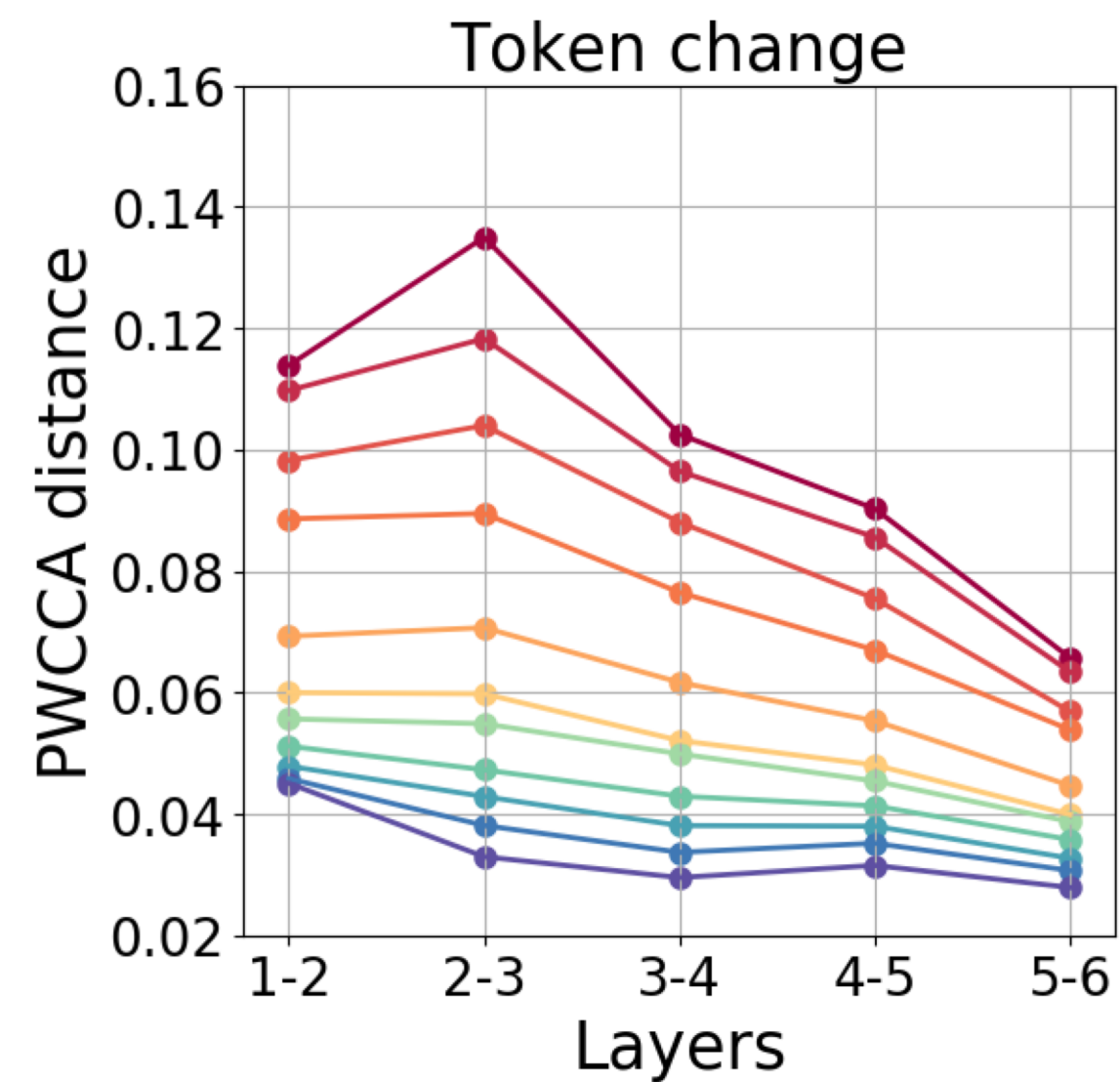


# Varying token frequency: Amount of change

- **Change:** how much representations of these tokens change between layers



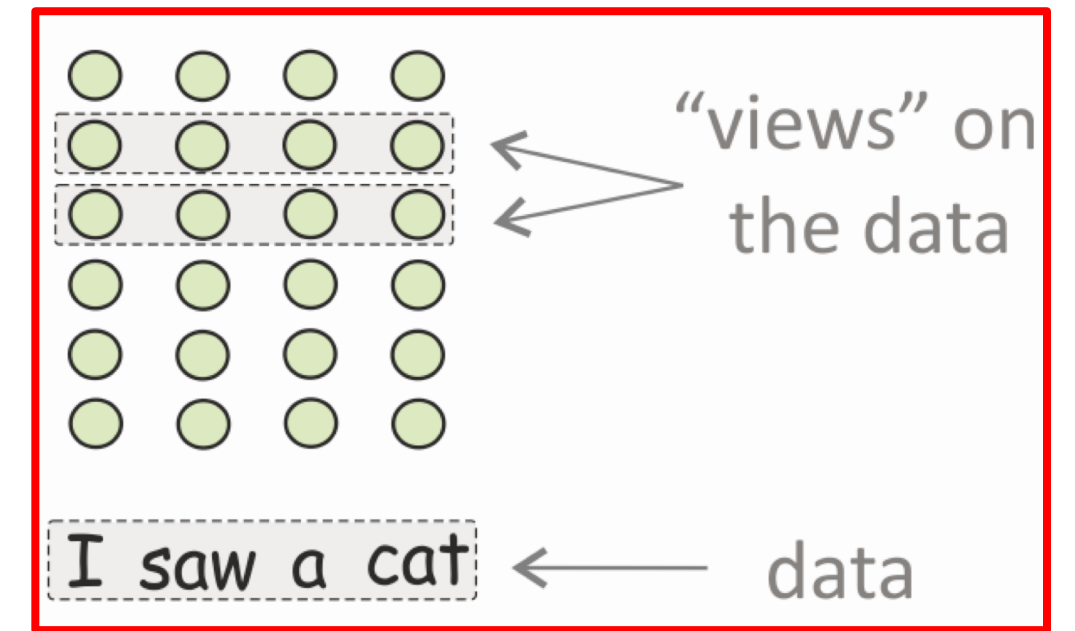
MT



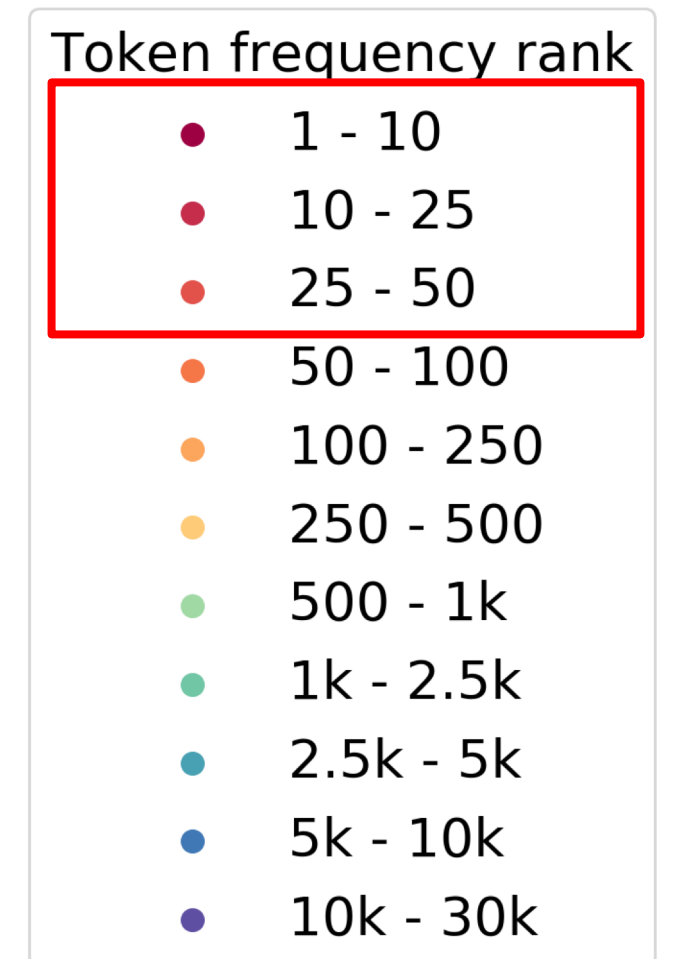
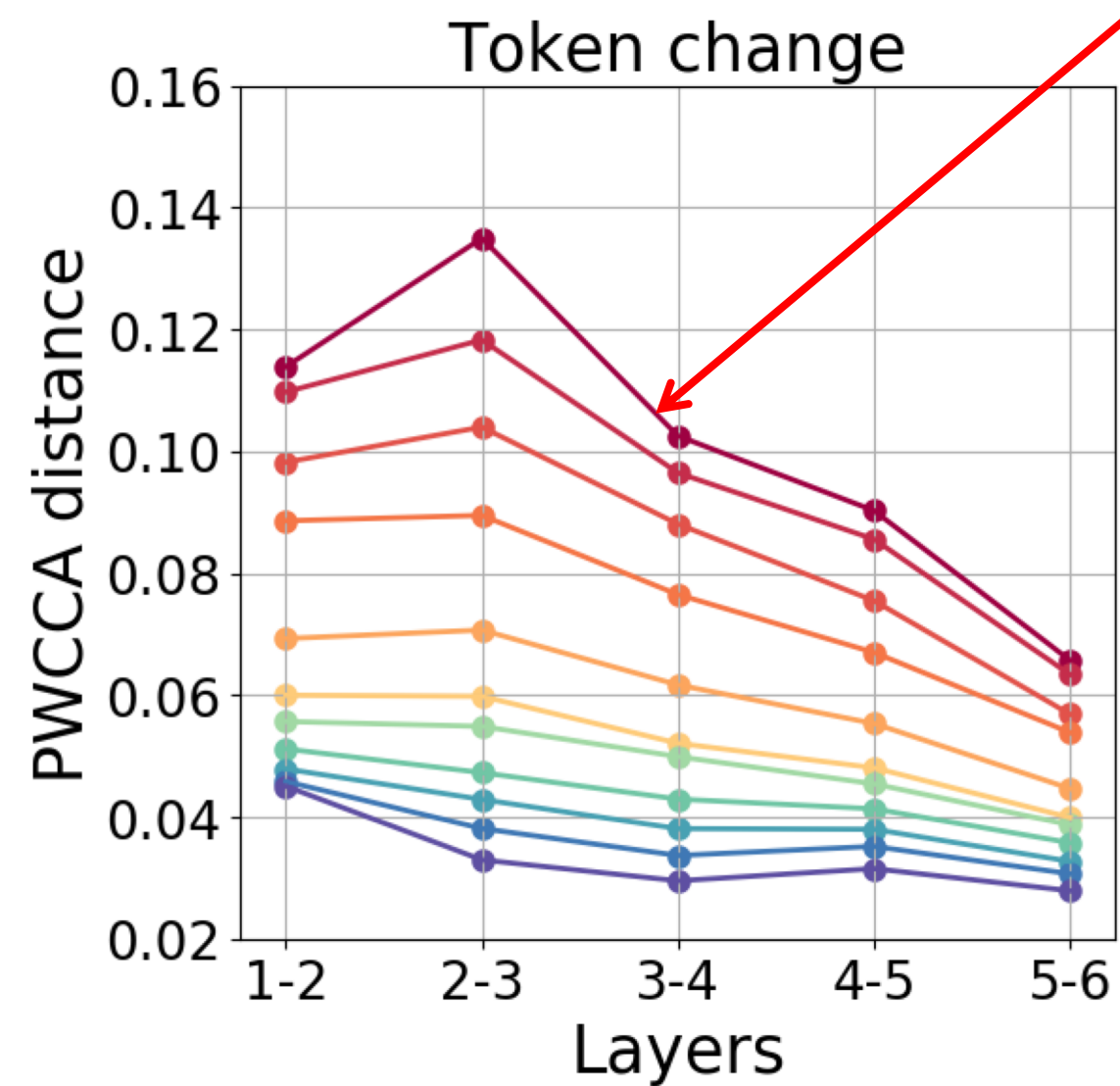
# Varying token frequency: Amount of change

- **Change:** how much representations of these tokens change between layers

Frequent tokens change more than rare

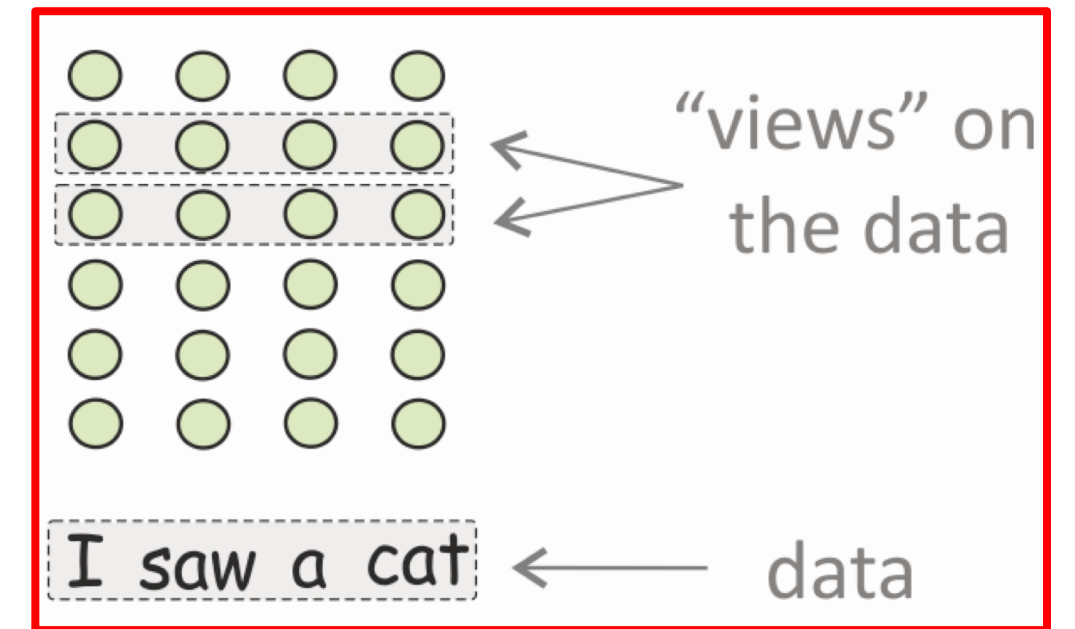


MT



# Varying token frequency: Amount of change

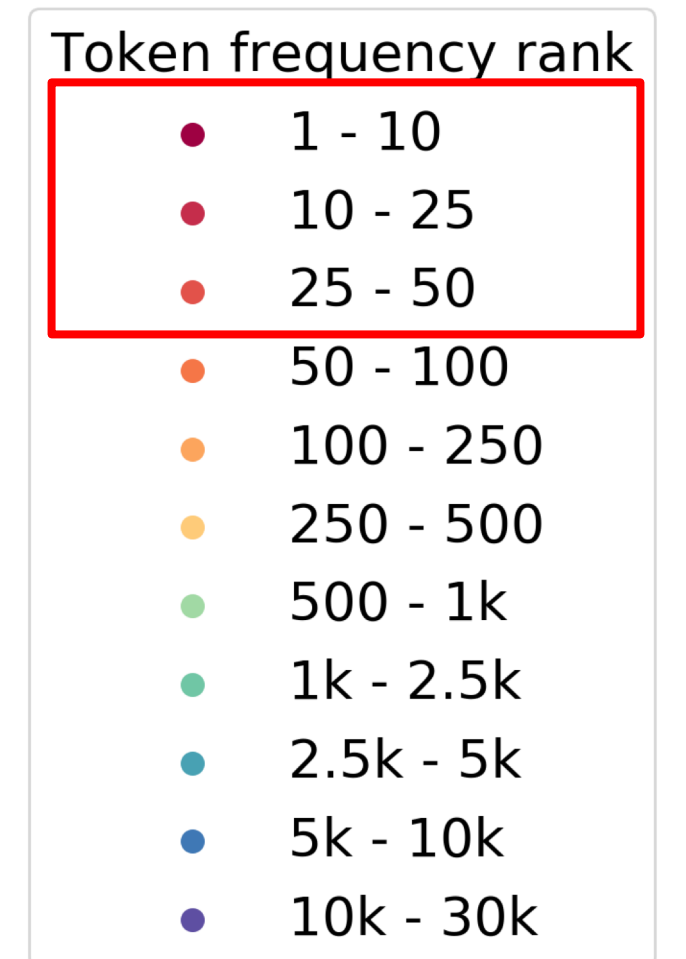
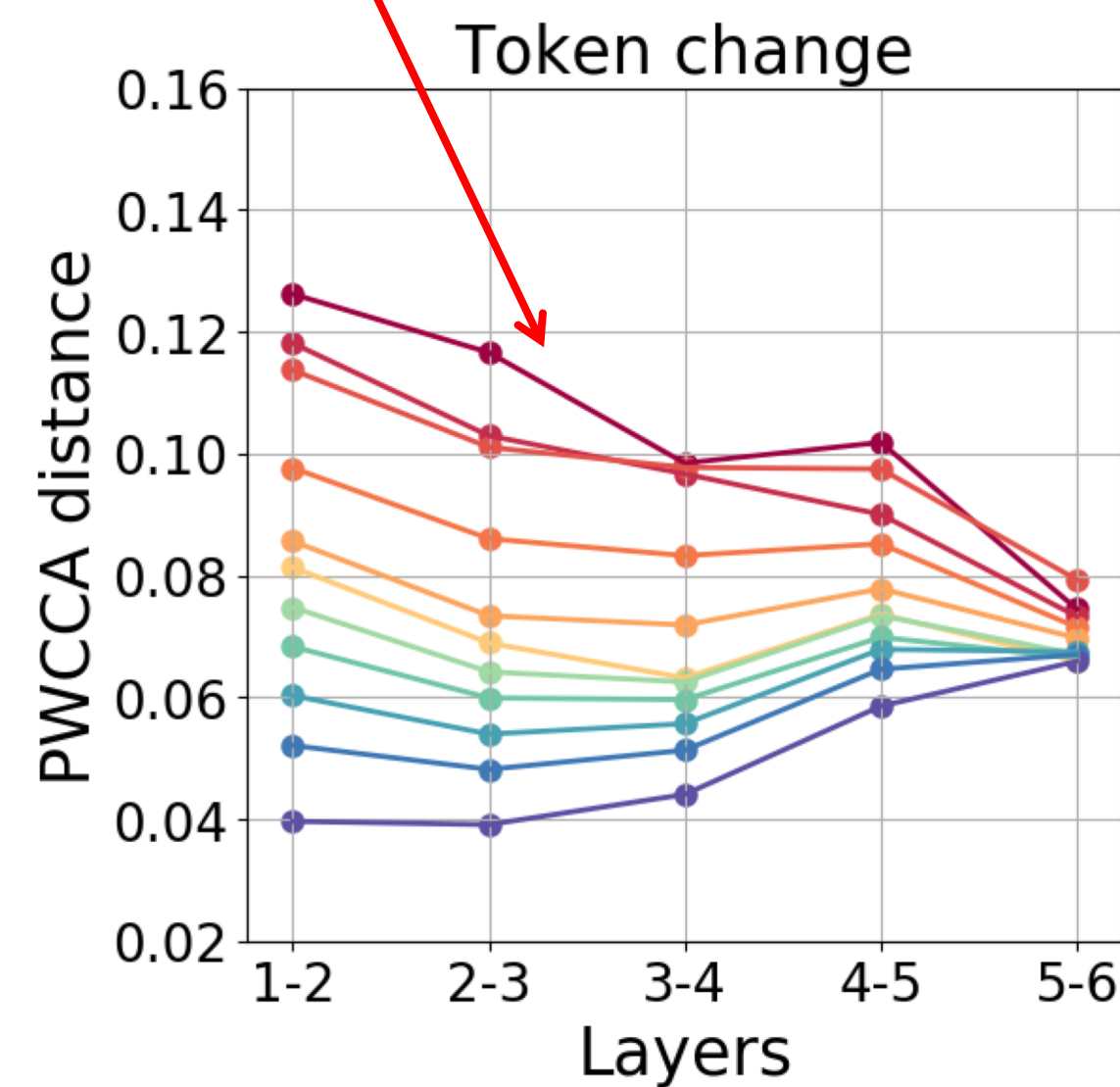
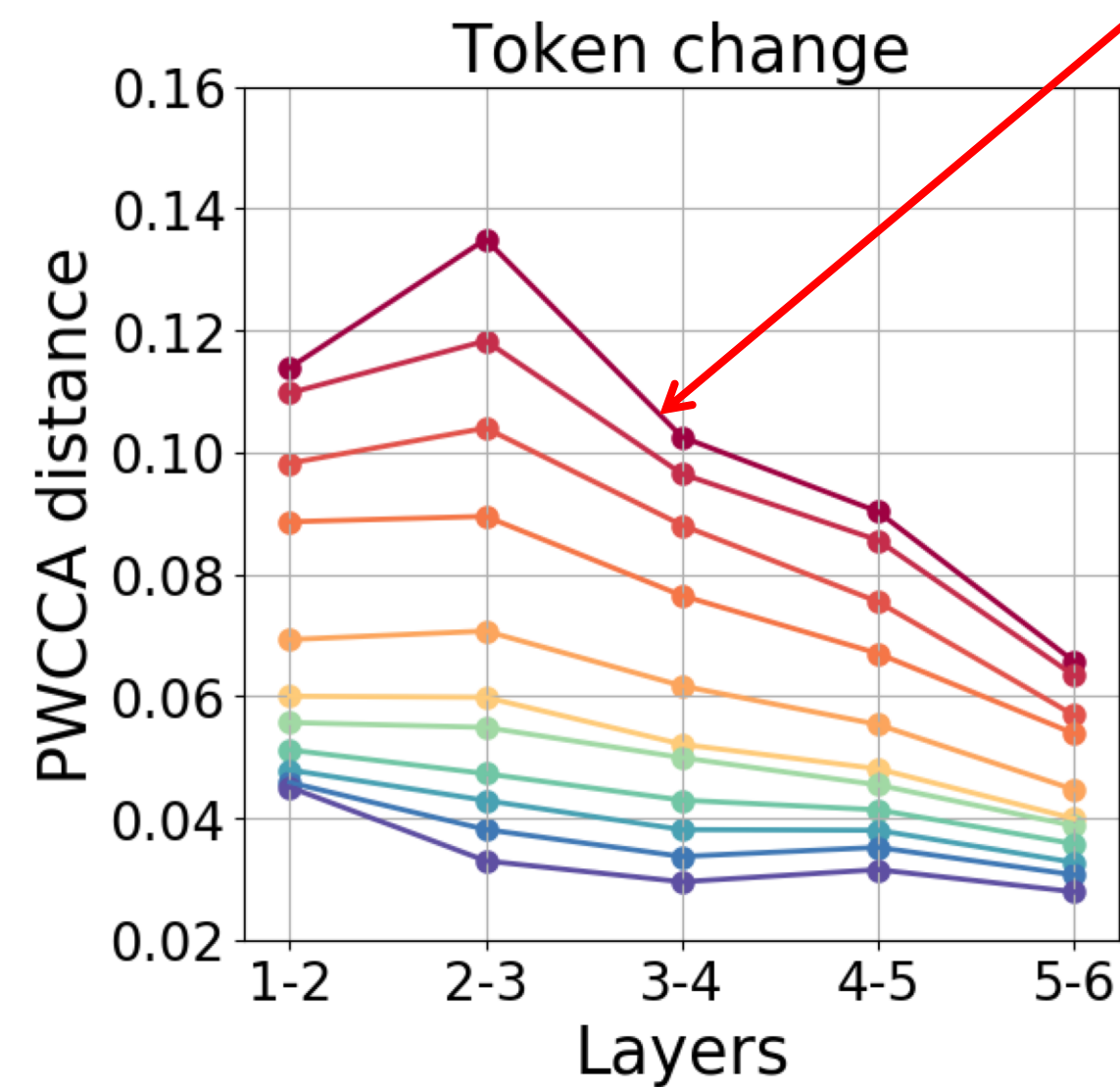
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Frequent tokens change more than rare

