



# A Deep Generative Model for Clickstream Analysis

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AMLD EPFL 2022, 28<sup>th</sup> March 2022

# Overview

## Problem

- In 2020, over 97% of global online shopping users **exited** the e-commerce websites **with no purchase**.
- E-commerce websites use **machine learning** to **detect when users are about to exit**, which helps them to trigger potential interventions:
  - Special coupons
  - Dynamic price promotions
- **Research question:** How can we detect the users who will exit with no purchase?

## Previous Works

Table 1: Overview of key literature for predicting user exits without purchase from clickstreams

Model	Long-term dependence	Latent states
LSTM [16, 32]	✓	
BiLSTM [39]	✓	
Mixture LSTM [31, 36]	✓	
HMM [5, 24]		✓
M3PP [11]		✓

- Variant of recurrent neural networks (RNN) to capture **long-term dependence** of the sequence of page clicks.
- Variant of Markov models to capture the **latent states** (i.e. latent shopping phases) of the users.

# Overview

## Problem

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## Our approach

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- We formalize a **tailored attentive deep Markov model** called (**ClickstreamDMM**) for detecting user exits without purchase.
- Our model is the first clickstream model that jointly learns both
  - **long-term** dynamics of the page clicks (via attention)
  - different **shopping phases** in clickstream setting (via a latent variable model).
- Our *ClickstreamDMM* consistently **outperformed** state-of-the-art algorithms in terms of
  - AUROC of 0.817 (**+11.5 %** improvement)
  - Based on **26,279 online sessions** provided by **Digitec Galaxus** (leading e-commerce platform in Switzerland).