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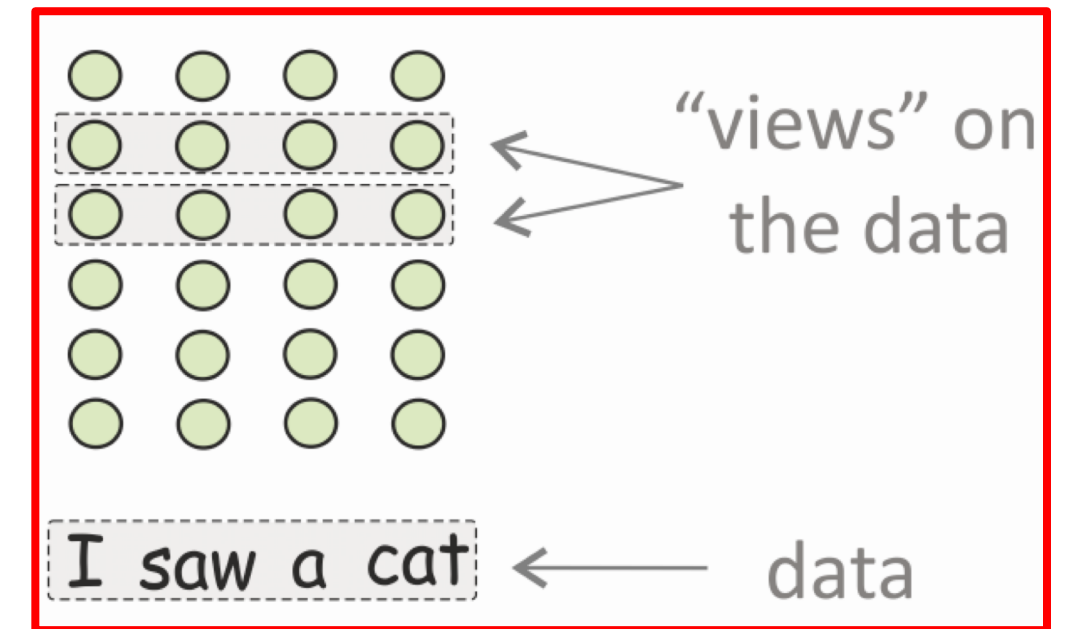
LM





# Varying token frequency: Amount of change

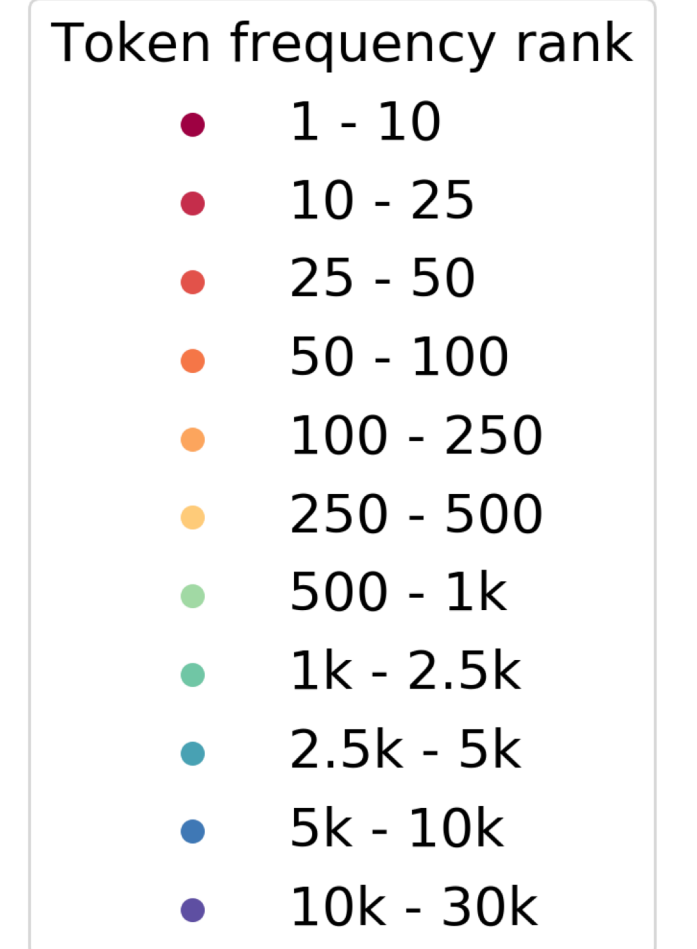
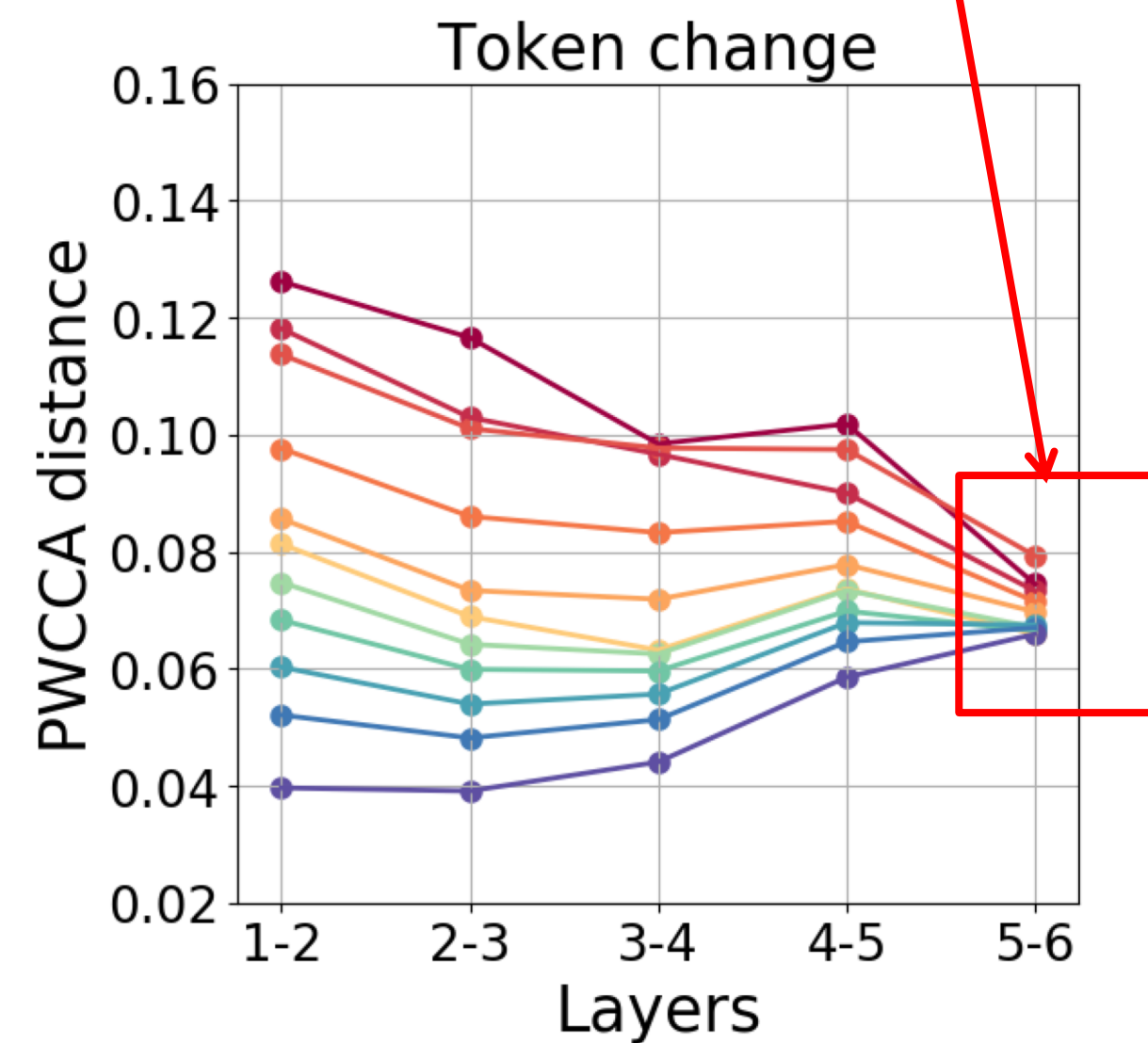
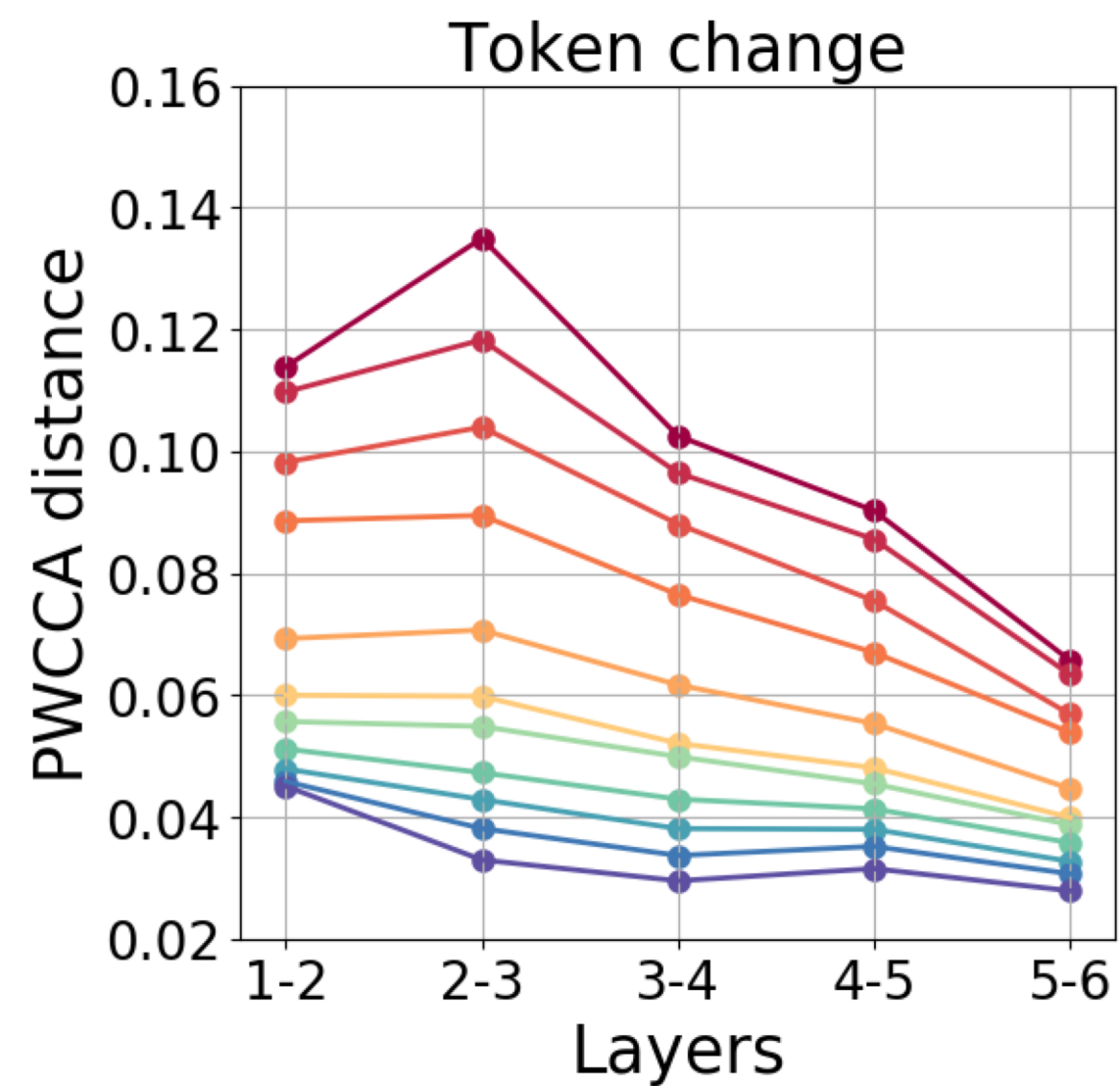
- **Change:** how much representations of these tokens change between layers



Roughly the same amount of change

MT

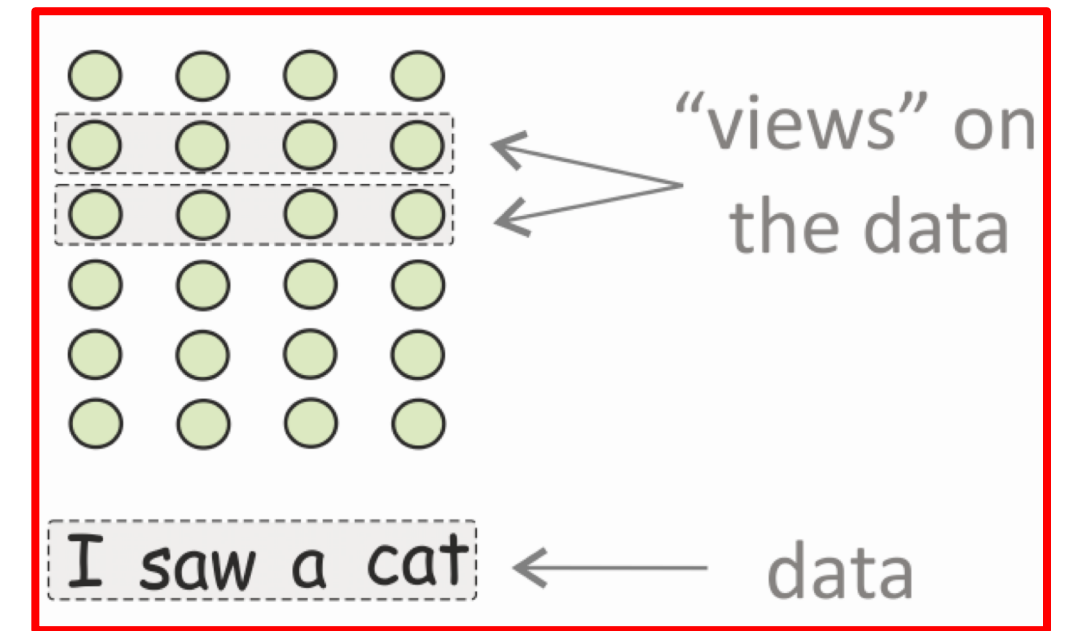
LM



# Varying token frequency: Amount of change

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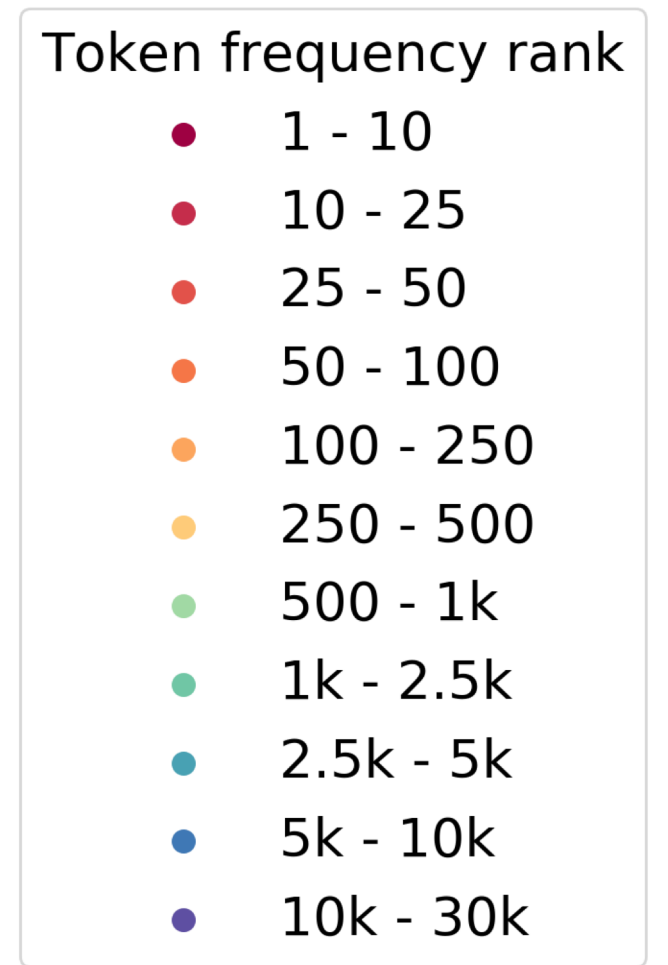
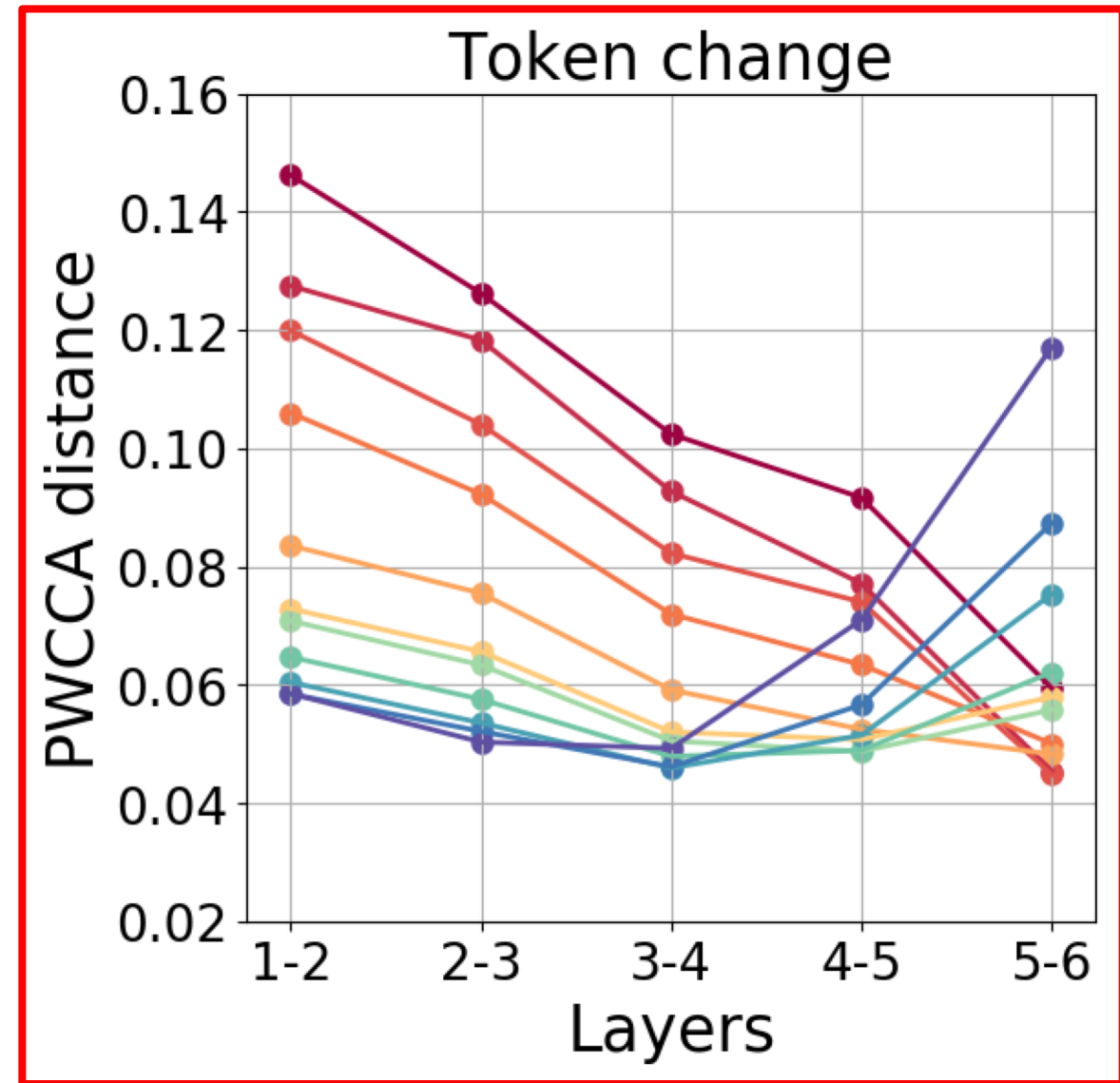
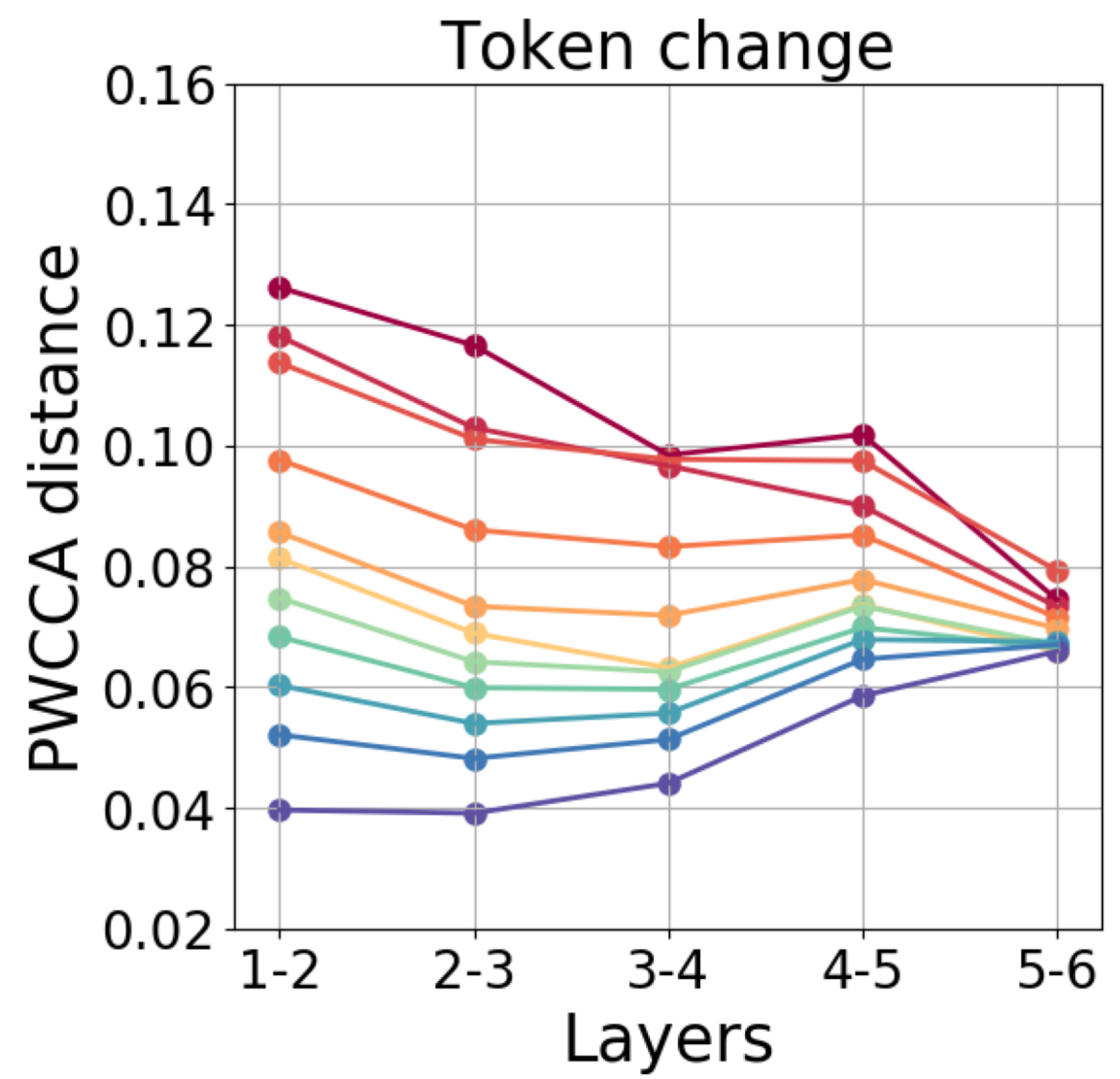
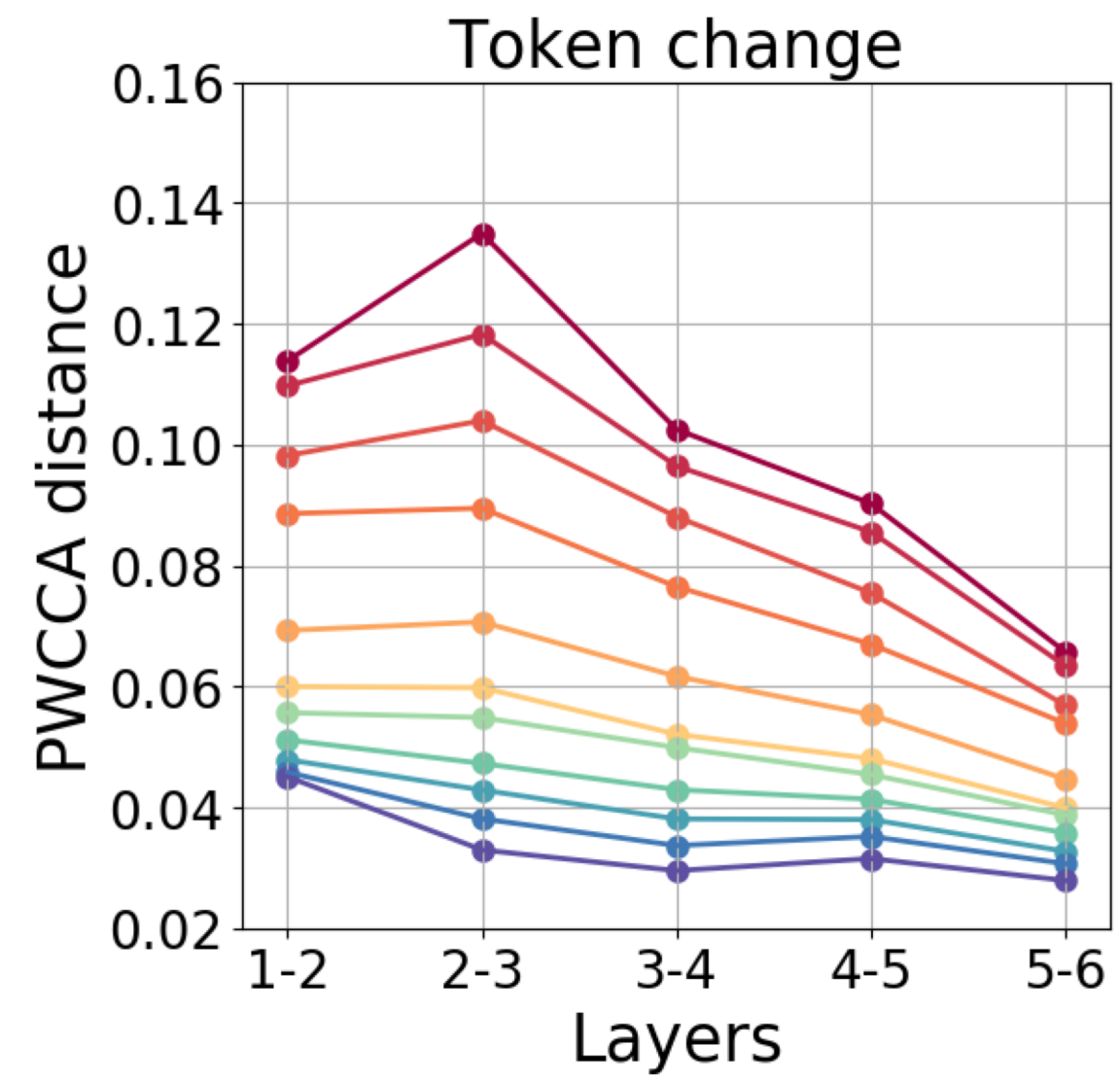
The two stages again!



MT

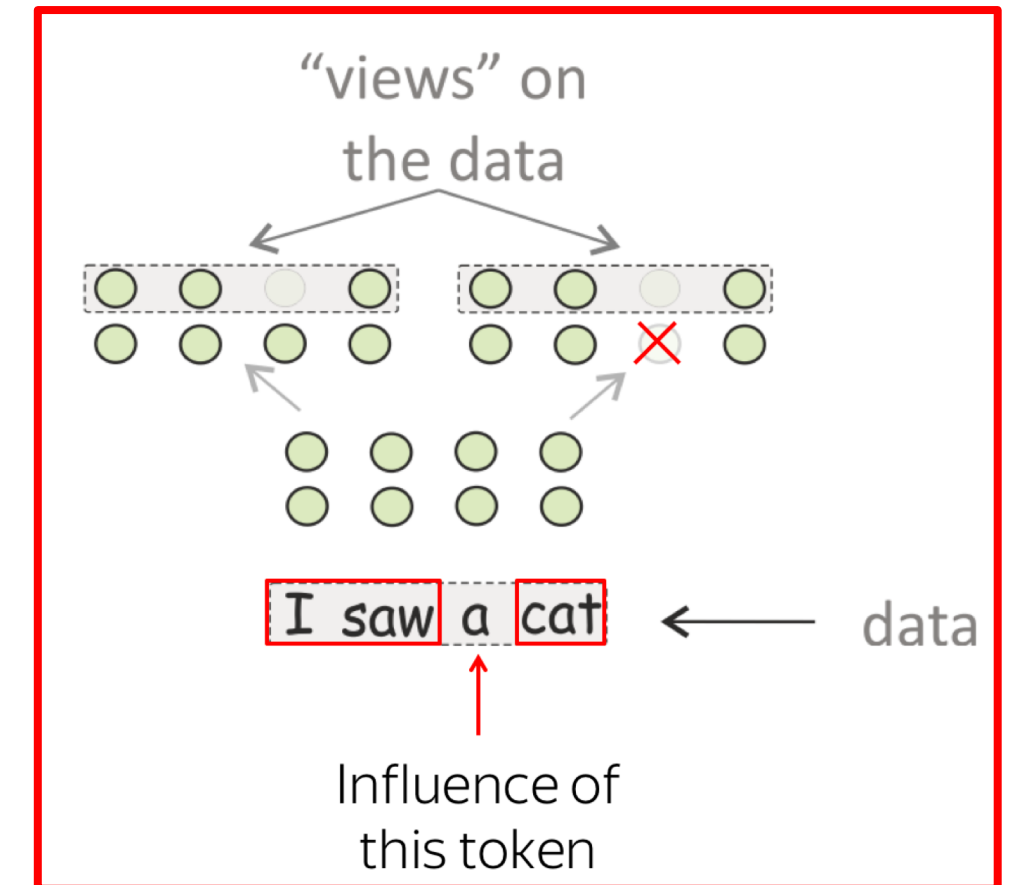
LM

MLM

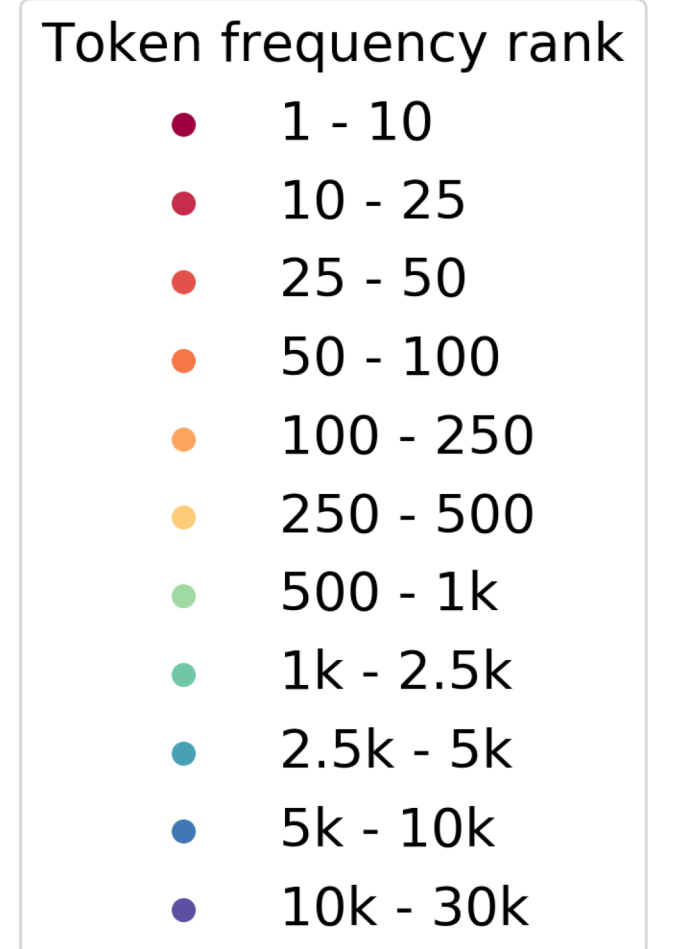
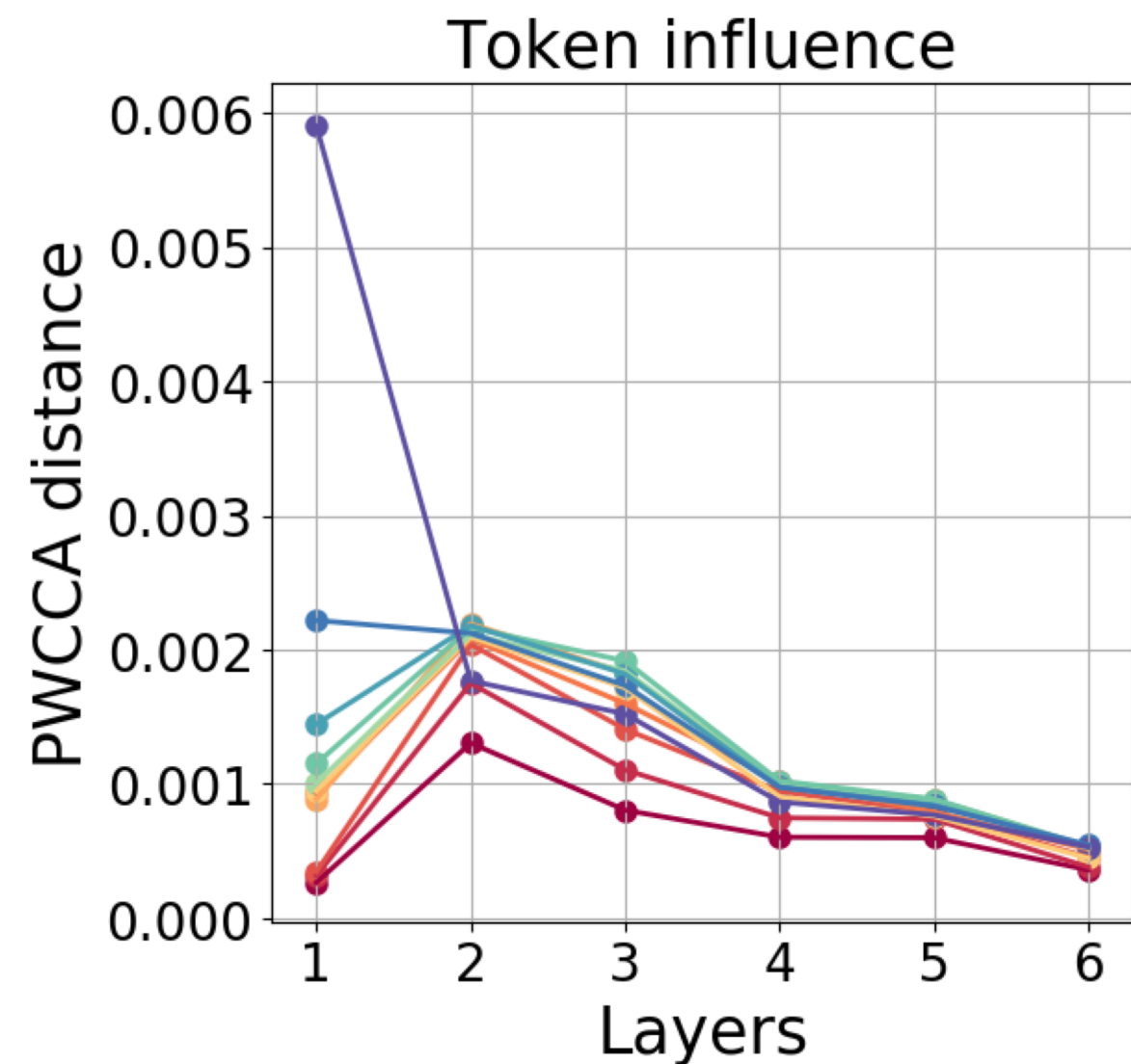


# Varying token frequency: Amount of influence

- Influence:** how much representations of other tokens change if this token is not present



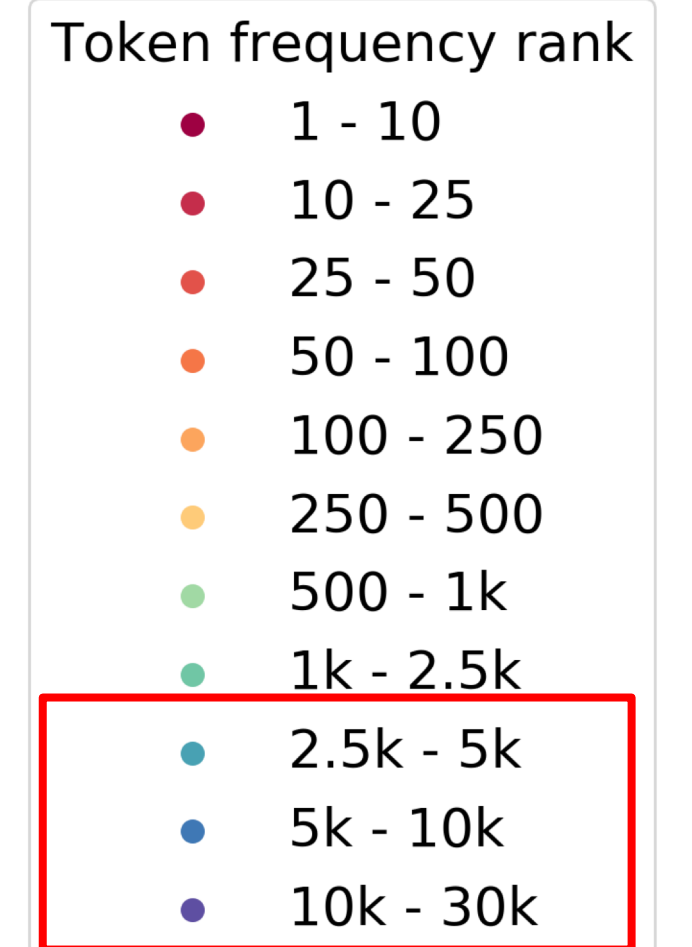
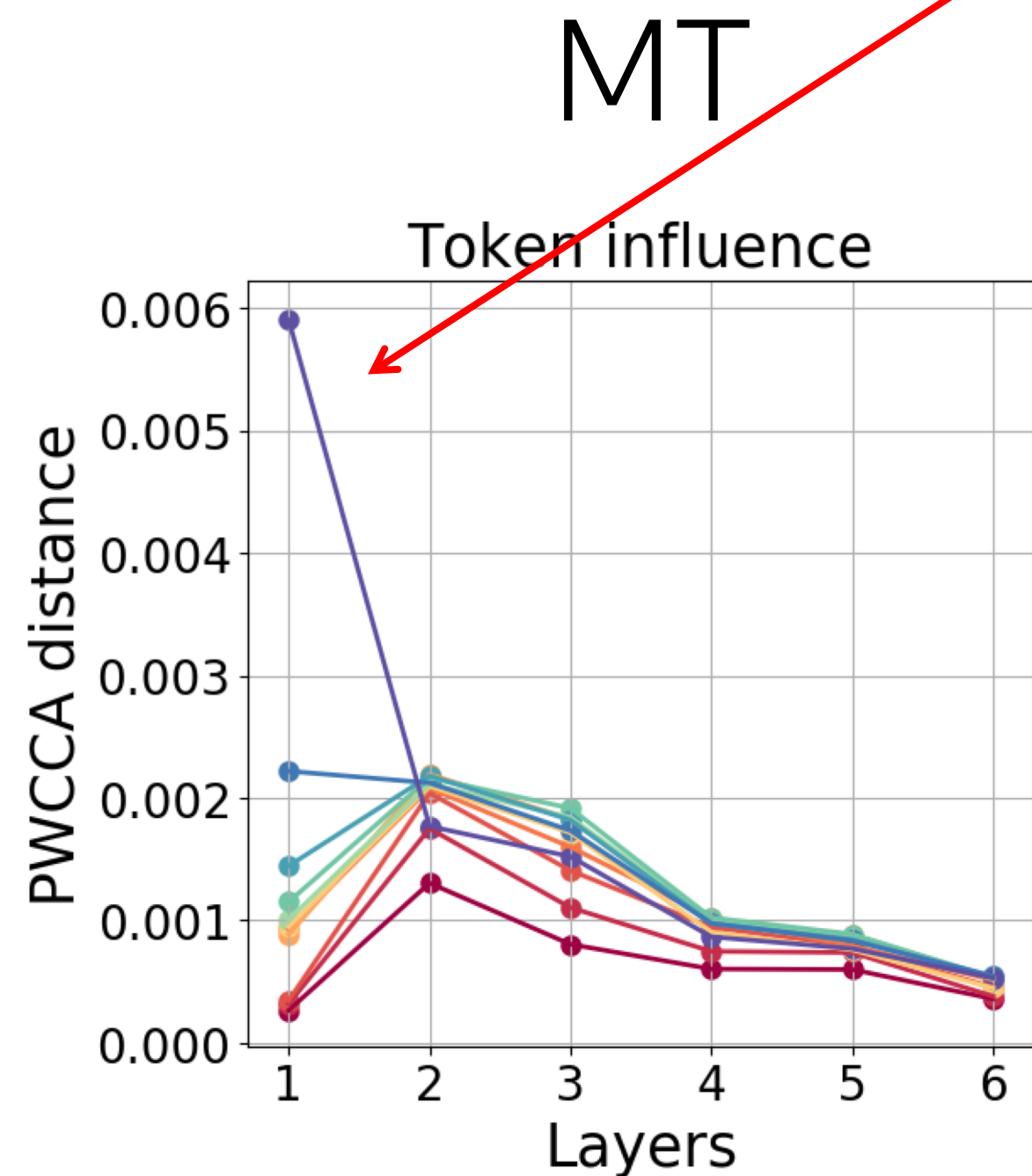
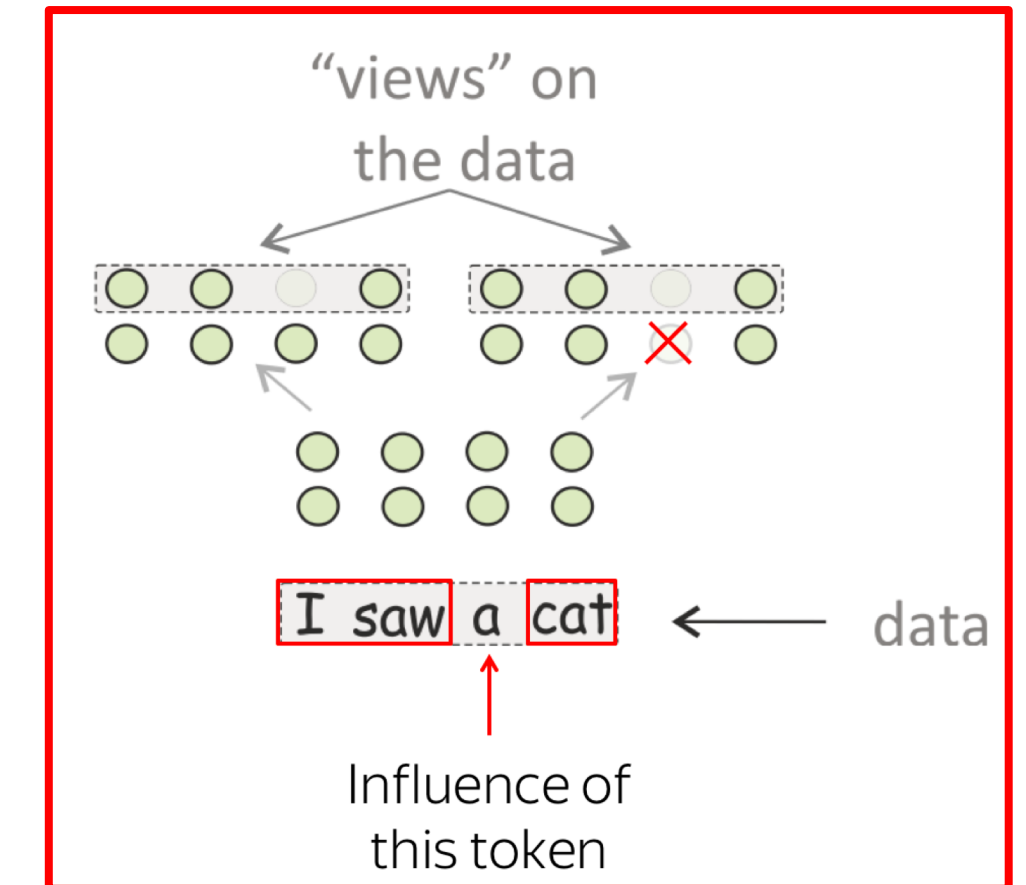
MT



# Varying token frequency: Amount of influence

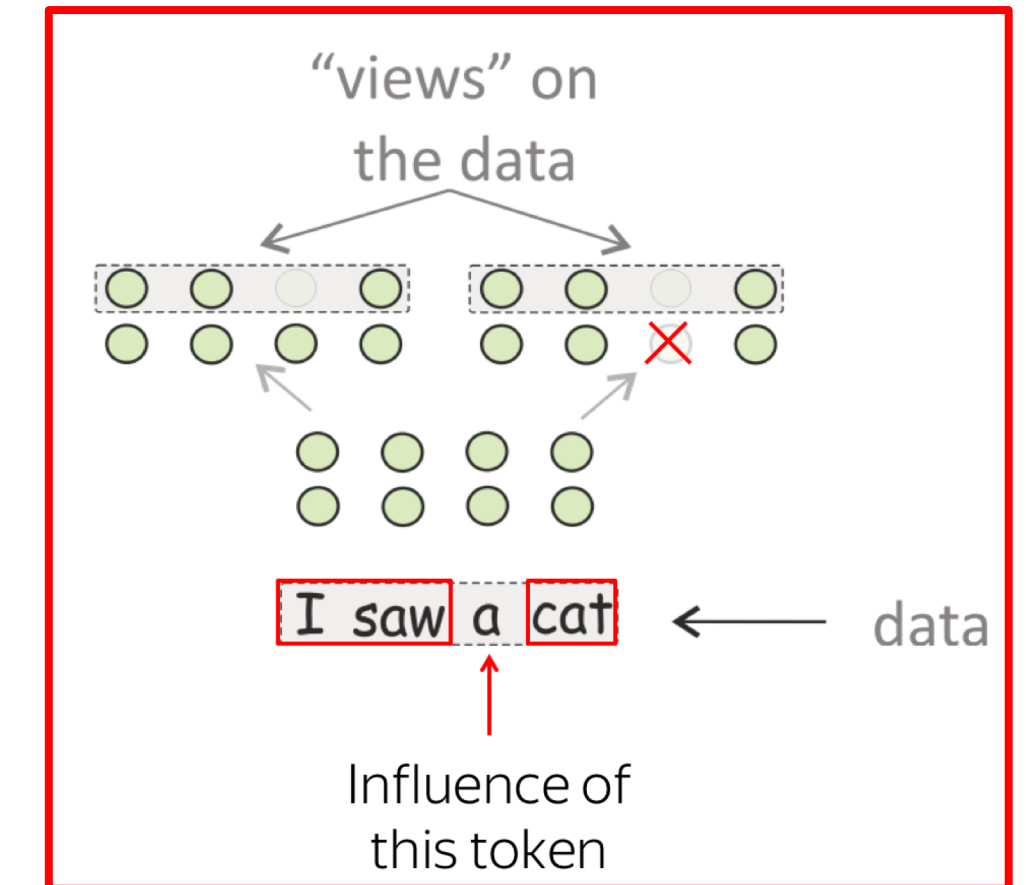
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Rare tokens influence more