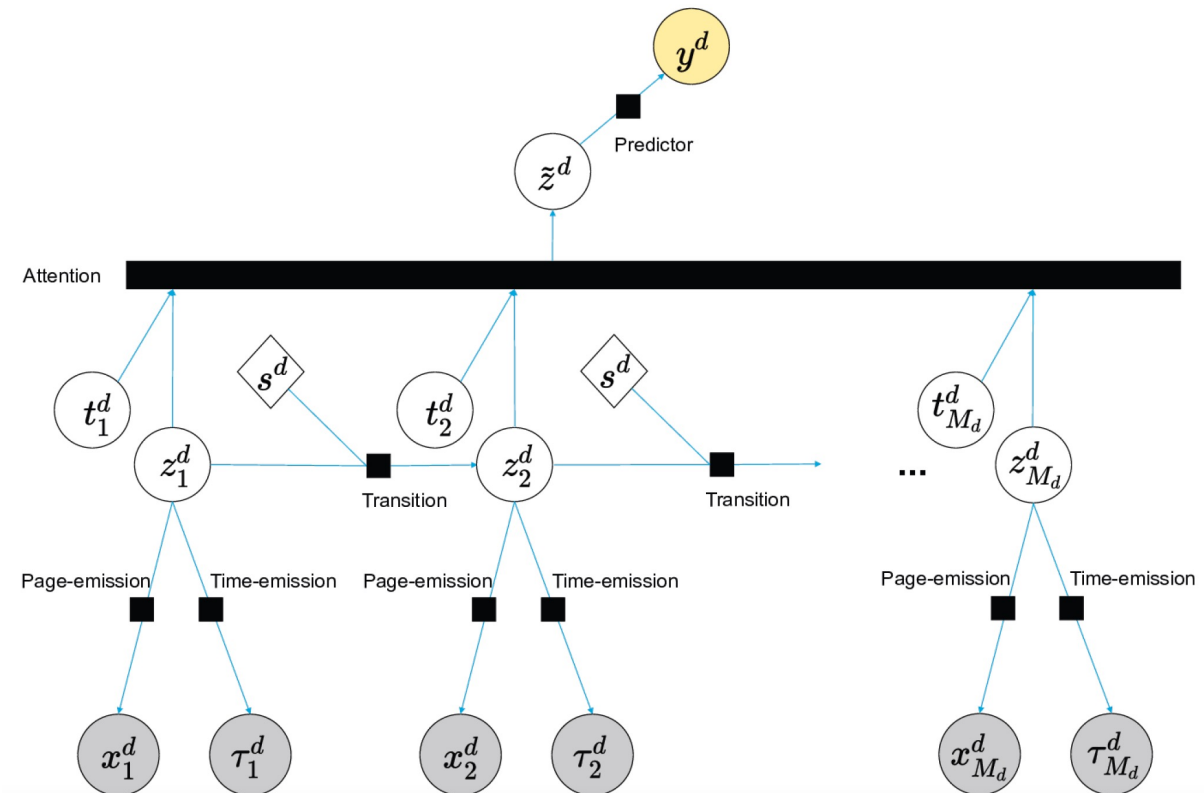
# Clickstream Data and Model

## Clickstream Data

- The dataset comprises a set of online sessions; each session is represented by **static** and **time-series** features.
  - Static features** encode user-level information (e. g., gender, age, account type), denoted by  $s$ .
  - Time-series** features encode the set of **page clicks**  $\{x_m\}_{m=1}^M$  and their associated **timestamps**  $\{t_m\}_{m=1}^M$ .
    - We further derive **time spent on a page (TSP)**  $\{\tau_m\}_{m=1}^M$ .
- For each online session, we predict whether the user will end the session with vs. without purchase  $y \in \{0,1\}$ .
  - $y = 0$  denotes no purchase,
  - $y = 1$  denotes purchase before the exit.

## Model

Figure 1: Model Architecture of *ClickstreamDMM*. Black squares denote neural networks.



# Clickstream Data and Model

## Components

- **Transition network** specifies transition probability among consecutive latent variables.

$$p(z_m | z_{m-1}, s)$$

- **Page-emission network** outputs the probability of a page click given the latent variable.