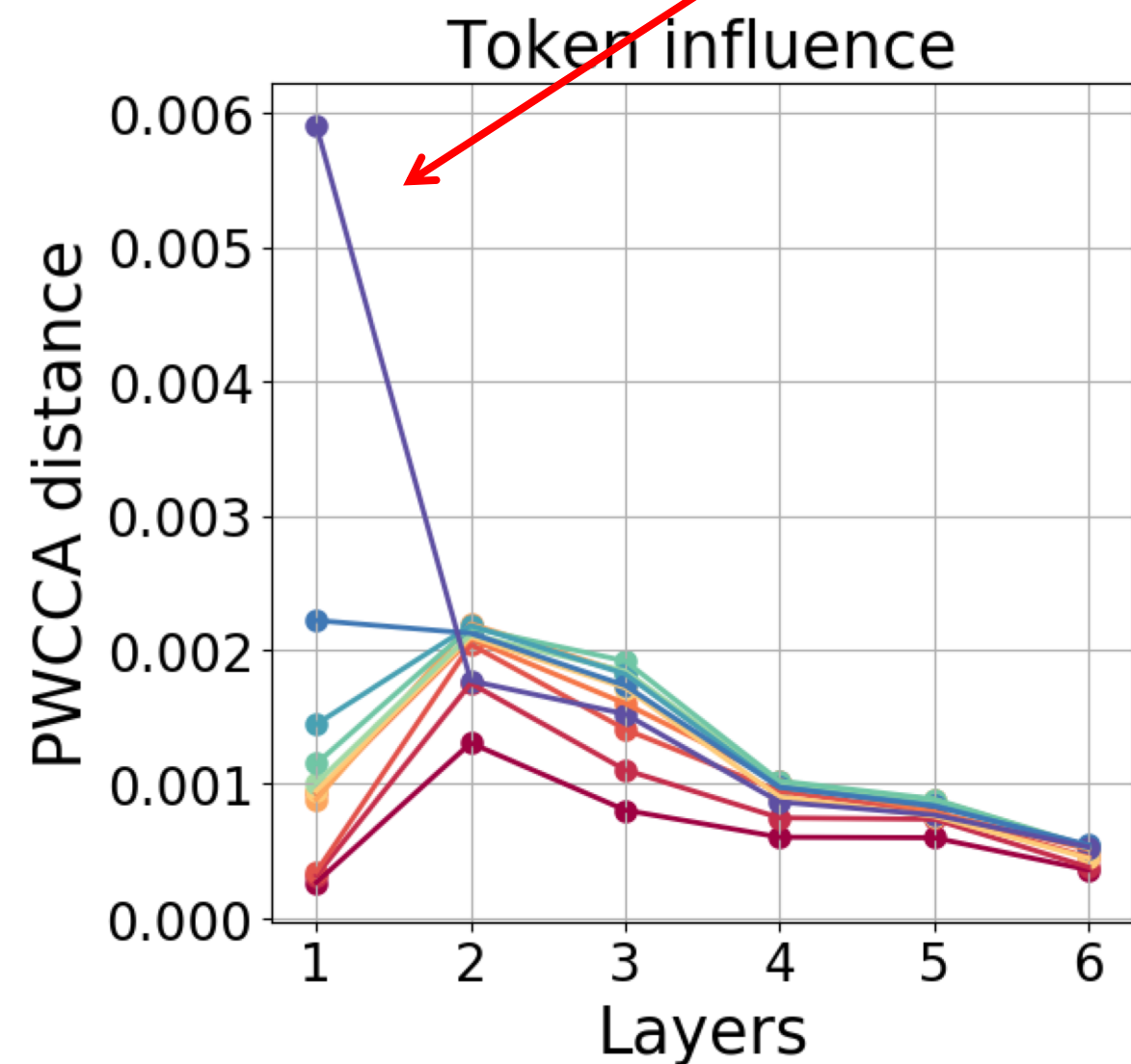
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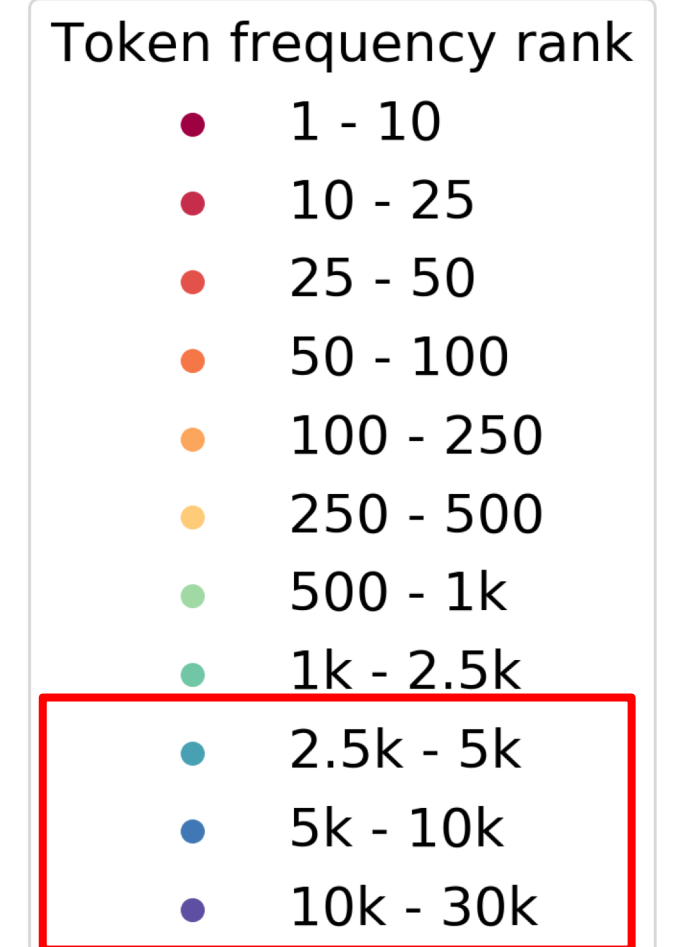
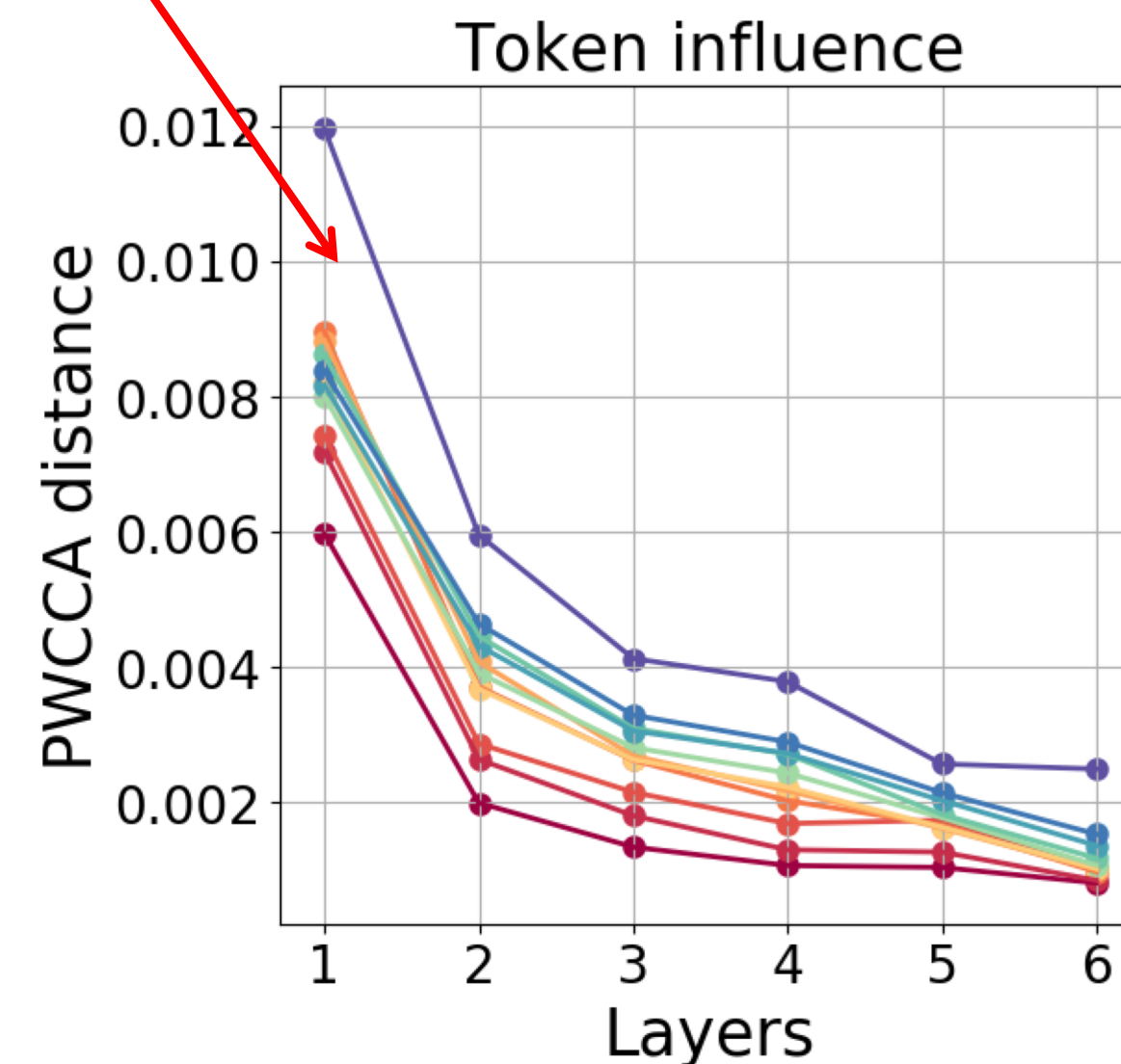


Rare tokens influence more

MT

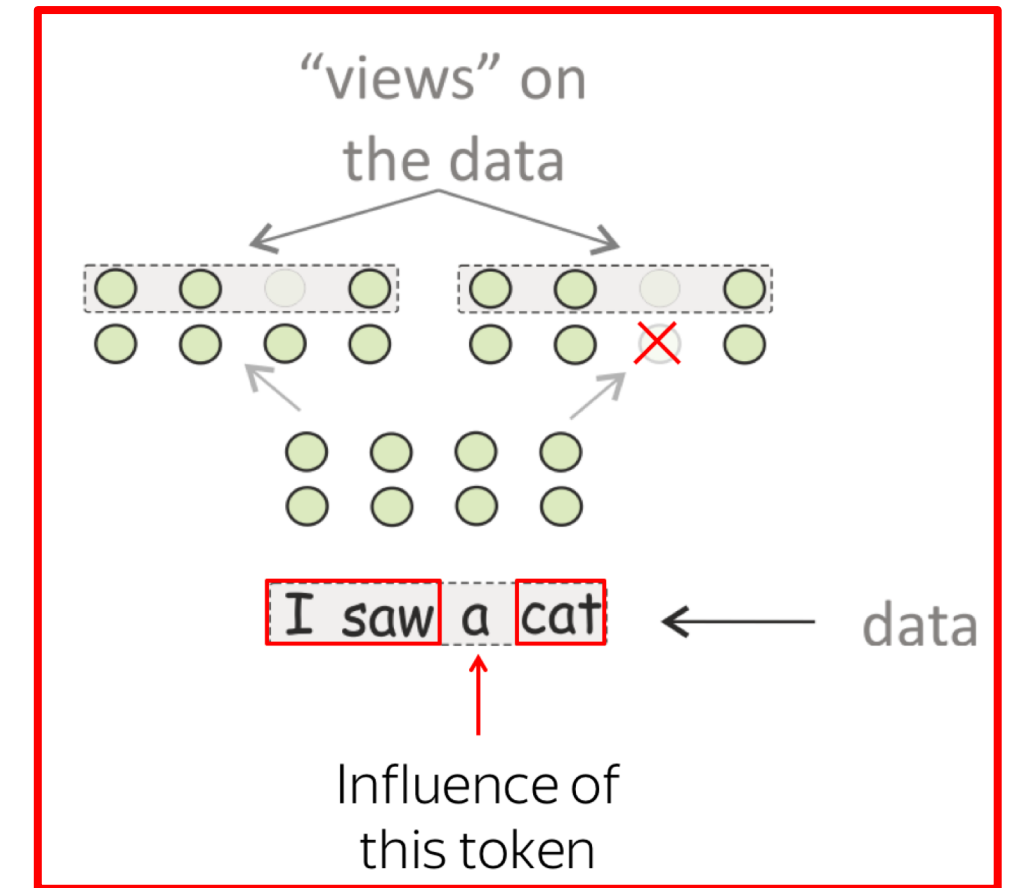


LM



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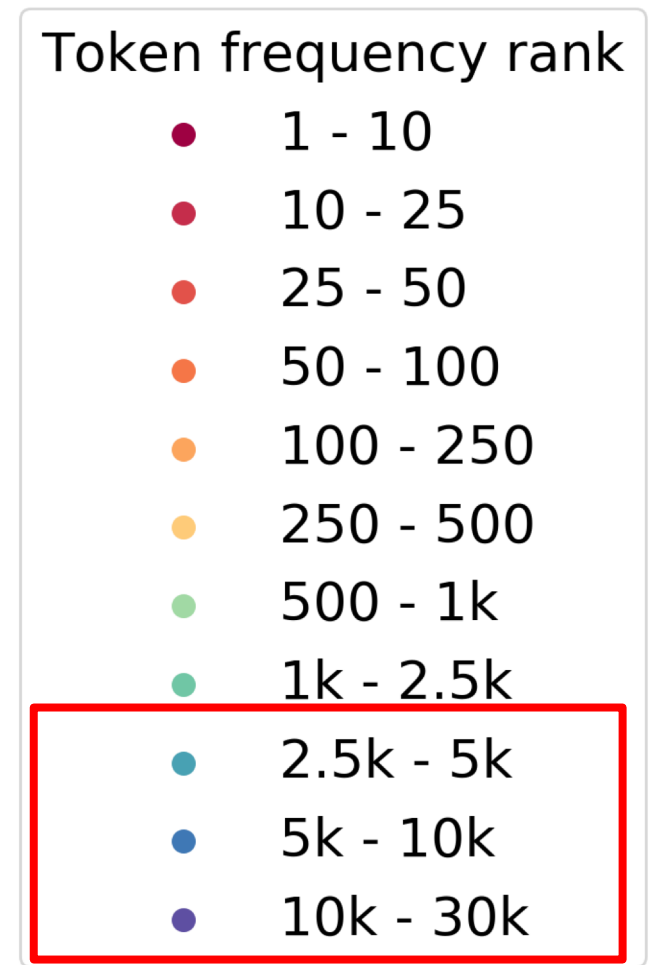
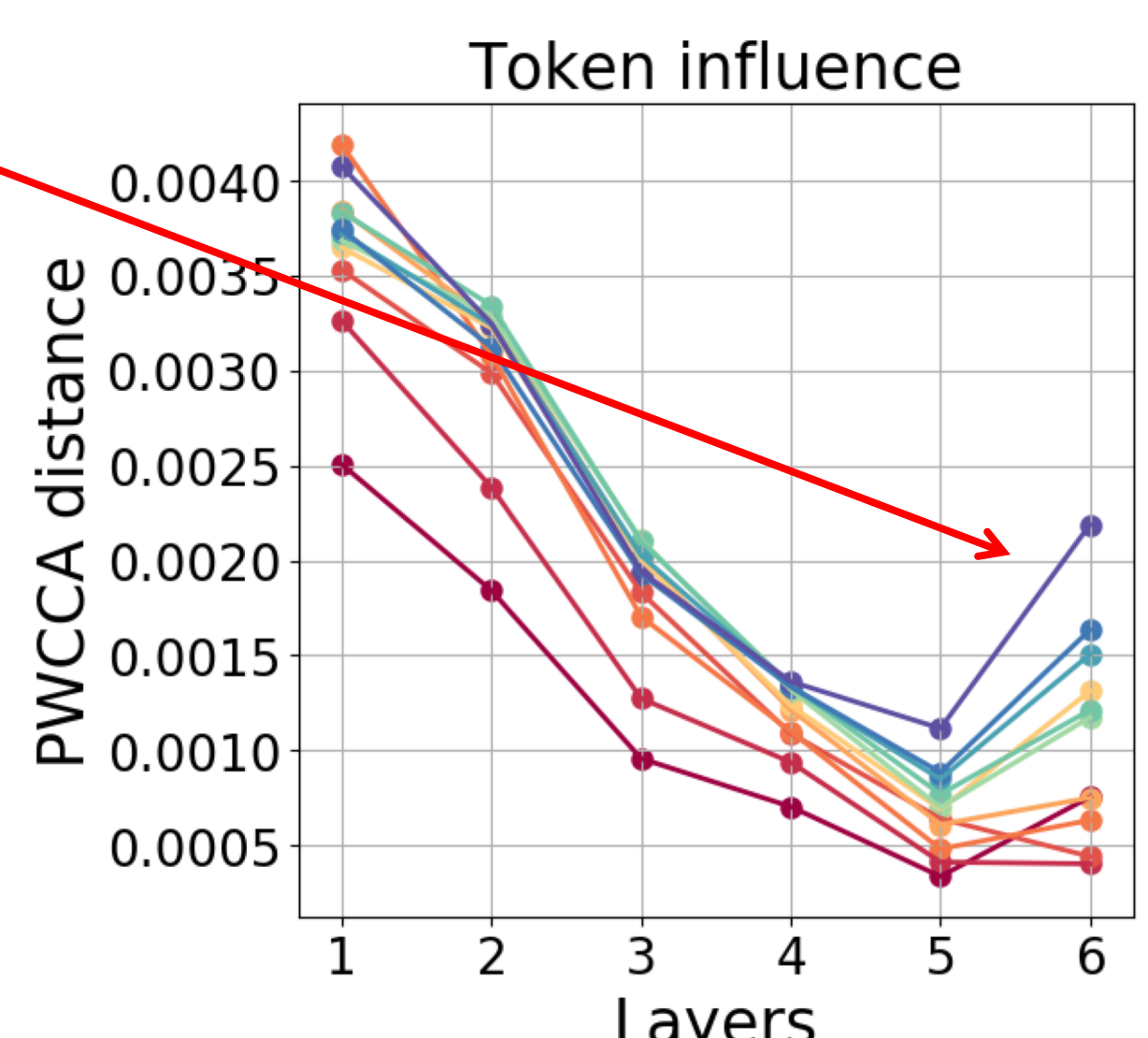
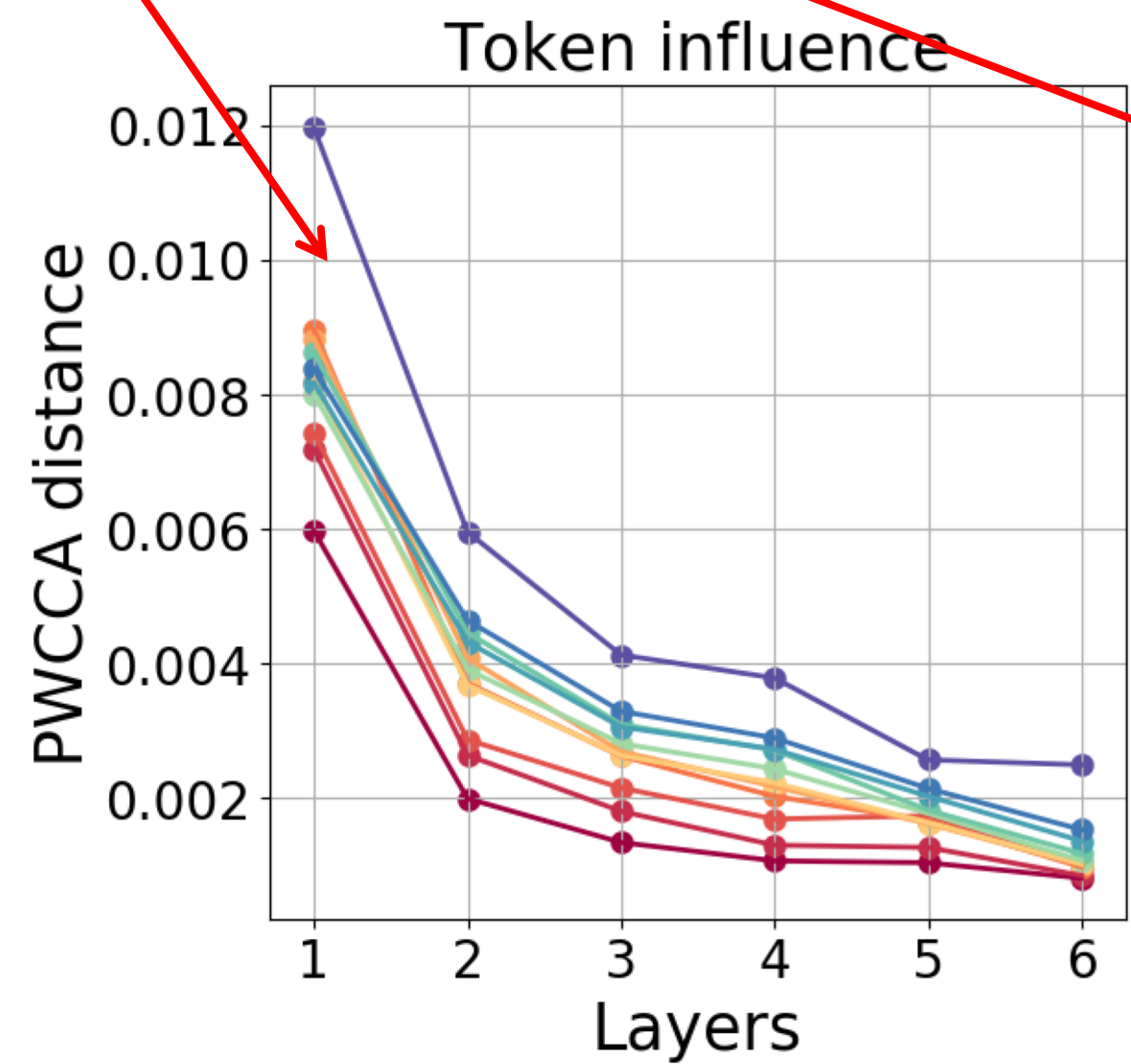
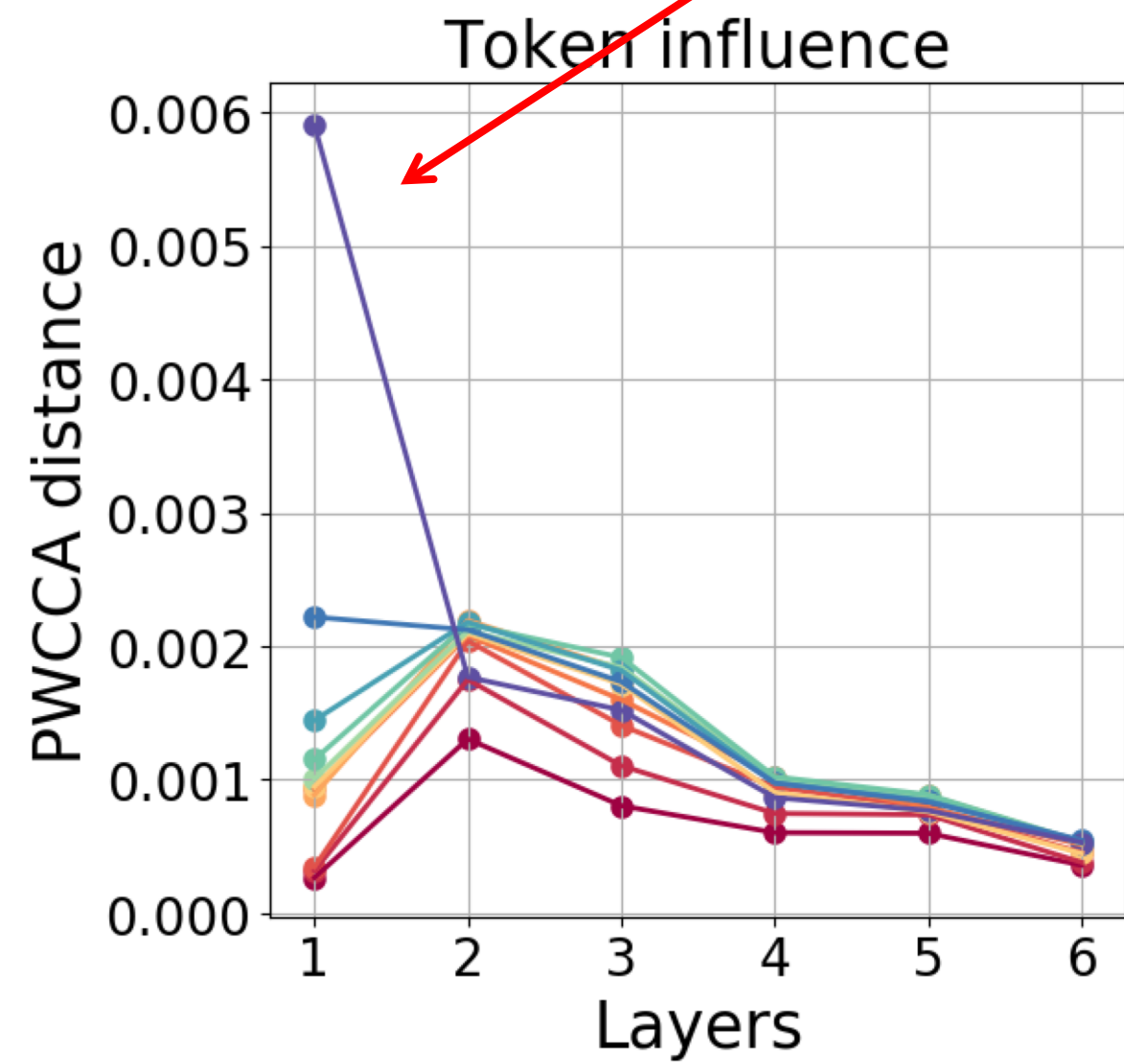


Rare tokens influence more

MT

LM

MLM



# Plan

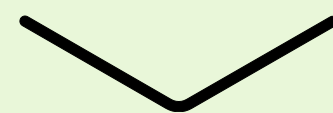
- Evolution of representations of individual tokens
- Training objectives: LM, MLM, MT
- "Puzzles" from previous work
- The Information-Bottleneck: our point of view
- Experiments
  - Information Bottleneck for token representations
  - Analyzing changes and influences
  - ...

# Plan

- Evolution of representations of individual tokens
- Training objectives: LM, MLM, MT
- "Puzzles" from previous work
- The Information-Bottleneck: our point of view
- Experiments
  - Information Bottleneck for token representations
  - Analyzing changes and influences
  - What does a layer represent?

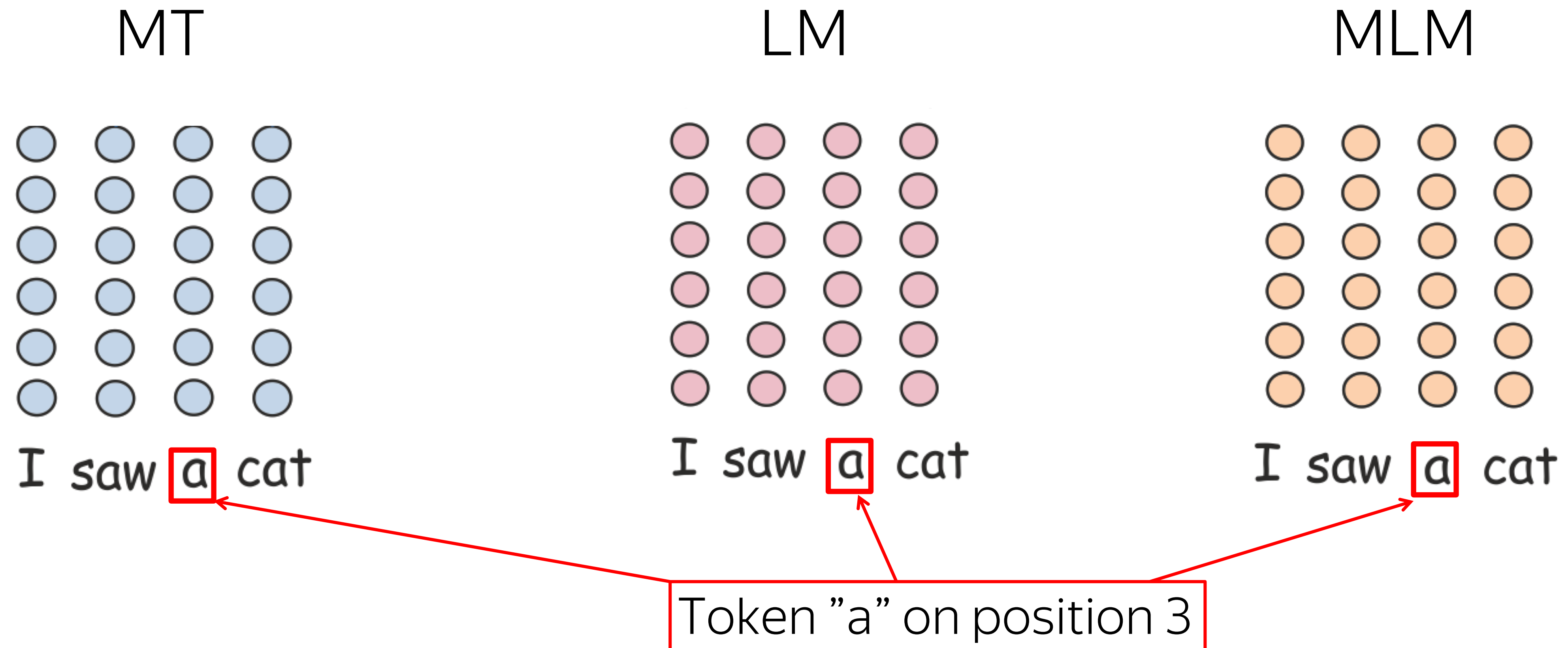


What does a layer represent?



# The bottom-up evolution

- All models start from the same representation: token identity and position



# Preserving token identity

The cats **are** tired of sitting on a mat

The cats **are** hungry

This **is** a great opportunity

**Are** you happy?

It **is** raining    This mat **is** full of cats

Simon **is** a lazy cat

**Is** it Jane?

What **is** an evolution?

These apples **are** so tasty!

They **were** on vacation last week

**Was** it a good vacation?

I **was** glad to see you

- Take large number of representations of different tokens

# Preserving token identity

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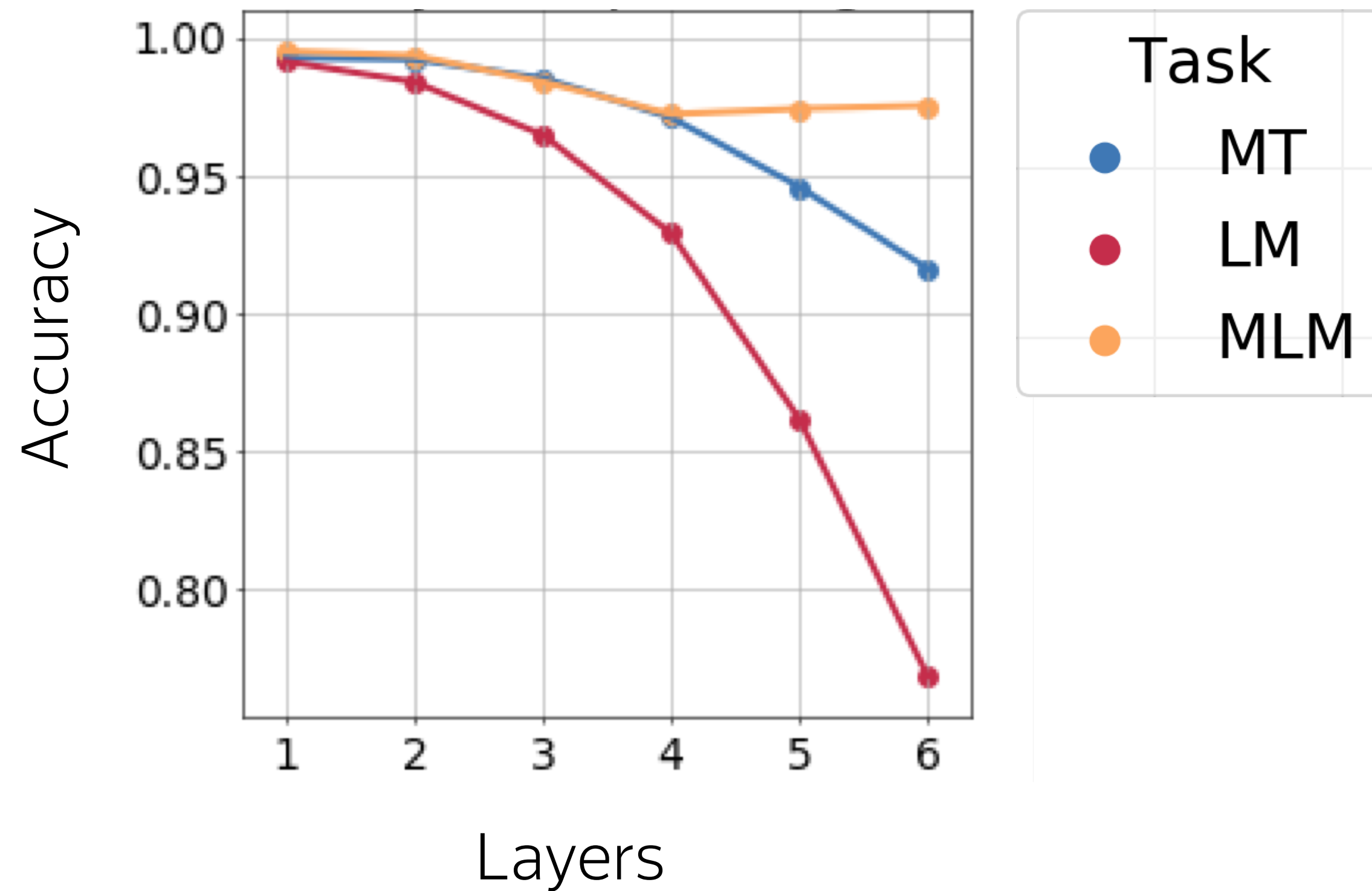
They **were** on vacation last week

**Was** it a good vacation?

I **was** glad to see you

- Take large number of representations of different tokens
- Evaluate the proportion of top-k neighbors which have the same token identity

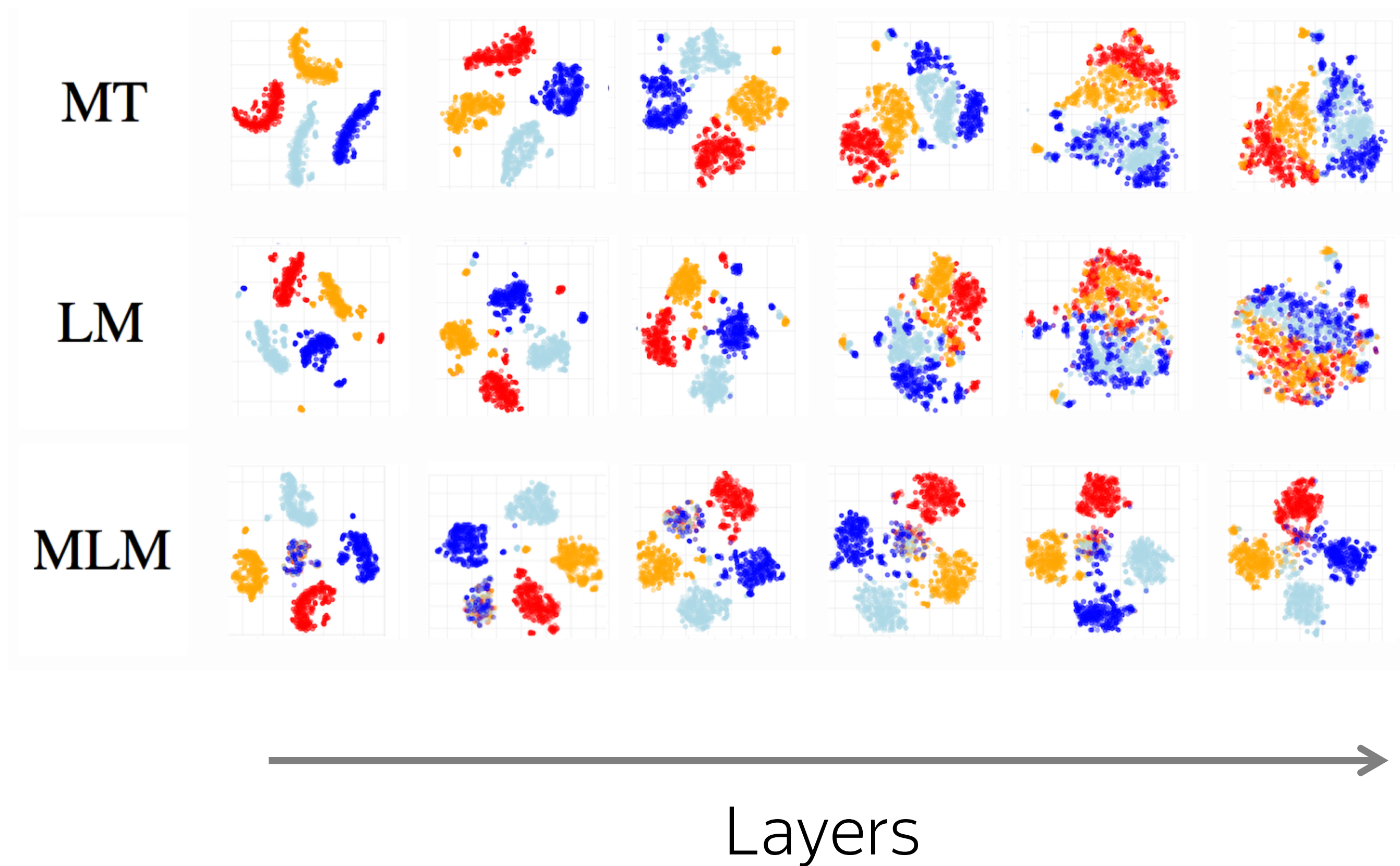
# Preserving token identity



Really similar to the MI results!

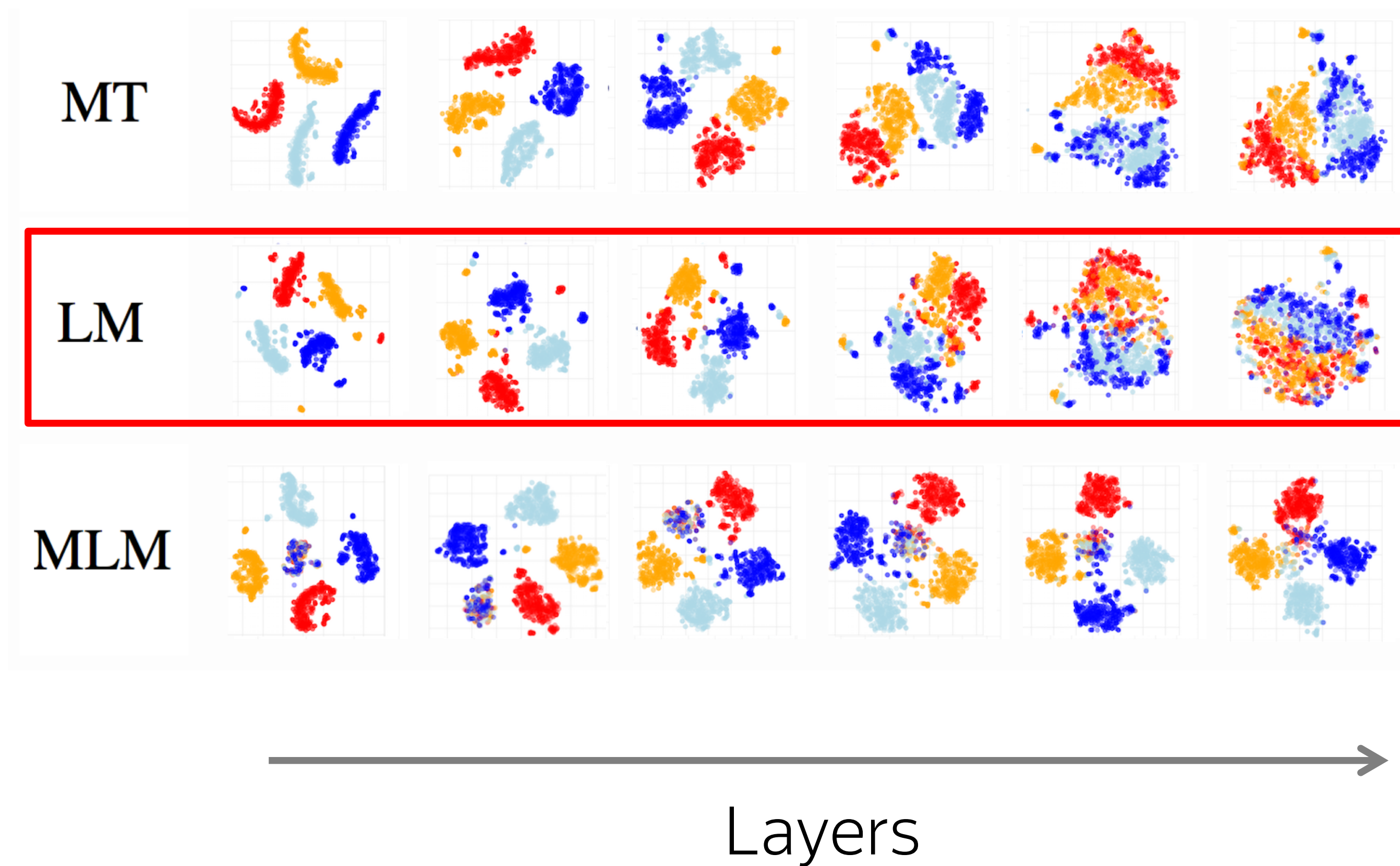
# Preserving token identity

- t-SNE of different occurrences of the tokens **is**, **are**, **was**, **were**



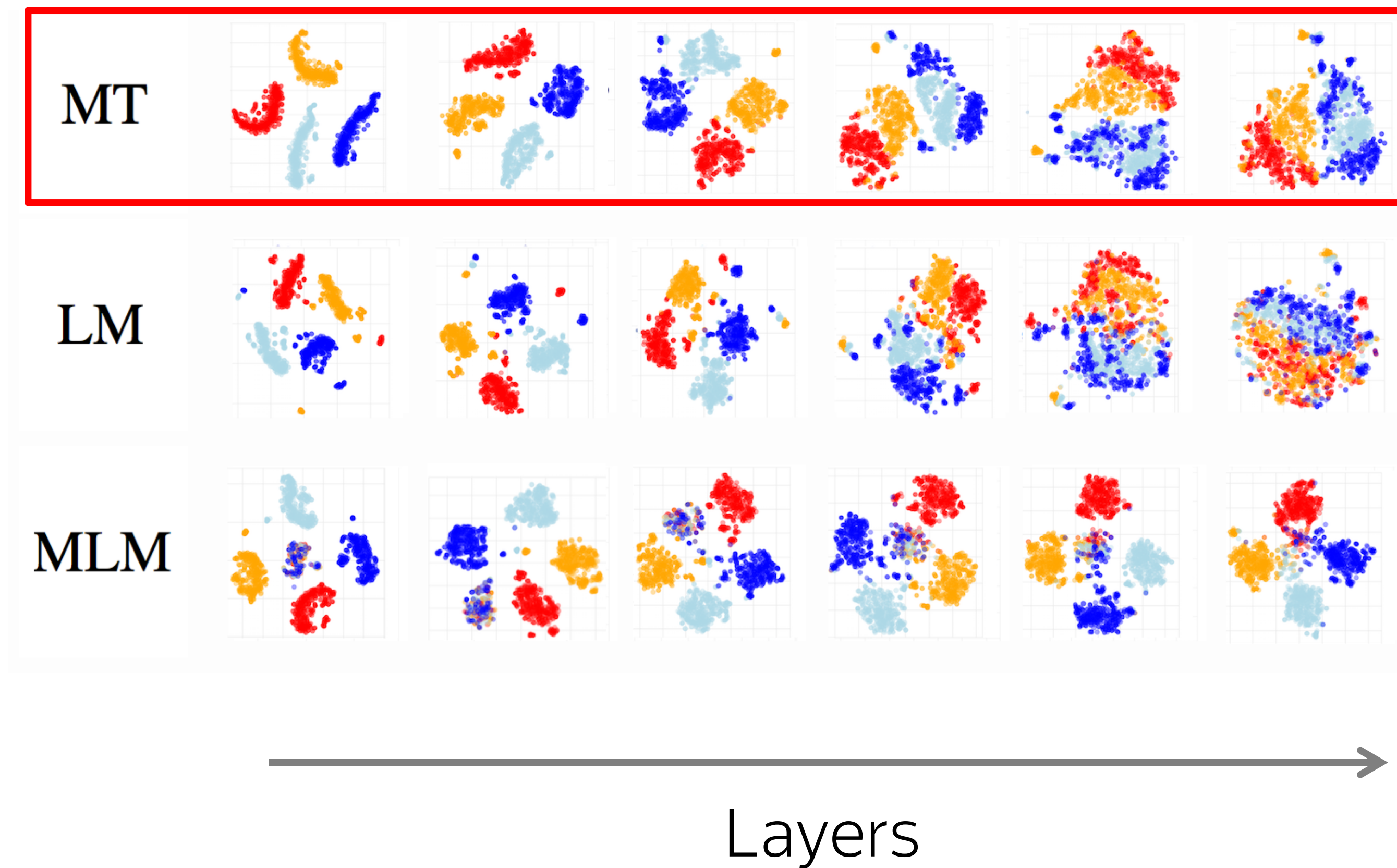
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# Preserving token identity

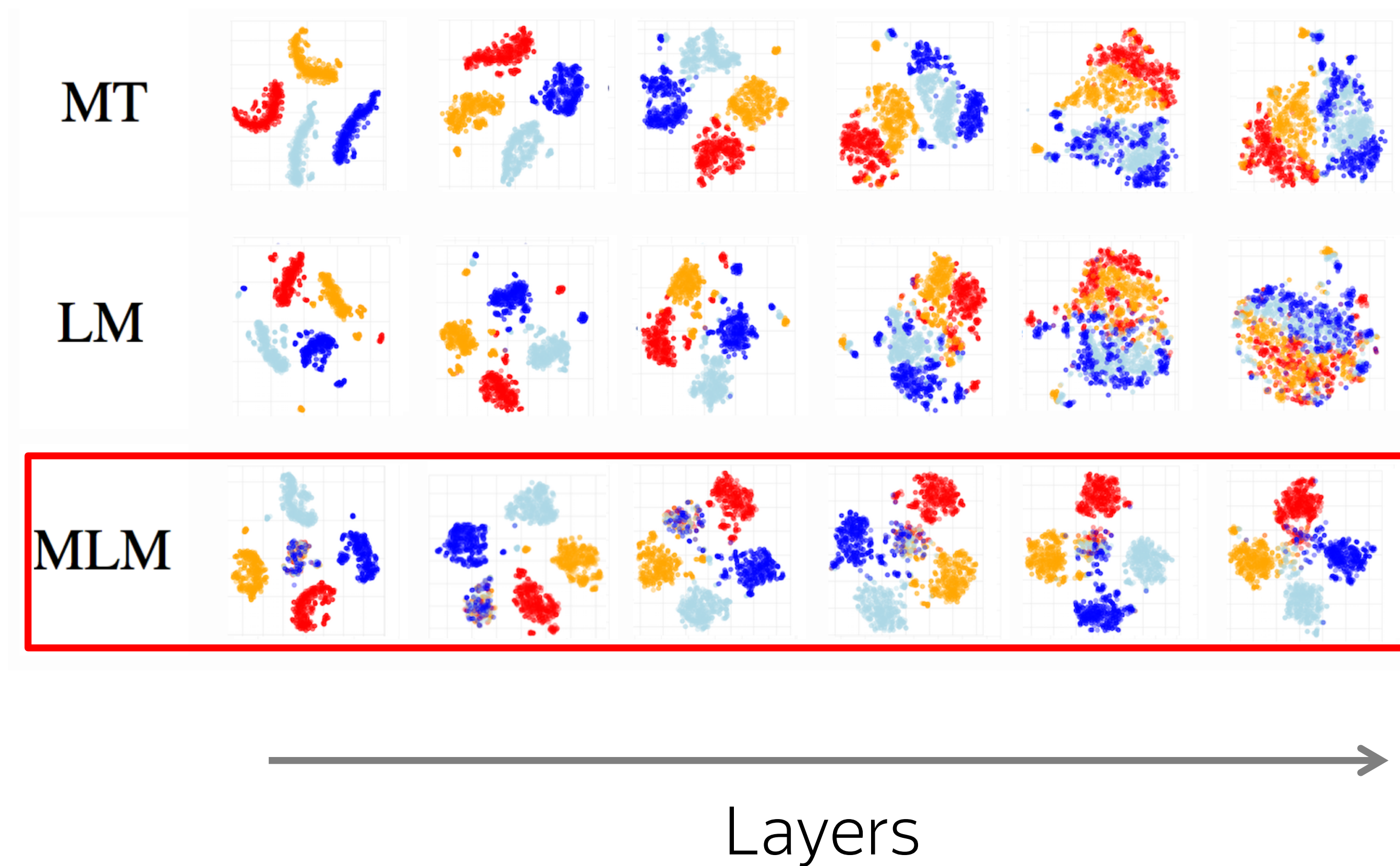
- t-SNE of different occurrences of the tokens **is**, **are**, **was**, **were**