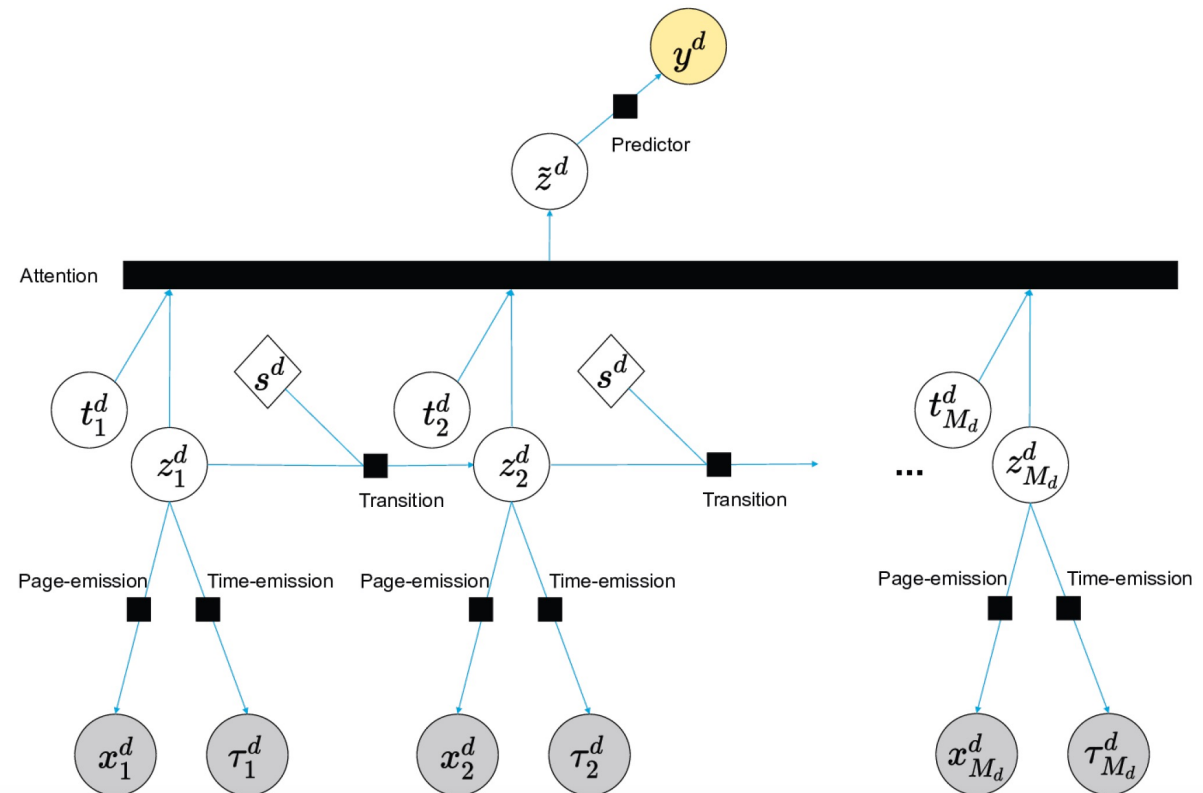
$$p(x_m | z_m)$$

- **Time-emission network** outputs the probability of time spent on the page (TSP) given the latent variable.

$$p(\tau_m | z_m)$$

## Model

Figure 1: Model Architecture of *ClickstreamDMM*. Black squares denote neural networks.



# Clickstream Data and Model

## Components

- **Attention network** allows the model to assign a different importance to each latent variable when making inferences of purchase probability.

$$z'_m = \tanh(W_{z'} z_m + b_{z'}),$$

$$\gamma_m = \frac{\exp(K(v, z'_m)) / (t_M + 1 - t_m)^\beta}{\sum_{m'=1}^M \exp(K(v, z'_{m'})) / (t_M + 1 - t_{m'})^\beta},$$

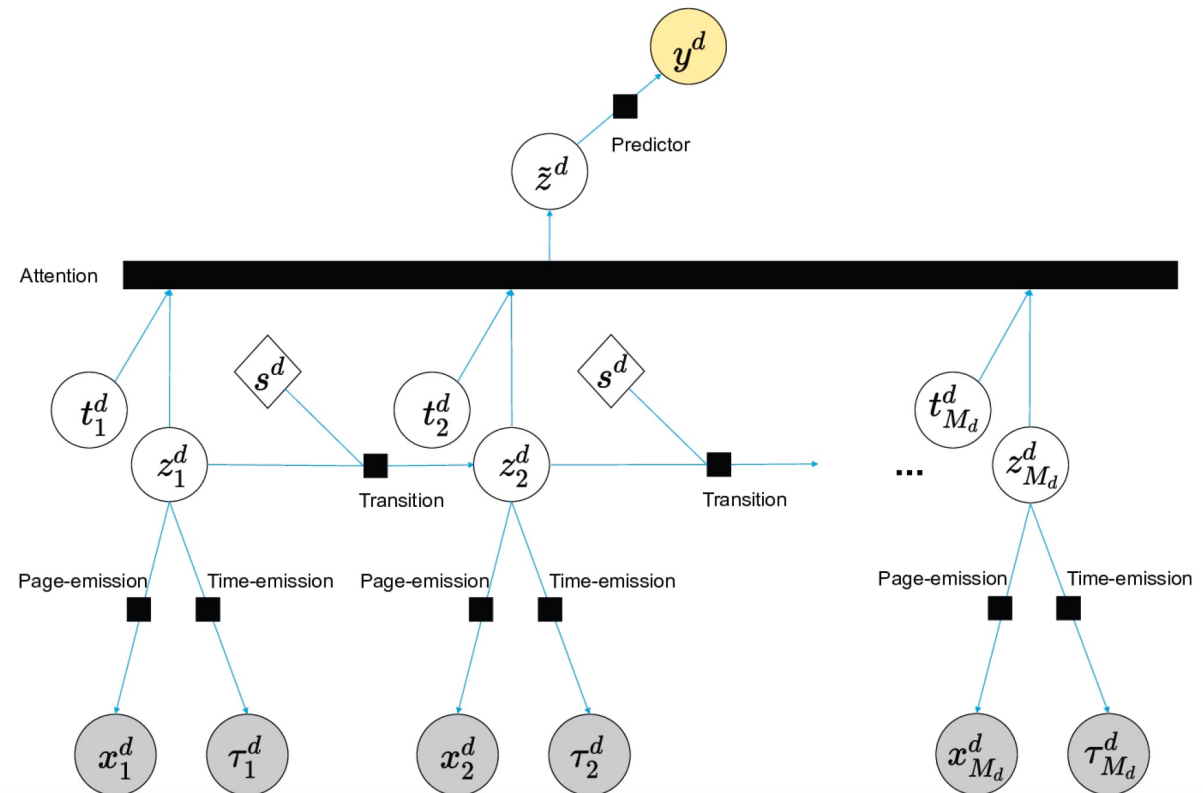
$$\tilde{z} = \sum_{m=1}^M \gamma_m z_m$$