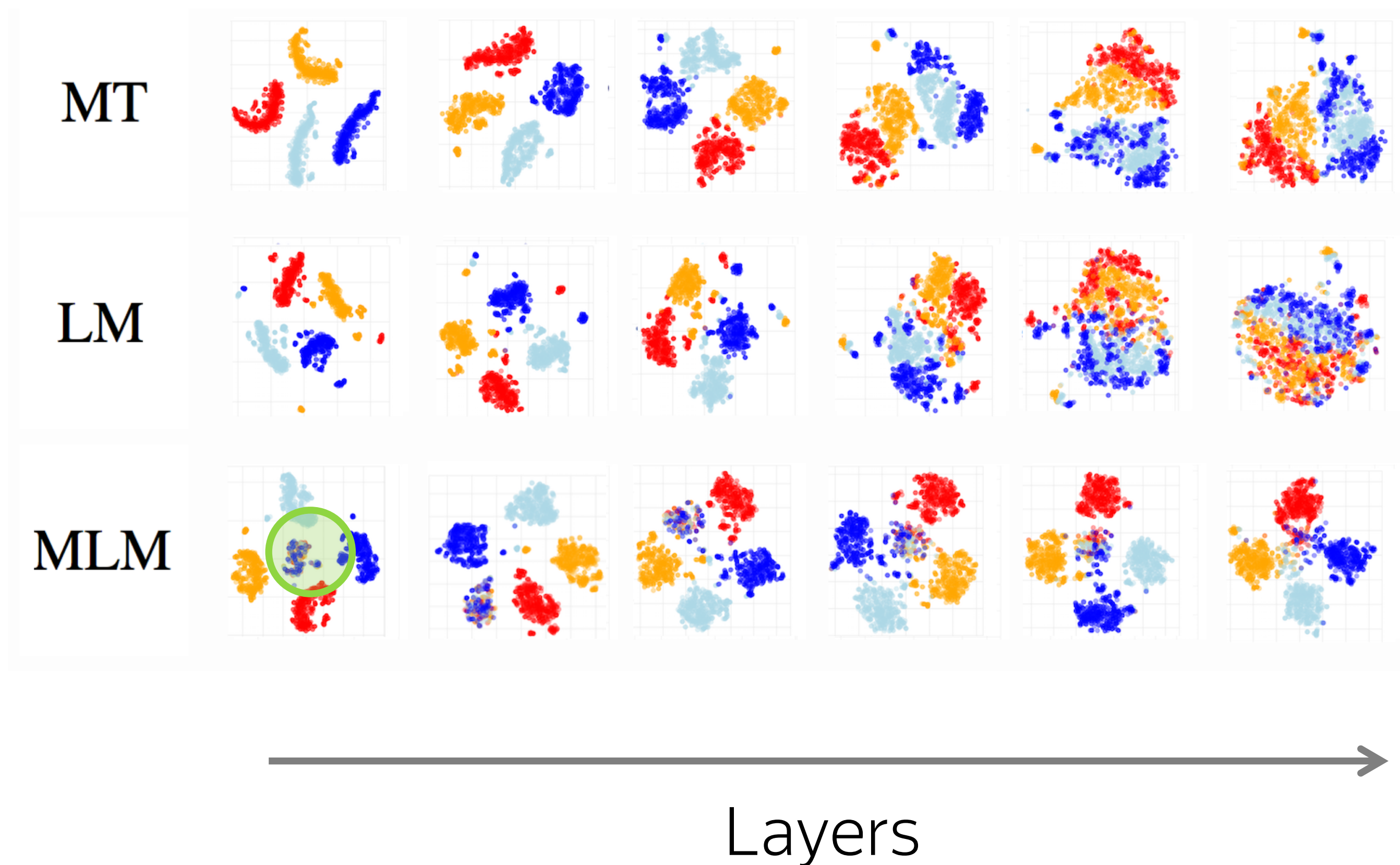
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# Preserving token identity

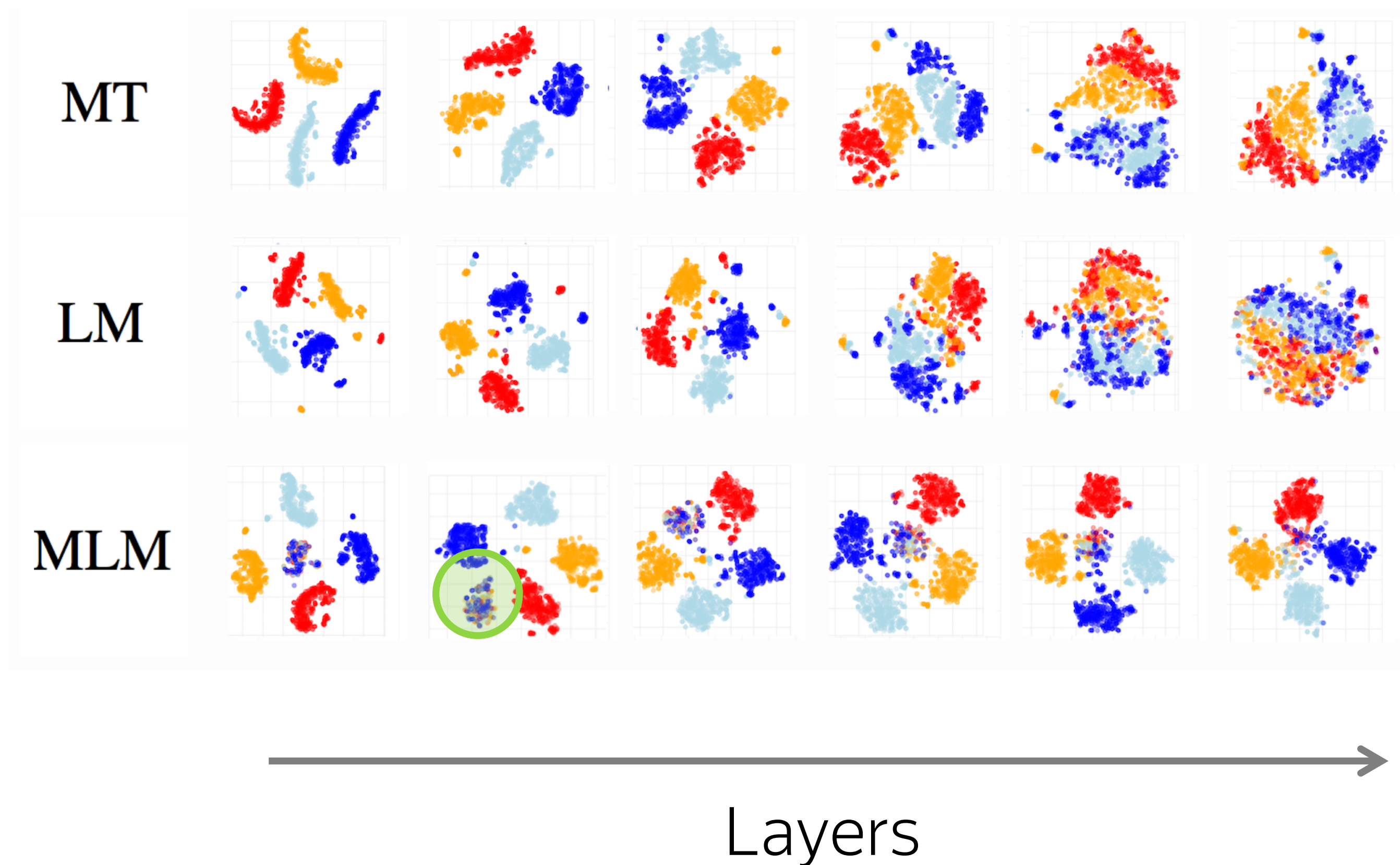
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Look how MLM disambiguates masked tokens

# Preserving token identity

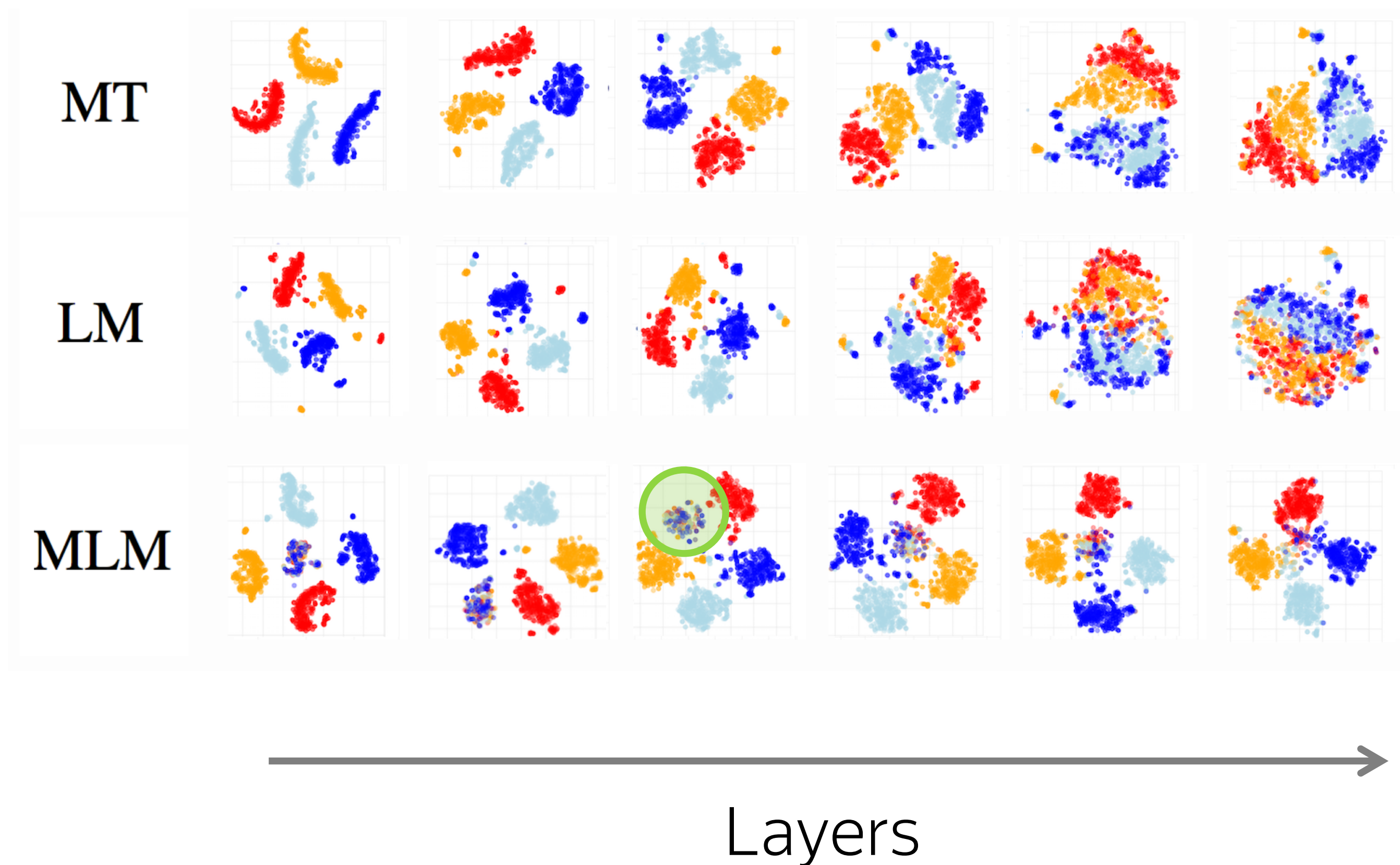
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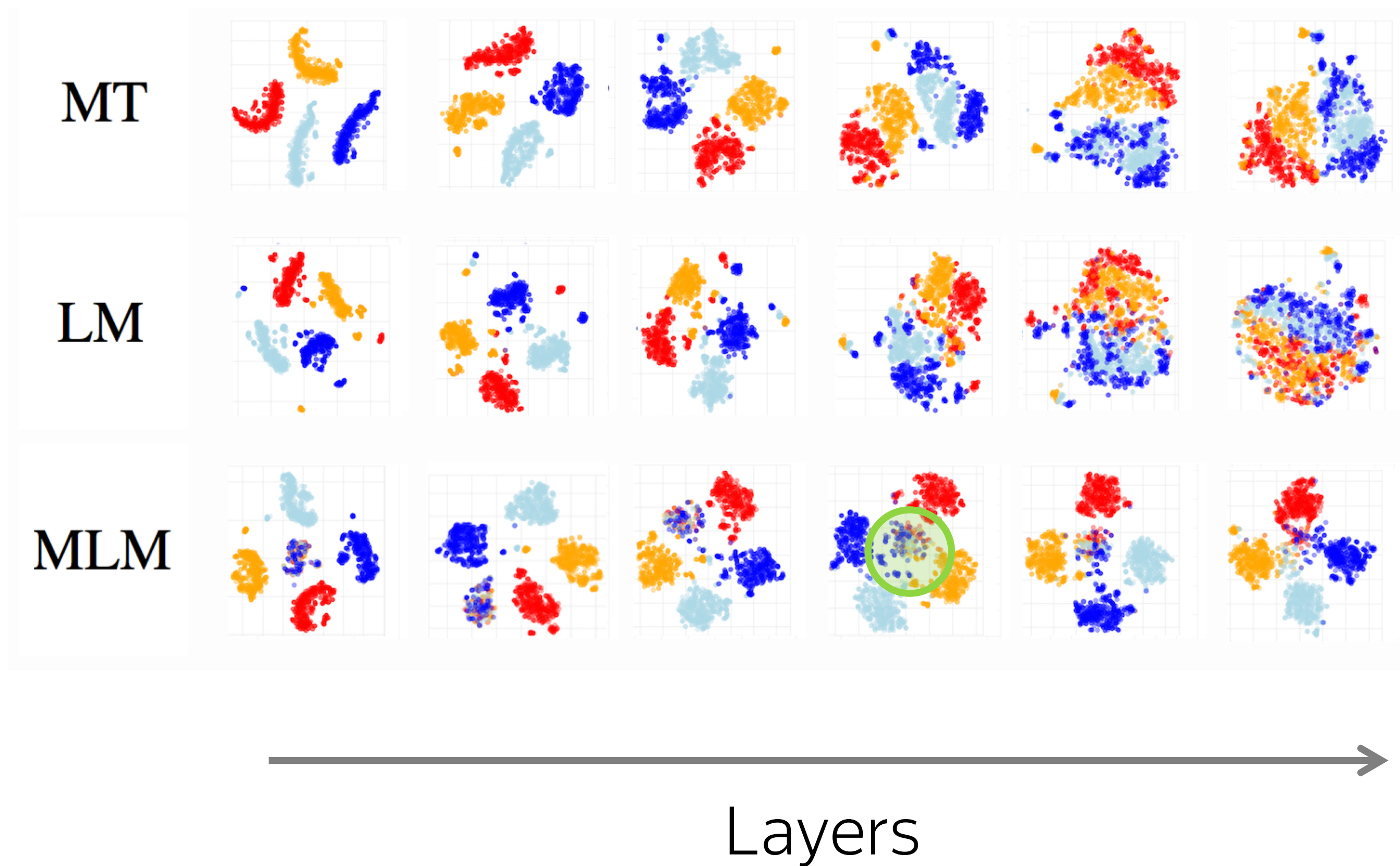
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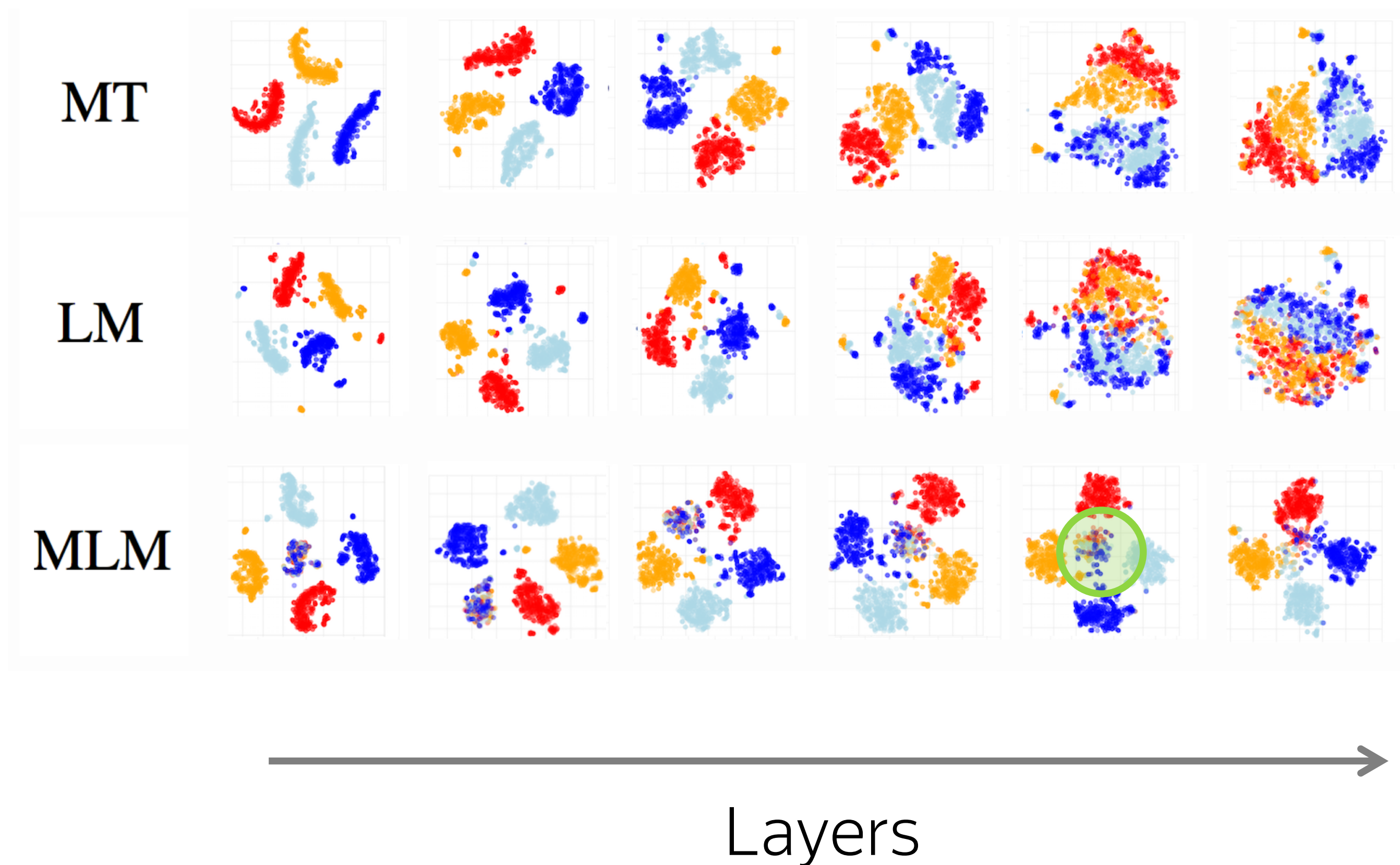
- t-SNE of different occurrences of the tokens **is**, **are**, **was**, **were**



Look how MLM  
disambiguates  
masked tokens

# Preserving token identity

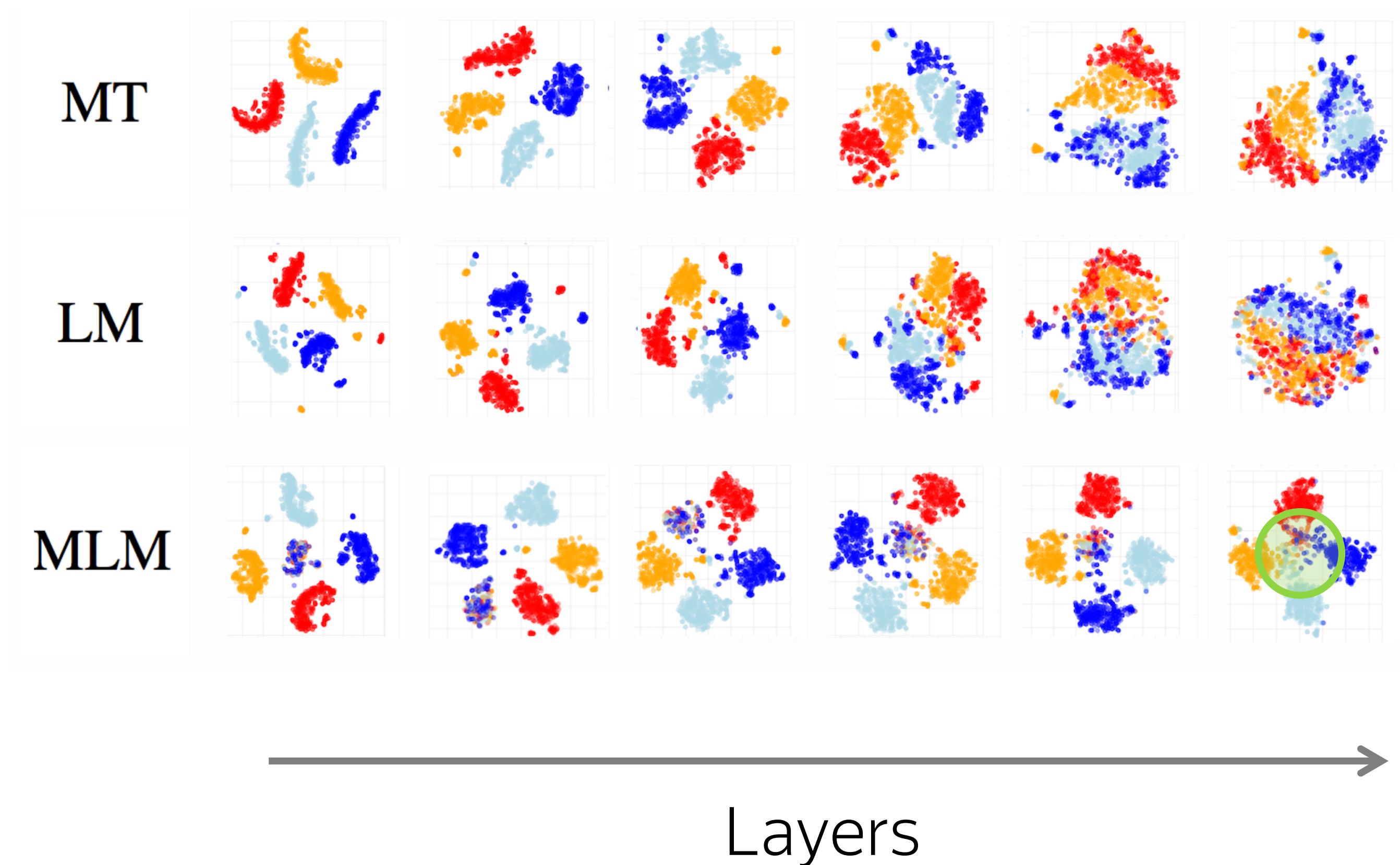
- t-SNE of different occurrences of the tokens **is**, **are**, **was**, **were**



Look how MLM disambiguates masked tokens

# Preserving token identity

- t-SNE of different occurrences of the tokens **is**, **are**, **was**, **were**