- **Predictor network** is the final step of making the inference of purchase probability.

$$\hat{y} = \text{sigmoid}(U_y \text{ReLU}(W_y \tilde{z} + b_y) + c_y)$$

## Model

Figure 1: Model Architecture of *ClickstreamDMM*. Black squares denote neural networks.



# Results

## Purchase prediction with early warnings

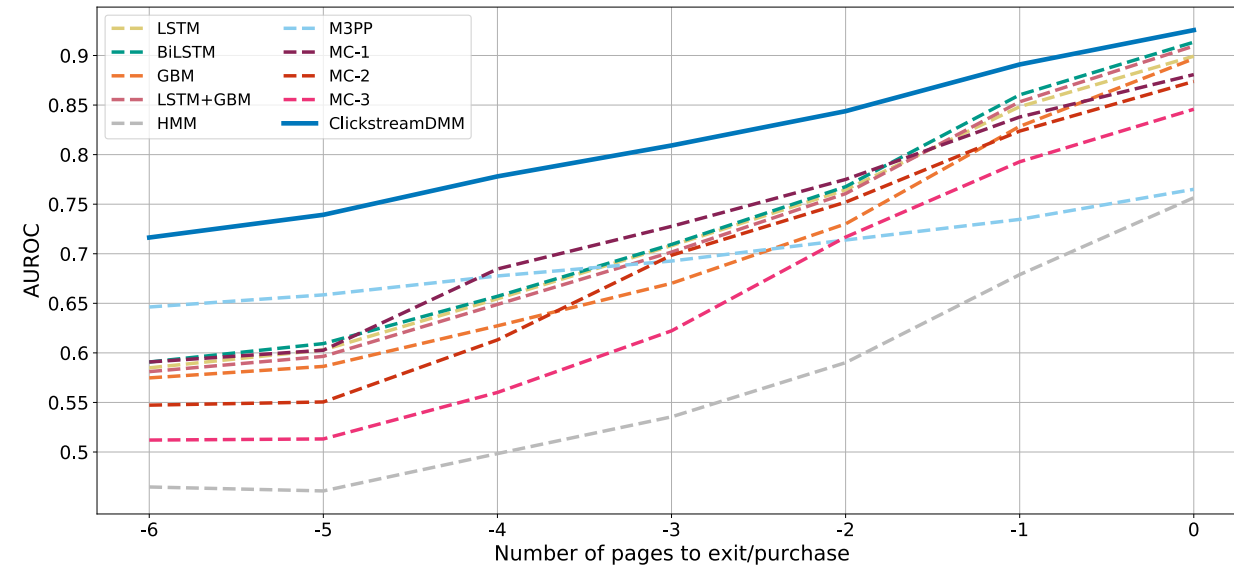
Table 2: The risk of exiting with no purchase is estimated starting from  $n = 6$  pages ahead to exit

Model	AUROC	AUPRC
LSTM [16, 32]	$0.726 \pm 0.014$	$0.472 \pm 0.012$
BiLSTM [39]	$0.733 \pm 0.017$	$0.497 \pm 0.015$
GBM	$0.705 \pm 0.006$	$0.500 \pm 0.011$
LSTM+GBM [16]	$0.725 \pm 0.011$	$0.505 \pm 0.012$
HMM [5, 24]	$0.572 \pm 0.005$	$0.259 \pm 0.003$
M3PP [11]	$0.701 \pm 0.012$	$0.447 \pm 0.012$
MC-1 [18]	$0.732 \pm 0.006$	$0.484 \pm 0.009$
MC-2 [18]	$0.697 \pm 0.007$	$0.456 \pm 0.010$
MC-3 [18]	$0.655 \pm 0.009$	$0.407 \pm 0.011$
<b>ClickstreamDMM (ours)</b>	<b><math>0.817 \pm 0.007</math></b>	<b><math>0.569 \pm 0.013</math></b>

Higher is better. Best value in bold.

## Illustration

Figure 2: Prediction performance when making predictions  $n = 6$  pages ahead to exit





## Conclusion

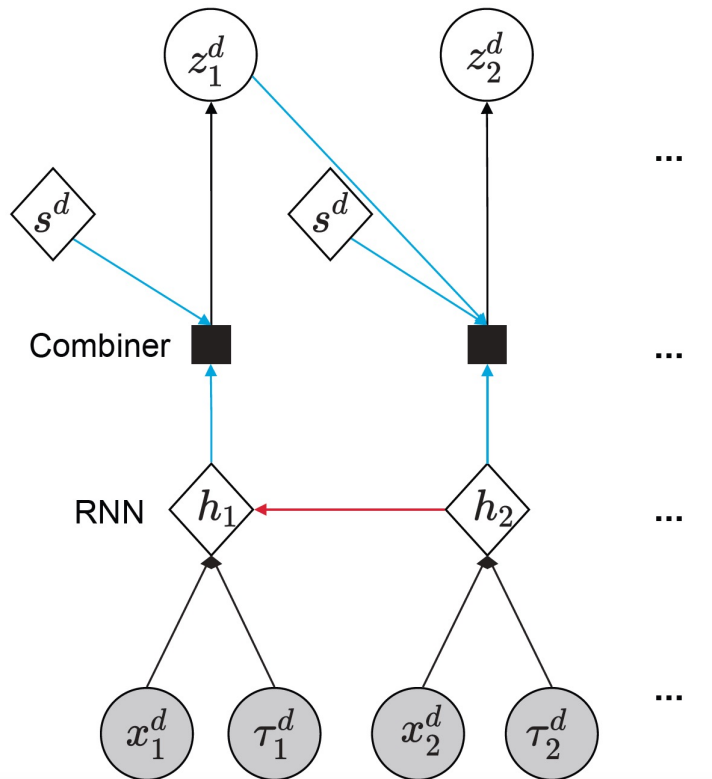
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- **Theory informed model:** *ClickstreamDMM* jointly captures **long-term dependence** of page clicks (via an attention network) and **different latent shopping phases** of users (via a latent variable model).
  - **Performance:** *ClickstreamDMM* is particularly effective when predictions are made multiple pages ahead. This is needed upon deployment, so that early warnings are generated to trigger marketing interventions.
  - **Generalizability:** *ClickstreamDMM* can be applied to other settings where time-series data has long-term dependencies and are driven by latent dynamics, such as healthcare analytics or churn prediction.
- Don't forget to check our paper ***A Deep Markov Model for Clickstream Analytics in Online Shopping*** in the ACM Web Conference 2022 (**WWW '22**).



## Posterior Approximation

Figure 3: Posterior Approximation of *ClickstreamDMM*. Black squares denote neural networks.



- Posterior distribution of the latent variables is approximated as

$$q(z_{1:M} \mid x_{1:M}, \tau_{1:M}, s) = \prod_{m=1}^M q(z_m \mid z_{m-1}, x_{1:M}, \tau_{1:M}, s)$$

- The formula above is further simplified as

$$q(z_m \mid z_{m-1}, x_{1:M}, \tau_{1:M}, s) = q(z_m \mid z_{m-1}, x_{m:M}, \tau_{m:M}, s)$$

## Loss Function

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- *ClickstreamDMM* minimizes the following loss

$$\mathcal{L}(y, \hat{y}, \mathcal{S}) = \ell(y, \hat{y}) - \alpha \text{ELBO}(\mathcal{S}).$$

as a combination of

- **Cross-entropy loss**

$$\ell(y, \hat{y}) = -\rho y \log(\hat{y}) - (1 - y) \log(1 - \hat{y})$$

- **Evidence Lower Bound (ELBO)**

$$\begin{aligned} \text{ELBO}(\mathcal{S}) = & \mathbb{E}_{q(z_{1:M} | x_{1:M}, \tau_{1:M}, s)} [\log p(x_{1:T}, \tau_{1:T} | z_{1:T})] \\ & - \text{KL}(q(z_{1:M} | x_{1:M}, \tau_{1:M}, s) || p(z_{1:M})). \end{aligned}$$