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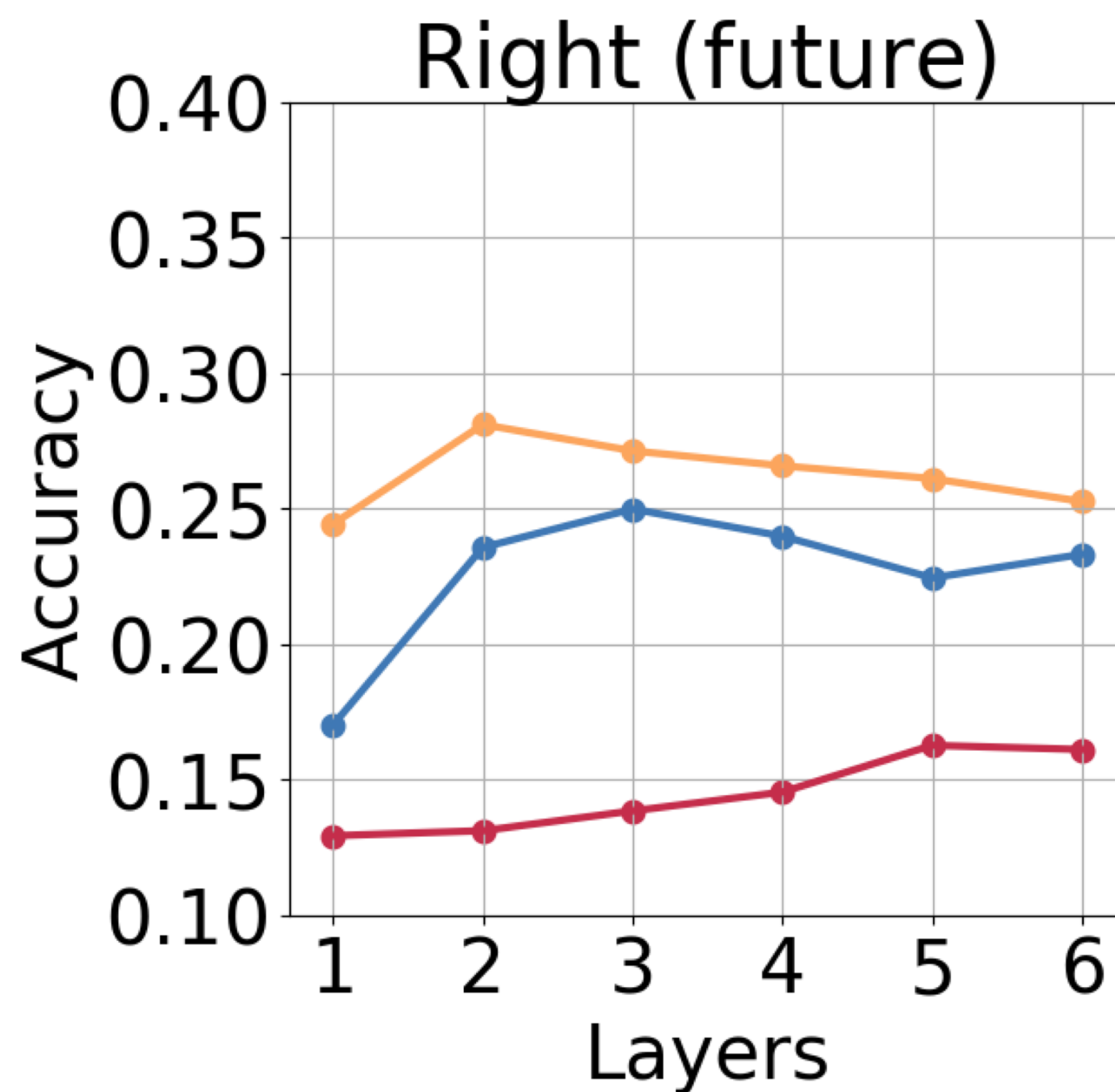
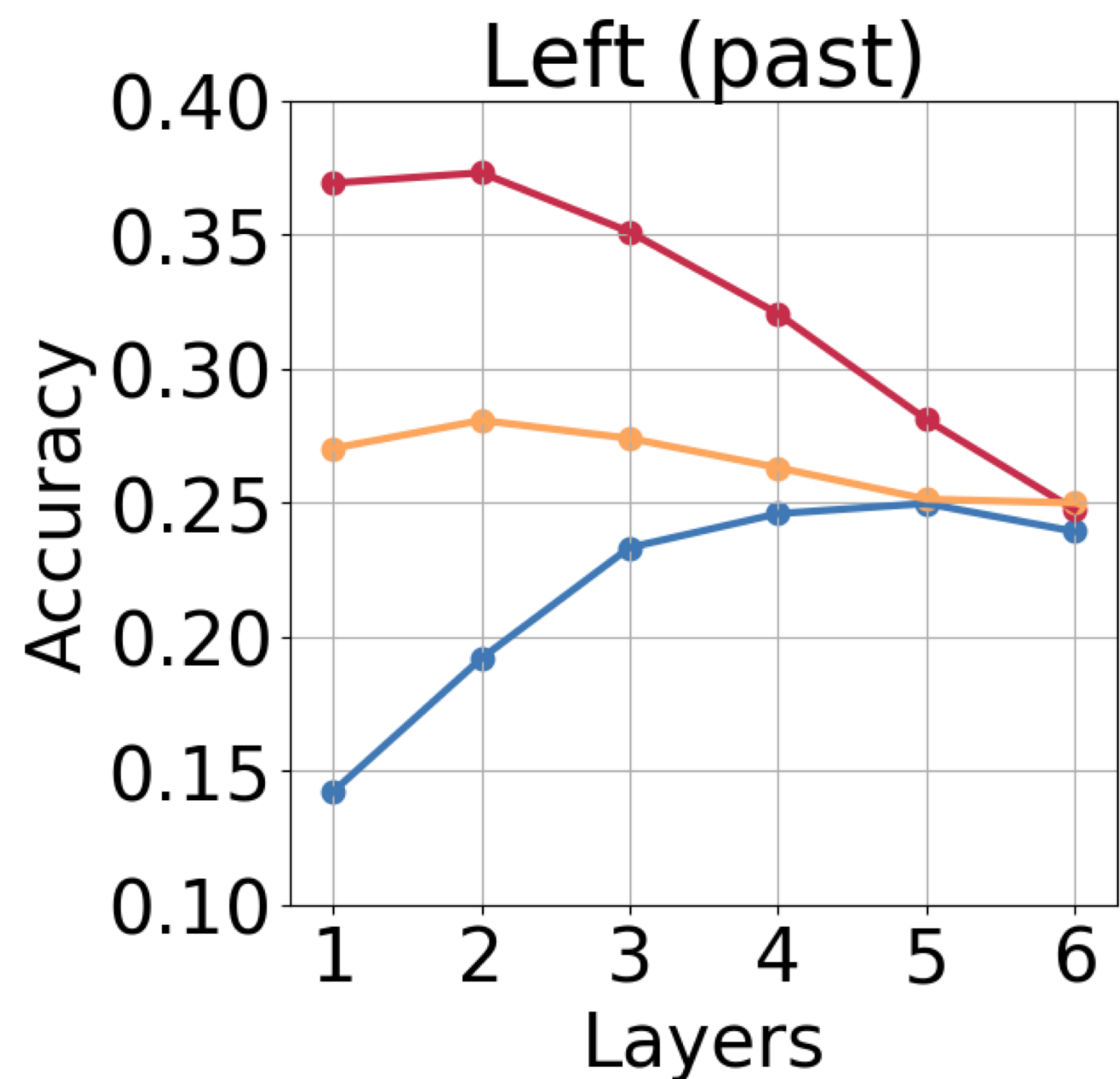
# What's next: lexical and syntactic context

We also look at:

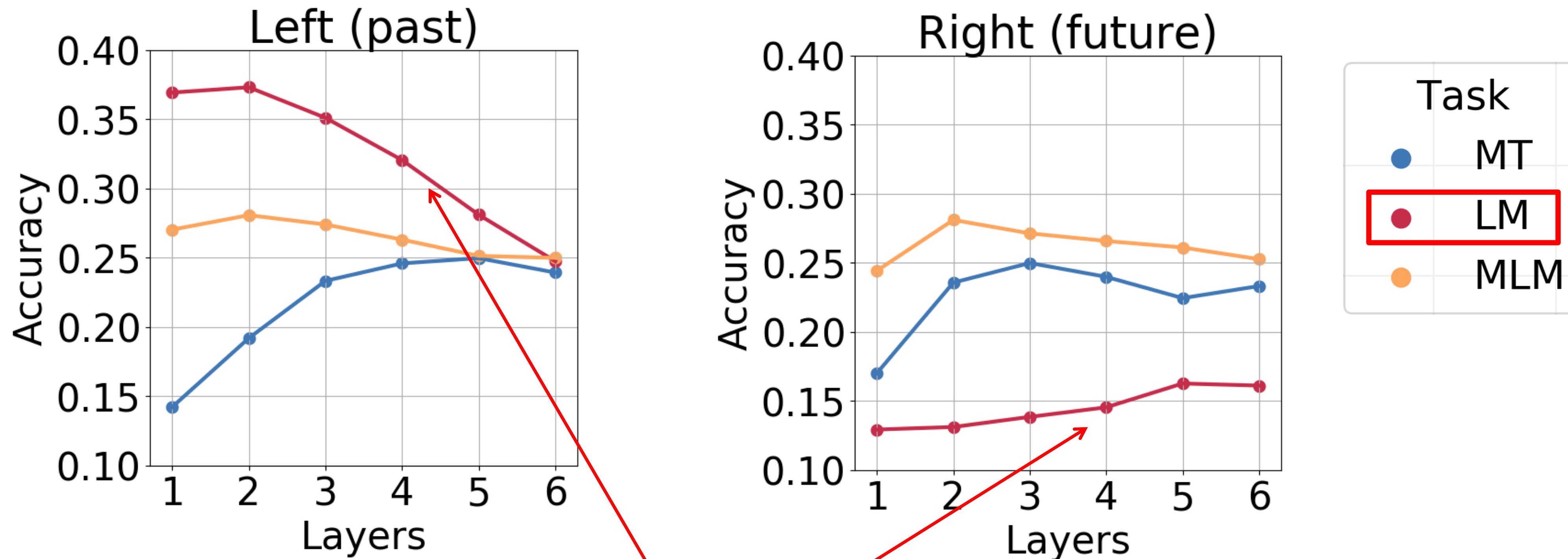
- Lexical context (identities of adjacent tokens)
- Syntactic context (CCG tags with their left/right parts)



# Lexical context (identities of adjacent tokens)

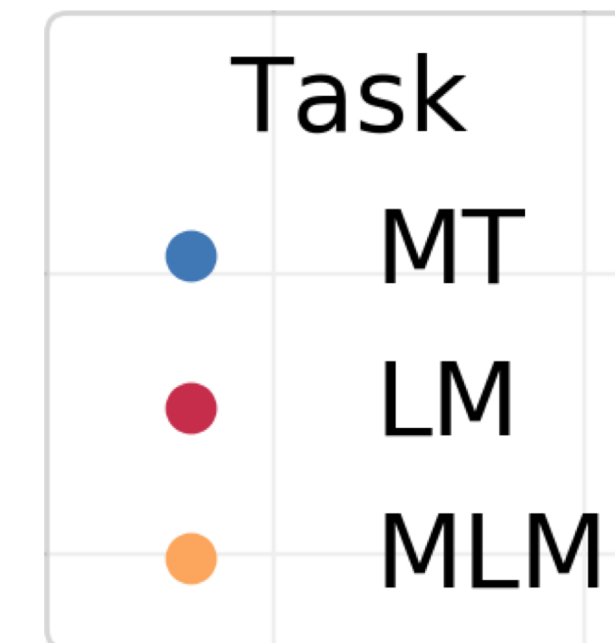
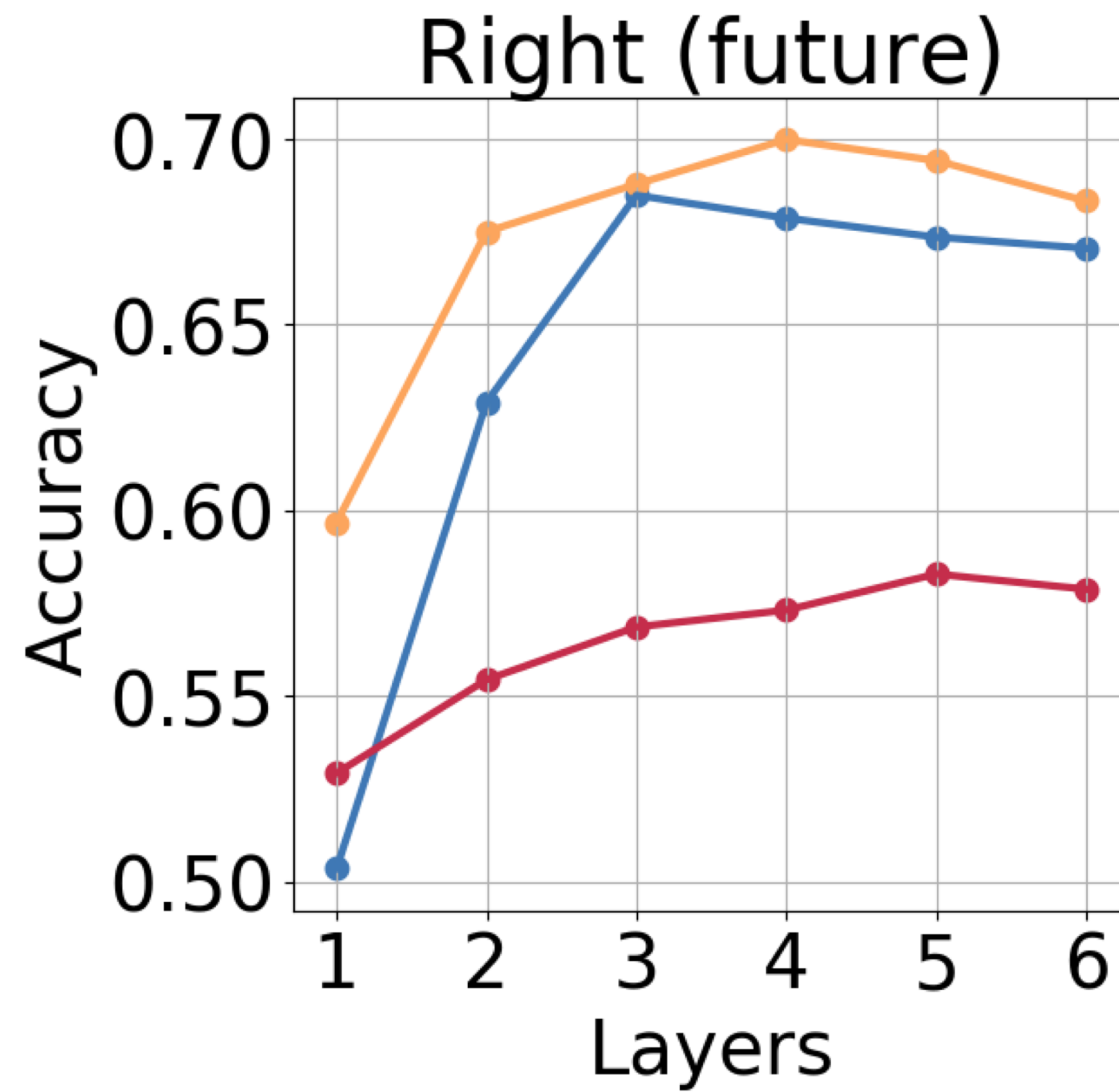
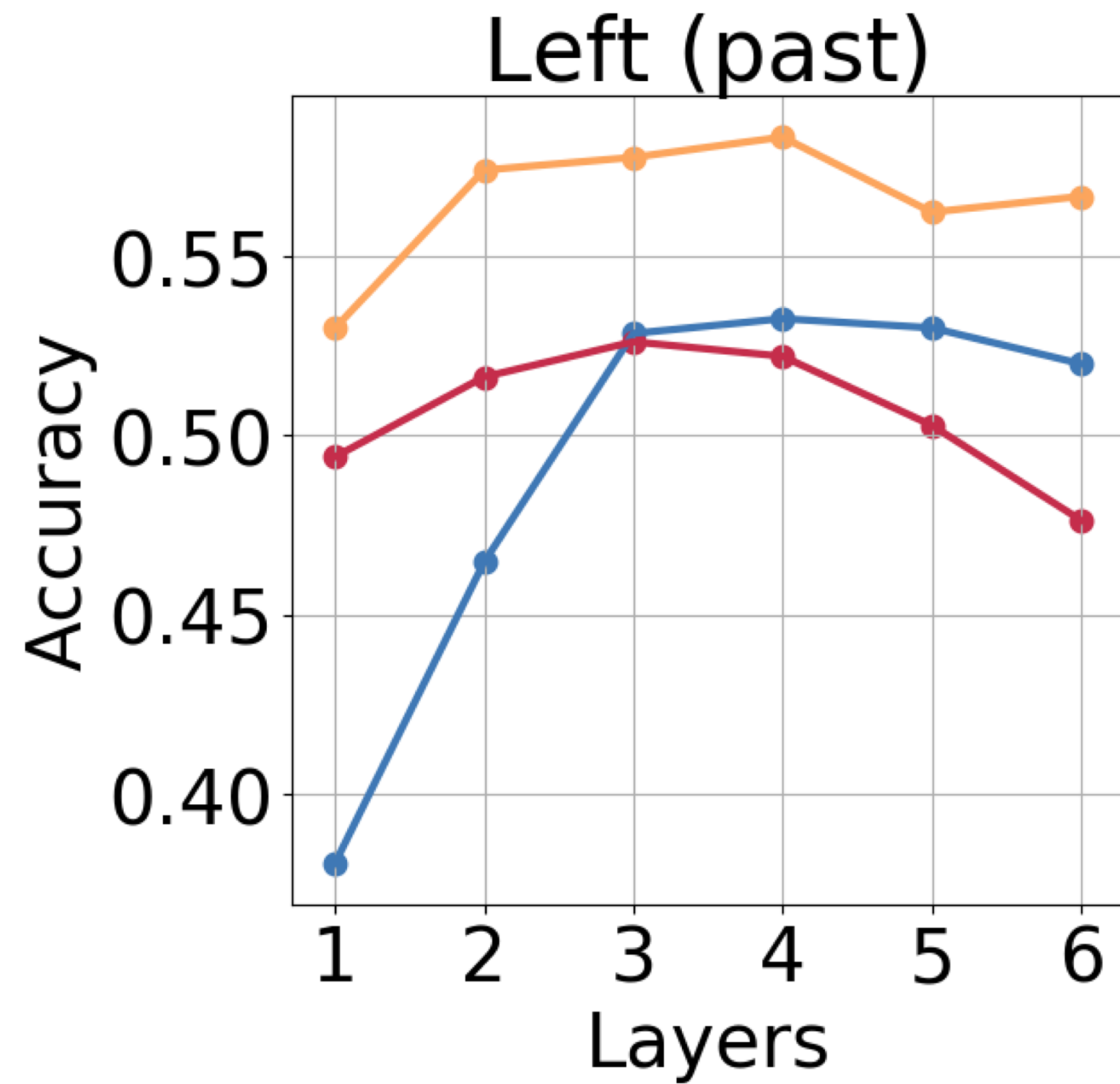


# Lexical context (identities of adjacent tokens)



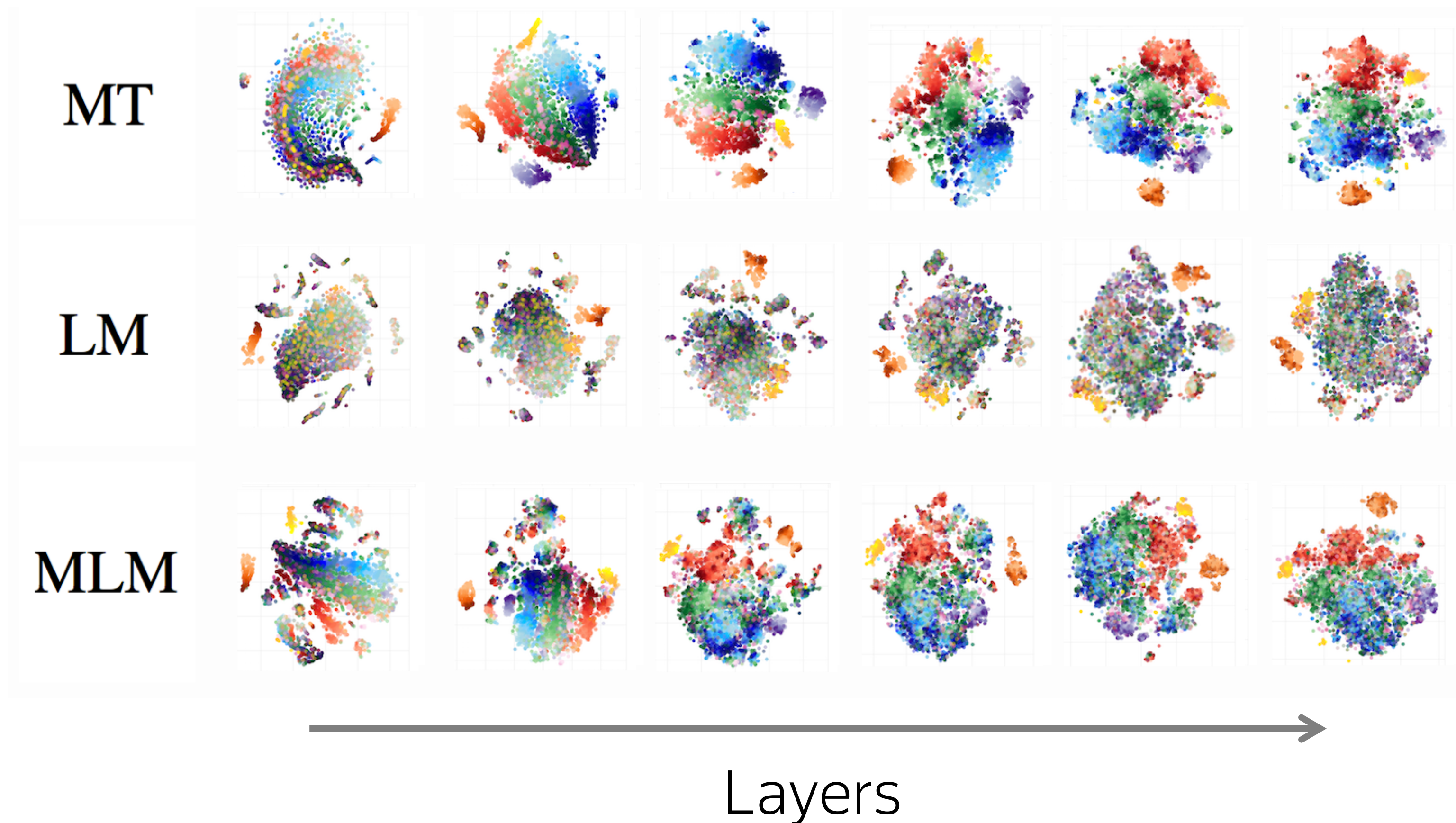
LM: forgets past, forms future

# Syntactic context (CCG tags)

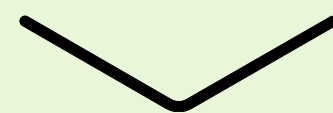


# Syntactic context (CCG tags)

- t-SNE of different occurrences of the token “is”. CCG tag is in color.