## Visualization of Latent Variables

Figure 4: Clustering of latent variables

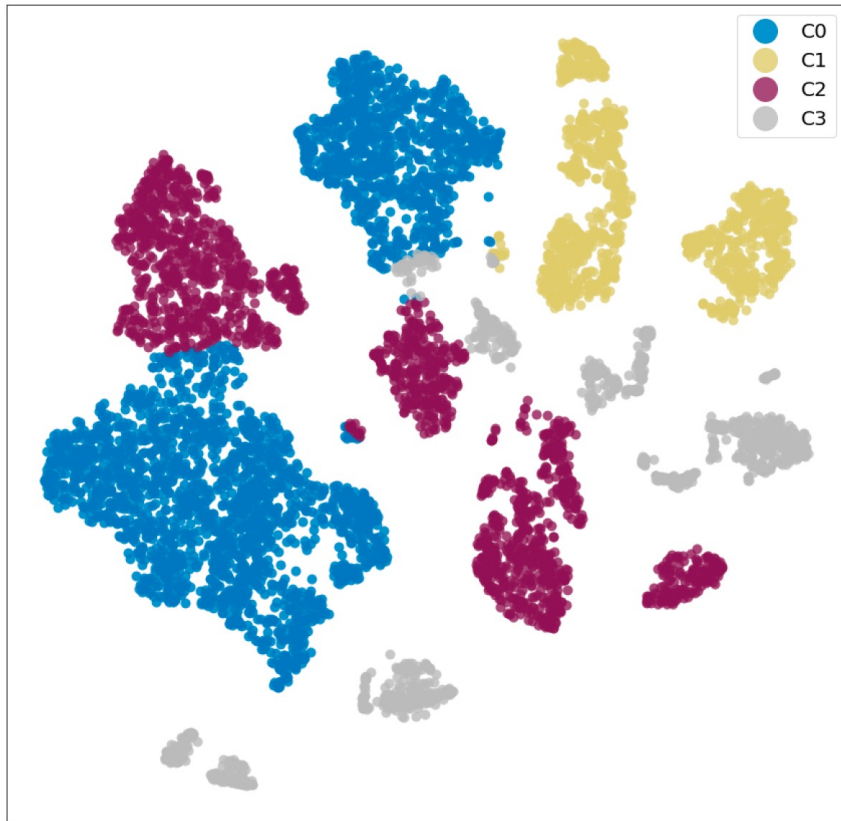
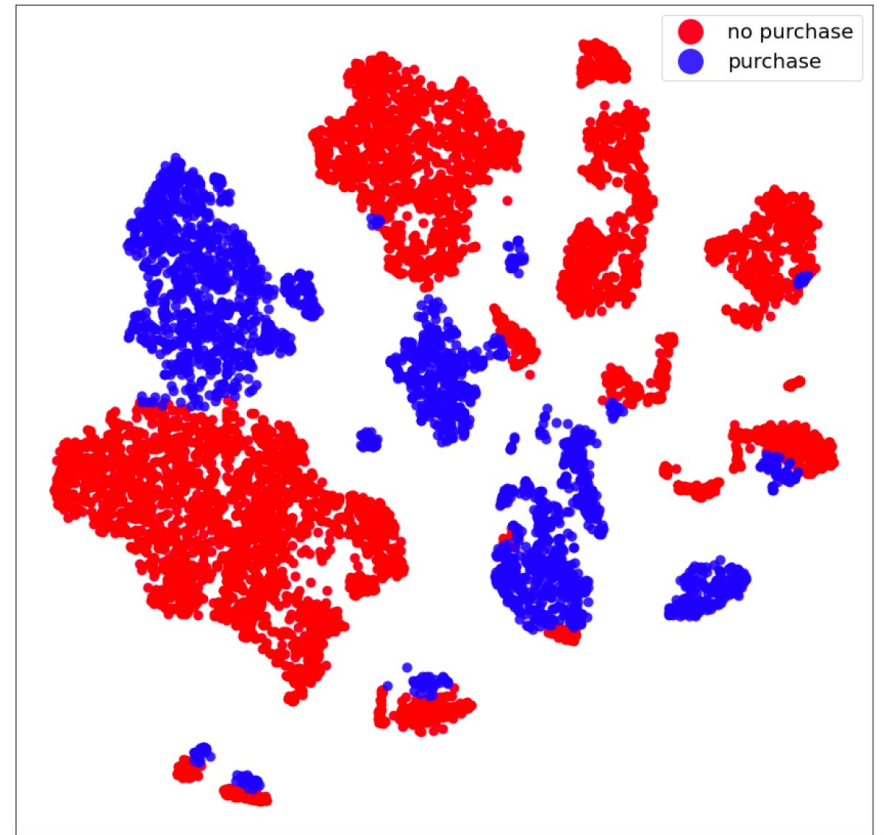


Figure 5: Latent variables of sessions with and without purchase



## Characteristics of Clusters

Figure 6: Relative frequency of page clicks by cluster (in %)

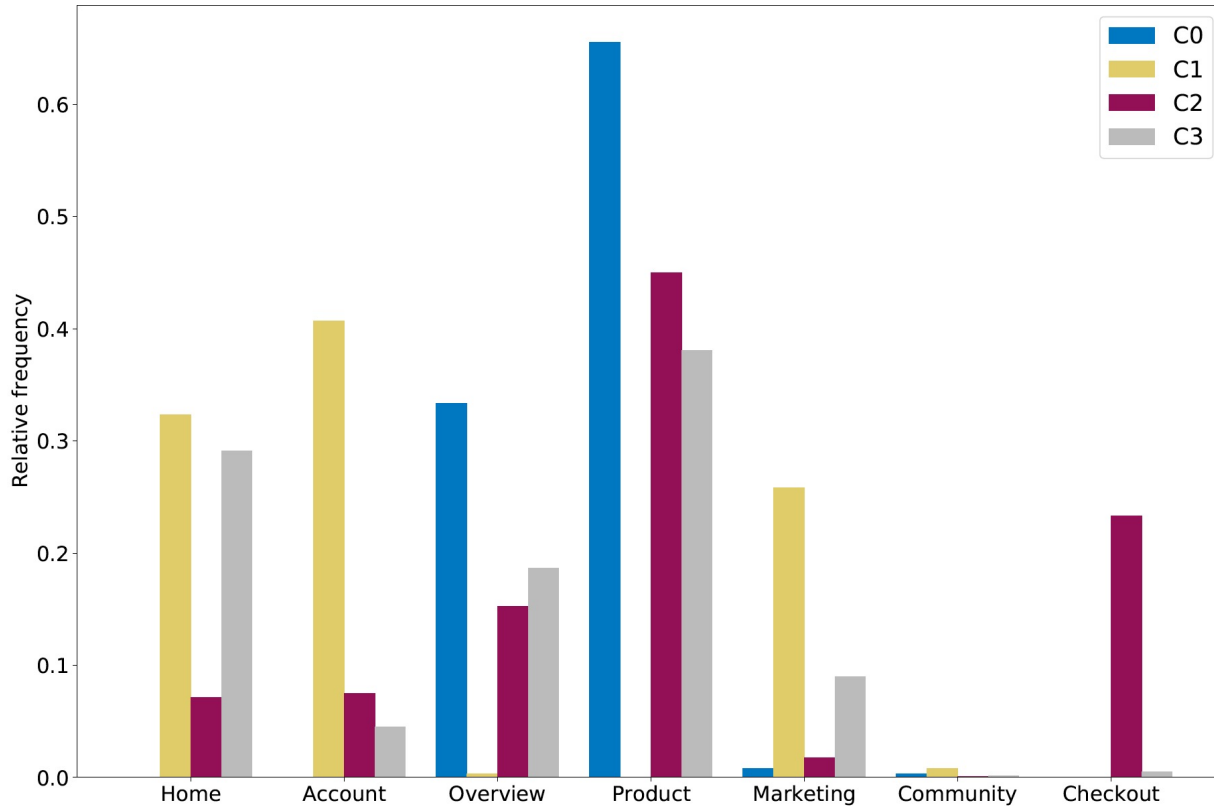


Figure 7: Transition matrix between clusters (left: current, top: next)