Relation to other works



# Previous work:

## Untrained LSTMs are better for token prediction

- Untrained LSTMs outperform trained ones for word identity prediction task (Zhang & Bowman, 2018)

# Previous work:

## MT behavior is monotonic, LM is not

- For constituent labeling prediction, MT shows monotonic behavior, while LM non-monotonic (Blevins et al, 2018)

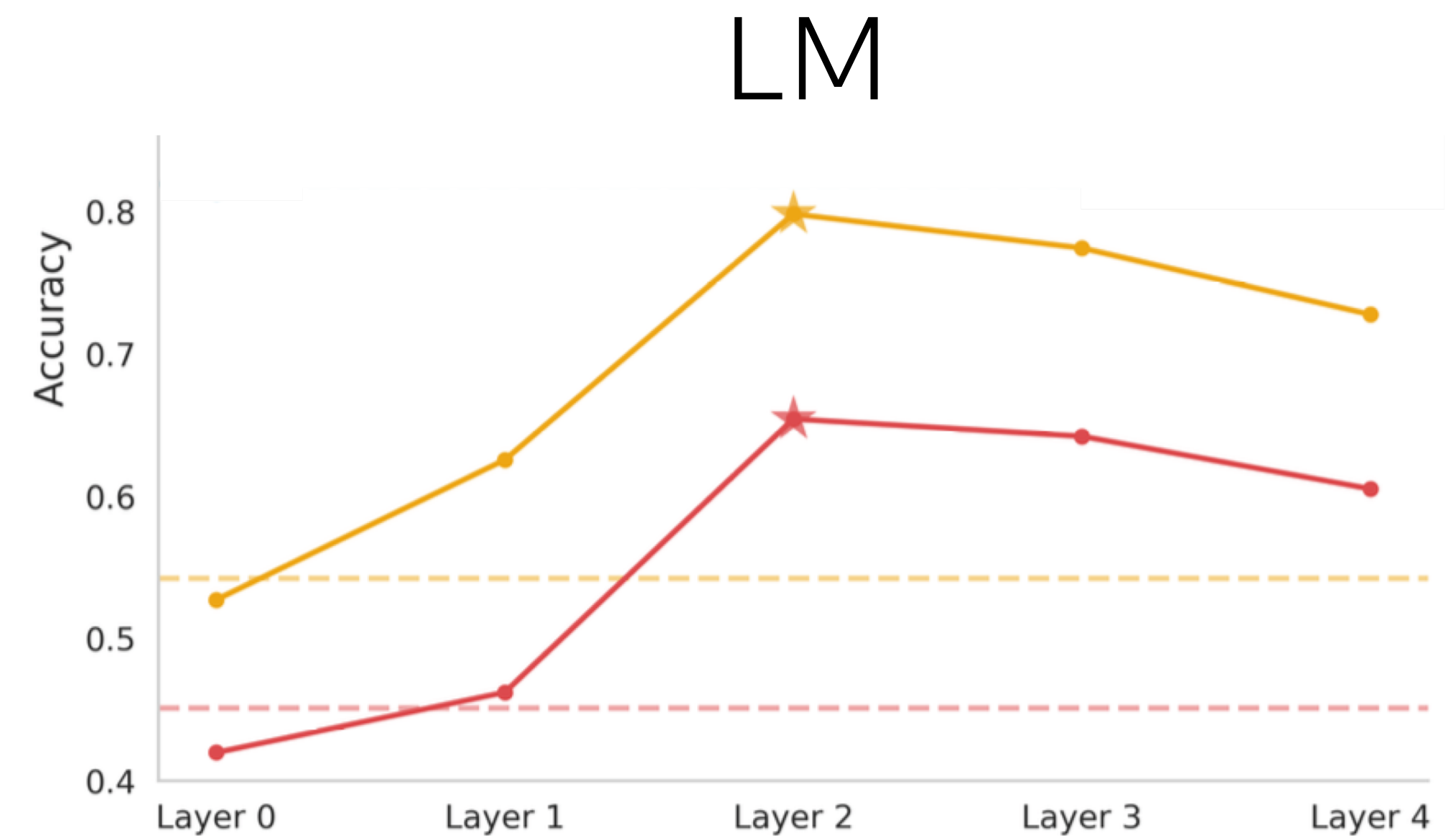
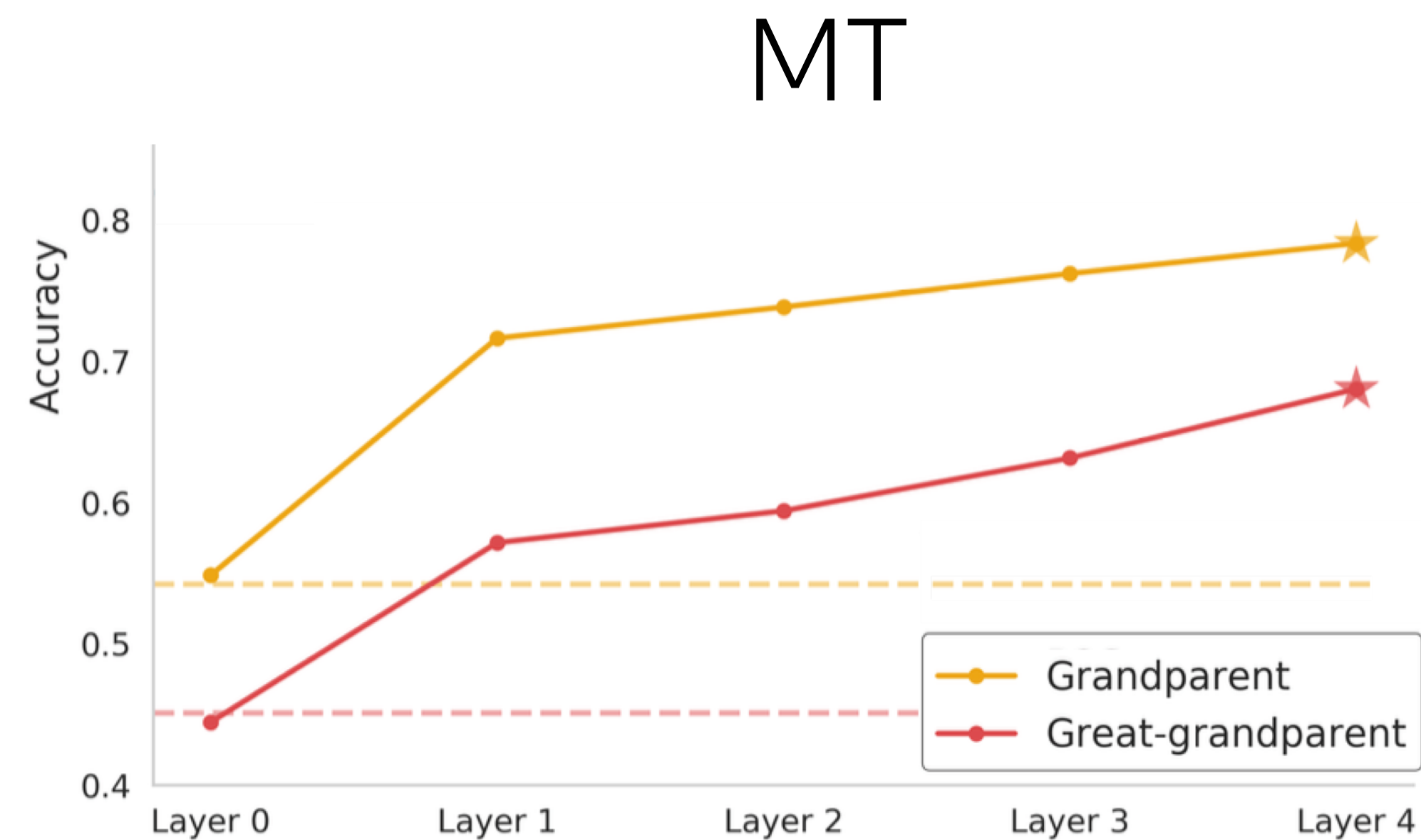


Illustration is from the original paper by Blevins et al, 2018

# Previous work:

## BERT behavior is not monotonic

- For different tasks the contribution of a layer to a task increases up to a certain layer, but then decreases at the top layers (Tenney et al, 2019)

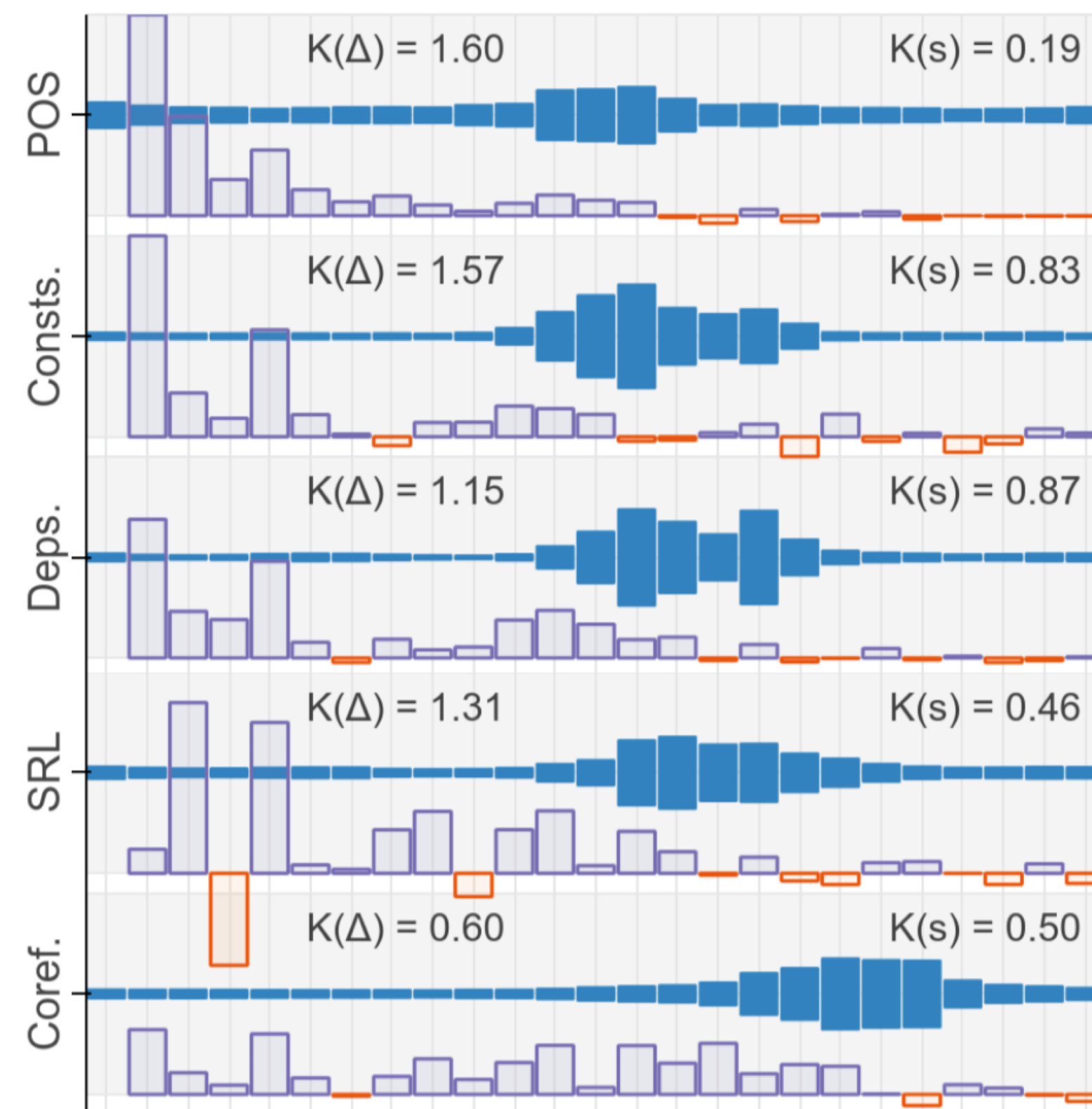


Illustration is from the original paper by Tenney et al, 2019



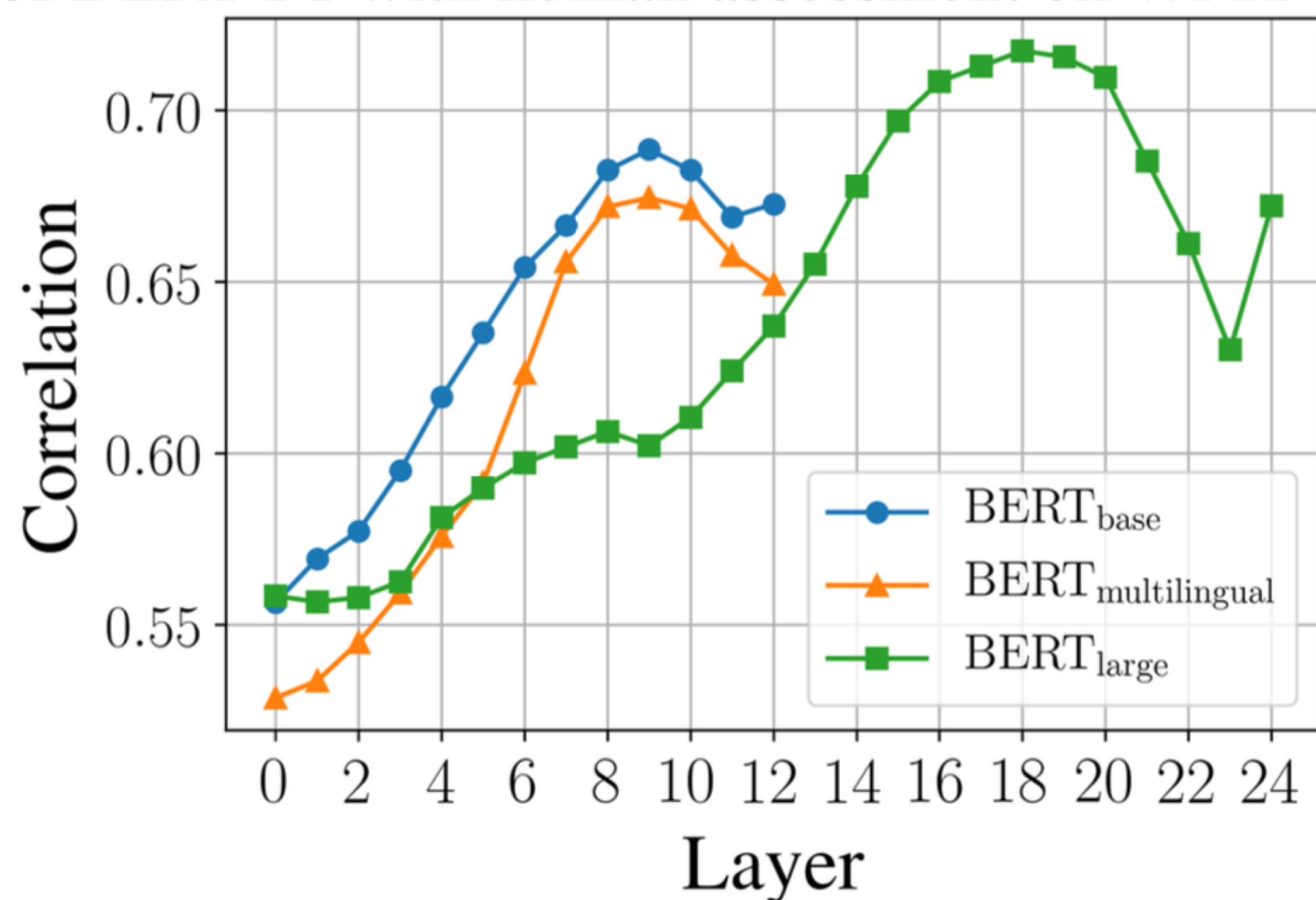
# Recent works

## BERTScore: Evaluating Text Generation with BERT

([Tianyi Zhang\\*](#), [Varsha Kishore\\*](#), [Felix Wu\\*](#), [Kilian Q. Weinberger](#), [Yoav Artzi](#), ICLR 2020)

- BERT representations are used to build a metric

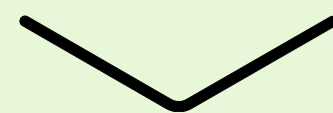
BERT models: Pearson Correlation of BERT-F1 with human assessment on WMT-16 to-en



The two stages:  
'context encoding' and  
'token reconstruction'

Illustration is from the original paper

# Conclusions



# Our key findings are:

- for LM, evolution is a transition from known past to the unknown future;
- MLMs initially acquire information about context, then recreate token; this happens in two stages;
- for MT, representations get refined with context, but most of the information is preserved.

# Our key contributions:

- we propose to view the evolution of a token representation from the compression/prediction trade-off perspective;
- we conduct a series of experiments supporting this view;
- we relate to some findings from previous work, putting them in the proposed perspective.

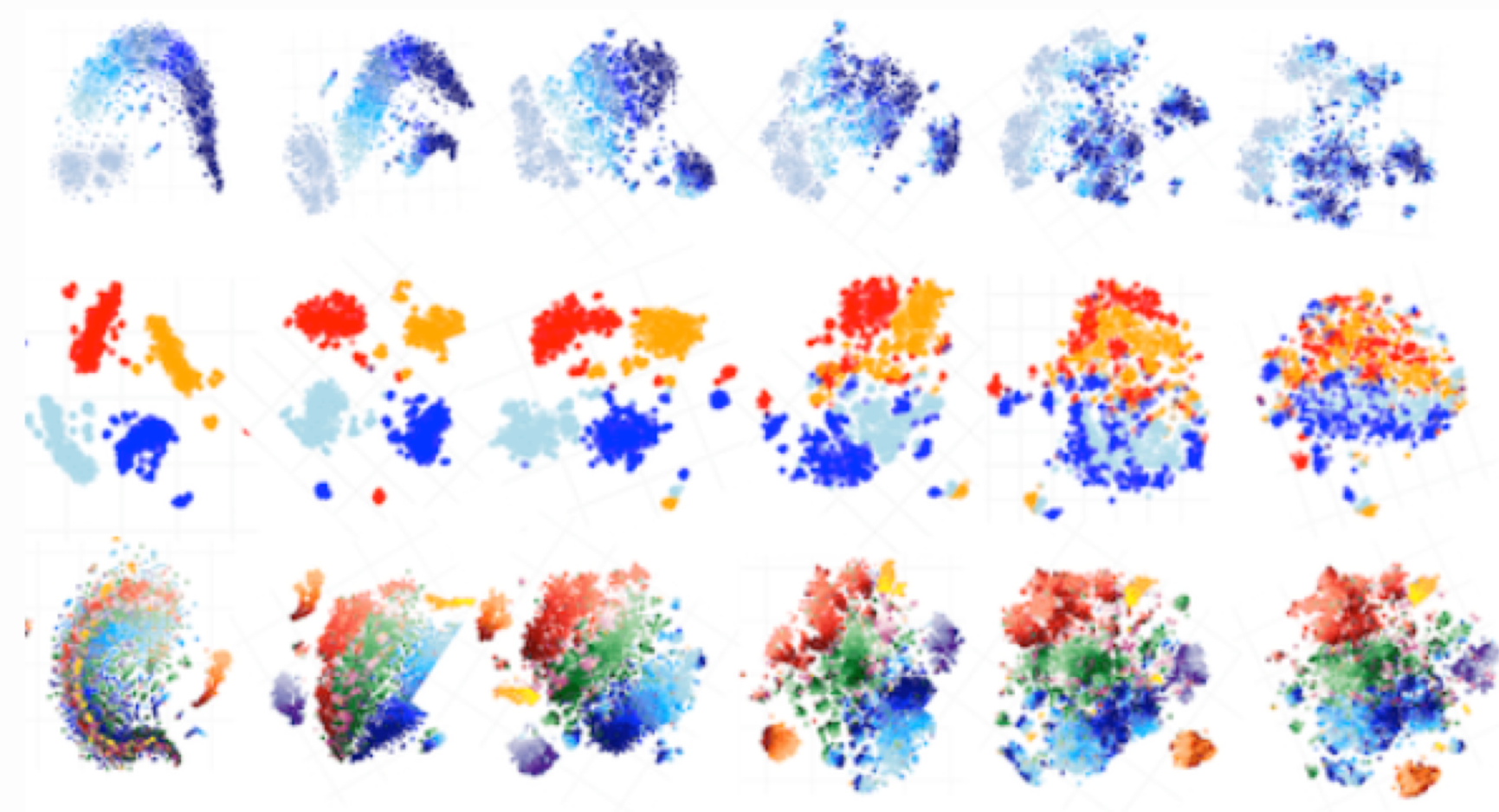
# Official blog post

## Evolution of Representations in the Transformer

This is a post for the EMNLP 2019 paper [The Bottom-up Evolution of Representations in the Transformer: A Study with Machine Translation and Language Modeling Objectives](#).

We look at the evolution of representations of individual tokens in Transformers trained with different training objectives (MT, LM, MLM - BERT-style) from the [Information Bottleneck](#) perspective and show, that:

- LMs gradually forget past when forming predictions about future;
- for MLMs, the evolution proceeds in two stages of **context encoding** and **token reconstruction**;
- MT representations get refined with context, but less processing is happening.



→☰ read more



read paper

September 2019

<https://lena-voita.github.io>

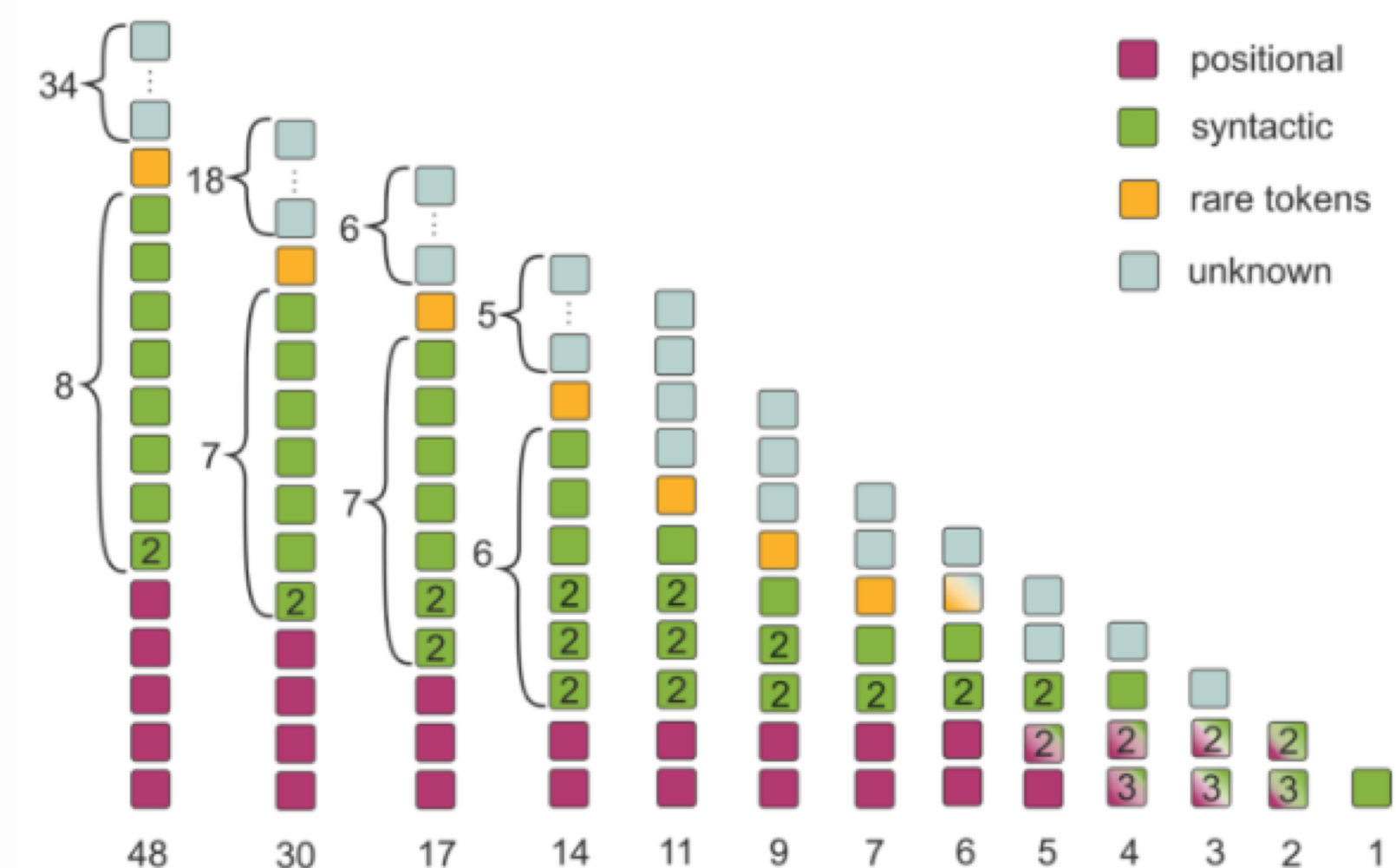
# More Analysis: The Story of Heads

## The Story of Heads

This is a post for the ACL 2019 paper [Analyzing Multi-Head Self-Attention: Specialized Heads Do the Heavy Lifting, the Rest Can Be Pruned](#).

From this post, you will learn:

- how we evaluate the importance of attention heads in Transformer
- which functions the most important encoder heads perform
- how we prune the vast majority of attention heads in Transformer without seriously affecting quality
- which types of model attention are most sensitive to the number of attention heads and on which layers



[→☰ read more](#)

[📄 read paper](#)

[</> view code](#)

June 2019

<https://lena-voita.github.io>

# Thank you!

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